

# RESIDENTIAL SEGREGATION IN GENERAL EQUILIBRIUM<sup>1</sup>

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March 2004

## Abstract

This paper studies the causes and consequences of racial segregation using a new general equilibrium model that treats neighborhood compositions as endogenous. The model is estimated using unusually detailed restricted Census microdata covering the entire San Francisco Bay Area, and in combination with a rich array of econometric estimates, serves as a powerful tool for carrying out counterfactual simulations that shed light on the causes and consequences of segregation. In terms of causes, and contrasting with prior research, our GE simulations indicate that equalizing income and education across race would be unlikely to result in significant reductions in racial segregation, as minority households would sort into newly formed minority neighborhoods. Indeed, among Asian and Hispanic households, segregation increases. In terms of consequences, this paper provides the first evidence that sorting on the basis of race gives rise to significant reductions in the consumption of local public goods by minority households and upper-income minority households in particular. These consumption effects are likely to have important intergenerational implications.

*Keywords:* segregation, general equilibrium, endogenous sorting, urban housing market, locational equilibrium, counterfactual simulation, discrete choice. (*JEL:* H0, J7, R0, R2)

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<sup>1</sup> We would like to thank Fernando Ferreira for outstanding research assistance. Thanks also to Pedro Cerdan and Jackie Chou for help in assembling the data. We are grateful to Pat Bajari, Steve Berry, Dennis Epple, Tom Nechyba, Holger Sieg and Chris Timmins for many valuable discussions, and to Joe Altonji, Gregory Besharov, Maureen Cropper, David Cutler, James Heckman, Vernon Henderson, Phil Leslie, Costas Meghir, Robert Moffitt, Michael Riordan, Steve Ross, Kerry Smith, Jon Sonstelie, Chris Taber, Chris Udry, and Jacob Vigdor for additional valuable comments. We also thank conference participants at the AEA, ERC, IRP, NBER, PET, SITE, and SIEPR, and seminar participants at Brown, Chicago, Colorado, Columbia, Duke, Johns Hopkins, Northwestern, NYU, PPIC, Stanford, Toronto, UC Berkeley, UC Irvine, UCLA, and Yale for useful suggestions. This research was conducted at the California Census Research Data Center; our thanks to the CCRDC, and to Ritch Milby in particular. We gratefully acknowledge financial support for this project provided by the National Science Foundation under grant SES-0137289 and by the Public Policy Institute of California.

# 1 INTRODUCTION

Residential segregation on the basis of race and ethnicity is a phenomenon present in every metropolitan area throughout the United States.<sup>1</sup> Given its pervasive nature, the causes and consequences of segregation have attracted considerable academic scrutiny. Researchers investigating the underlying causes have attempted to assess the extent to which racial segregation can be explained by differences in income, wealth, and education across race;<sup>2,3</sup> in terms of consequences, a number of papers have explored the effects of living in a segregated neighborhood on individual outcomes.<sup>4</sup>

This paper studies the causes and consequences of segregation from a new perspective. The primary economic analysis builds on a series of theoretical papers that have analyzed residential sorting in a general equilibrium setting. Important examples include work by Epple, Filimon and Romer (1984, 1993), Benabou (1993, 1996), Fernandez and Rogerson (1996, 1998), and Nechyba (1999, 2000). All feature models with multiple communities, heterogeneous agents who are mobile across communities, and community compositions that are endogenous to the sorting process. As these papers demonstrate, general equilibrium sorting models provide a coherent framework for analyzing interdependent individual decisions that drive aggregate outcomes,<sup>5</sup> proving particularly useful in tracing the complex and otherwise difficult-to-predict effects of policy. Thus Fernandez and Rogerson (1996) provide a tractable analytical framework for examining the effects of school finance reforms that both change school funding and alter household location decisions. In a more complex setting, Nechyba (2000) sets out a computational model that explores the effects of school vouchers using general equilibrium simulations, allowing for households to choose schools and relocate across neighborhoods. In

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<sup>1</sup> In the year 2000, for example, black households in the Detroit metropolitan area lived in Census tracts that were on average almost 80 percent black and only 15 percent white, while in marked contrast, white households lived in Census tracts that were only 5 percent black and 90 percent white. In the San Francisco Bay Area, where racial divisions might seem less severe, the typical black household lives in a neighborhood with more than nine times the fraction of black households found in neighborhoods resided in by the typical white household.

<sup>2</sup> See Massey and Denton (1987, 1989, 1993), Miller and Quigley (1990), Harsman and Quigley (1995), Borjas (1998) and Bayer, McMillan, and Rueben (2004a), among others.

<sup>3</sup> A related body of work has explored whether racial segregation is driven by the decentralized preferences of households as they make their residential location decisions or by some form of centralized discrimination. Cutler, Glaeser, and Vigdor (1999) examine segregation patterns over the full course of the 20<sup>th</sup> century, concluding that centralized racism was much more important in driving segregation in the earlier part of the century. Other notable papers include King and Mieszkowski (1973), Yinger (1978), Schafer (1979), and Kiel and Zabel (1996).

<sup>4</sup> See Borjas (1995) and Cutler and Glaser (1997) for important contributions.

<sup>5</sup> Epple, Filimon and Romer (1984, 1993) focus on conditions needed to prove existence in multi-community models that incorporate voting.

both papers, allowing for mobility gives rise to effects in general equilibrium that would not be apparent in partial equilibrium, where household sorting is abstracted from.

In common with the applied theory literature, the current paper also specifies a general equilibrium multi-community model that treats neighborhood compositions as endogenous. However, it explores the potential of equilibrium sorting models in a new direction, analyzing locational equilibria in actual metropolitan areas. This gives rise to two differences relative to prior literature. In terms of the sorting model itself, we provide a very rich parameterization of household preferences, allowing the household location decision to be driven by a wide range of potentially relevant choice characteristics, including endogenous characteristics such as the race of one's neighbors – the rich data we have access to make this feasible. The model permits household preferences to vary in a very flexible way with observable household characteristics, so that households of different races can place a different valuation on having neighbors of a given race – a horizontal model is natural in this context.<sup>6</sup>

Second, while prior work has typically used an analytic approach or relied on calibration of a few main parameters, we estimate a wide range of demand parameters directly using unusually detailed restricted Census microdata. These cover the entire San Francisco Bay Area, providing a wealth of household characteristics and detailed information on household locations and characteristics of neighbors. Our estimation approach draws on the notion of revealed preference: examining actual location decisions vary on average with household characteristics, one can learn how preferences for housing and neighborhood attributes vary with these characteristics. An important feature of our approach is that it accounts for an important endogeneity problem arising due to the correlation of neighborhood sociodemographics with unobserved housing and neighborhood quality. Among the rich array of preference estimates that we recover, it is clear that racial interactions in the utility function are powerful.

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<sup>6</sup> As noted in Epple, Filimon and Romer (1993), there is an important tradeoff to be made between incorporating voting in multiple-community models on the one hand and abstracting from the political process entirely on the other. The inclusion of voting necessitates restrictions to be placed on preferences in order to ensure existence of an equilibrium. Important recent papers by Epple and Sieg (1999) and Epple, Romer and Sieg (2001) estimate equilibrium models that include voting over the level of public goods, restricting households to have shared rankings over a single public goods index. In this paper, we abstract from the political process to focus on racial segregation, a phenomenon that is primarily the product of decentralized location decisions made by heterogeneous households. Doing so allows us to specify preferences in a very flexible way. We also note that in a Californian context, state financing of education has left relatively little discretion over public goods determination at the local level.

In combination with these econometric estimates, our equilibrium sorting model provides a powerful tool for shedding new light on the causes and consequences of residential segregation in a general equilibrium setting. We address two hypotheses, prompted by a striking empirical observation: neighborhoods with both a high fraction of minority households and even moderate levels of income (and education) tend to be in relatively short supply in many metropolitan areas - this is readily apparent from Table 12 below. The short supply of such neighborhoods implies that a household's choice of neighborhood along other dimensions, including school quality, neighborhood income and education, is often tied together very explicitly with race. This has the effect of raising the implicit price that minority households pay for these neighborhood amenities, as consuming more of these neighborhood amenities typically requires living in a neighborhood with fewer minorities, while the opposite is typically true for white households.<sup>7</sup>

Our first hypothesis, prompted by the short supply problem, relates to the causes of segregation. The previous literature universally suggests that an elimination of racial differences in income, wealth, or education would decrease segregation: we hypothesize that segregation could in fact increase once general equilibrium considerations are taken into account. In particular, as minority households move up the income distribution, the distribution of available neighborhoods will necessarily change. Because predominantly minority neighborhoods with even moderate income and education levels are in short supply in most metropolitan areas and would presumably be desirable to minority households, the increased formation of such neighborhoods could lead to increasing segregation among minorities, working against any segregation reduction due to the more even distribution of sociodemographic characteristics across race.

A natural way to address this hypothesis is to compare the current equilibrium and a new equilibrium in which racial differences in important socio-demographics have been eliminated. We accomplish this using counterfactual simulations that shift many minority households up the income distribution and then calculate a new sorting equilibrium for the entire metropolitan area, allowing house prices to adjust and new types of neighborhood to form endogenously - descriptive or partial equilibrium approaches have no adequate way of accounting for this kind of possibility. Our results indicate that the elimination of racial differences in income (or education) would lead to a moderate *increase* in the segregation of the high-income members of each major

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<sup>7</sup> The impact of the bundling of housing and neighborhood attributes in models of location choice is analyzed in Bayer (1999). The importance of issue bundling in a political economy context has been studied in Besley and Coate (2001).

racial group in the Bay Area and to an increase in the overall segregation of Asian and Hispanic households. Partial equilibrium predictions of the model work in the opposite direction.<sup>8</sup>

Our second hypothesis relates to the consequences of segregation. In contrast with the previous literature, which has emphasized the effects of living in a segregated neighborhood on various individual outcomes, we draw attention to the way that race alters residential location decisions in the first place. Accordingly, we advance the hypothesis that racial sorting in the housing market serves to lower the consumption of a wide variety of neighborhood amenities by minority households, pointing specifically to the implicit price mechanism described above. In particular, when the size of a minority population is relatively small and its members relatively poor on average, racial sorting in the housing market tends to raise the implicit price that households in this group face for neighborhood amenities, thereby leading to a reduction in their consumption.

We address this hypothesis by comparing the current equilibrium and a new equilibrium in which racial factors have been eliminated from the household choice process: a comparison of consumption patterns for households of different races and income levels in the current versus new equilibrium will then reveal whether consumption of neighborhood attributes is significantly affected. Our general equilibrium simulations provide the first evidence in the literature that sorting on the basis of race itself (whether driven by preferences directly or discrimination) leads to large reductions in the consumption of public safety and school quality by all black and Hispanic households and large reductions in the housing consumption of high-income black and Hispanic households.<sup>9</sup> These effects are likely to have a significant impact on the inter-generational persistence of racial differences in education, income, and wealth.

The rest of the paper is organized as follows: Section 2 outlines the key feature of our San Francisco Bay Area dataset. Using these data, Section 3 provides evidence on the distribution of neighborhoods available in the housing market as well as the actual neighborhood

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<sup>8</sup> One concern with this counterfactual simulation is that it assumes the general structure of racial preferences would be unaffected by the elimination of racial differences in income or education. In practice, major changes in the distribution of income or education across race might affect racial preferences – for example, with more high-income blacks in a metropolitan area for example, segregating forces could be weakened. To address this concern, we provide additional evidence based on an analysis of segregation patterns across the 330 US metropolitan areas, the results indicating that the elimination of racial differences tends to increase segregation when there are many minority households. See Section 8 below.

<sup>9</sup> We remain agnostic throughout this paper as to whether these interactions arise as the result of the preferences of each race for living with neighbors of the same race or discrimination in the housing market. While this distinction has important welfare implications, the point made here concerning the impact of racial interactions on the consumption of housing and neighborhood attributes remains regardless of which explanation prevails. We discuss this issue in greater detail below.

choices that households in different race and income categories make. This descriptive evidence motivates our two hypotheses. Sections 4, 5 and 6 describe the main analytical tool used in this paper - an equilibrium model of residential sorting, describing the model, its estimation, and the estimated preference parameters in turn. Section 7 uses the estimated model to conduct a series of general equilibrium simulations that provide direct evidence on our central hypotheses. Section 8 provides additional evidence using 2000 Census data from across metropolitan areas, and Section 9 concludes.

## 2 DATA

The main analysis conducted in this paper is facilitated by access to restricted Census microdata for 1990. These restricted Census data provide the detailed individual, household, and housing variables found in the public-use version of the Census, but also include information on the location of individual residences and workplaces at a very disaggregate level. In particular, while the public-use data specify the PUMA (a Census region with approximately 100,000 individuals) in which a household lives, the restricted data specify the Census block (a Census region with approximately 100 individuals), thereby identifying the local neighborhood that each individual inhabits and the characteristics of each neighborhood far more accurately than has been previously possible with such a large-scale data set.

For our primary analysis, we use data from six contiguous counties in the San Francisco Bay Area: Alameda, Contra Costa, Marin, San Mateo, San Francisco, and Santa Clara. We focus on this area for two main reasons: because it is reasonably self-contained, and because the area is sizeable along a number of dimensions, including over 1,100 Census tracts, and almost 39,500 Census blocks, the smallest unit of aggregation in the data. The sample consists of just over 242,000 households.

The Census provides a wealth of data on the individuals in the sample – race, age, educational attainment, income from various sources, household size and structure, occupation, and employment location.<sup>10</sup> In addition, it provides a variety of housing characteristics: whether the unit is owned or rented, the corresponding rent or owner-reported value,<sup>11</sup> number of rooms,

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<sup>10</sup> Throughout our analysis, we treat the household as the decision-making agent and characterize each household's race as the race of the 'householder' – typically the household's primary earner. We assign households to one of four mutually exclusive categories of race/ethnicity: Hispanic, non-Hispanic Asian, non-Hispanic Black, and non-Hispanic White.

<sup>11</sup> As described in the Data Appendix, we construct a single price vector for all houses, whether rented or owned. Because the implied relationship between house values and current rents depends on expectations about the growth rate of future rents in the market, we estimate a series of hedonic price regressions for each of over 40 sub-regions of the Bay Area housing market. These regressions return an estimate of the

number of bedrooms, type of structure, and the age of the building. We use these housing characteristics directly and in constructing neighborhood characteristics, characterizing stock of housing in the neighborhood surrounding each house, as well as neighborhood racial, education and income distributions based on the households within the same Census block group, a Census region containing approximately 500 housing units. We merge additional data describing local conditions with each house record, constructing variables related to crime rates, land use, local schools, topography, and urban density. For each of these measures, a detailed description of the process by which the original data were assigned to each house is provided in a Data Appendix. The list of the principal housing and neighborhood variables used in the analysis, along with means and standard deviations, is given in the first two columns of Table 1.

### 3 NEIGHBORHOOD SEGREGATION AND CONSUMPTION PATTERNS

These detailed data for the San Francisco Bay Area help bring to light two striking aspects of neighborhood choice in the housing market equilibrium: there is a shortage of neighborhoods with both a high fraction of minorities and even moderate levels of neighborhood amenities; and minority households face a higher implicit price for such amenities than white households do.

**Segregation Patterns.** Before turning to these, we first describe the general pattern of segregation in the Bay Area by examining average racial exposure rates. These exposure rates characterize the average racial composition of the neighborhoods in which households in a particular sociodemographic category (e.g., high-income Asian households) reside;<sup>12</sup> throughout the portion of our analysis based on the Bay Area, we use Census block groups to define neighborhoods.

The top panel of Table 2 reports average racial exposure rates by race. The measures shown in the first column imply, for instance, that Asians in the Bay Area live in Census block groups that are on average 23 percent Asian, 7 percent black, 12 percent Hispanic, and 57 percent white. Comparing the racial exposure rates to the population of the Bay Area as a whole, a clear pattern emerges, with households of each race residing with households from the same race in proportions significantly higher than their proportions for the full Bay Area. The middle panel

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ratio of house values to rents for each of these sub-regions and we use the average of these ratios for the Bay Area, 264.1, to convert monthly rent to house value for the purposes of reporting results at the mean.

<sup>12</sup> A variety of segregation measures are available, and while no single measure is perfect, we choose to work with the exposure rate measures because they are easy to interpret and can be decomposed in a variety of meaningful ways.

shows the pattern of exposure for the top and bottom income quartile of households of each race, along with the fraction of households in each race-income category. For example, the average exposure of blacks to other blacks declines from 49 percent for those in the lowest quartile of the income distribution to only 24 percent – still more than triple the fraction of blacks in the Bay Area as a whole.

The bottom panel of Table 2 makes clear that high-income minority households, and high-income blacks in particular, have a significant propensity to live with poorer households of the same race. It reports the average exposure of households in the top quartile of the overall income distribution for each race to households of the same race in each income quartile. The second row, for example, shows that blacks in the top quartile of the income distribution live on average in neighborhoods that consist of 9.8 percent blacks in the bottom quartile of the income distribution and 3.5 percent blacks in the top quartile. Thus blacks in the top income quartile are ‘over-exposed’ to blacks in the poorest quartile, living on average in neighborhoods with almost three times the fraction of these households in the Bay Area as a whole.<sup>13</sup>

**Neighborhood Choices.** To motivate our two central hypotheses more directly, Tables 3 and 4 describe the distribution of neighborhoods in which households of each race in the top and bottom quartile of the income distribution reside, respectively. In each case, neighborhoods are ranked by the fraction of households of the same race, and deciles of the distribution are then reported. Focusing first on the second panel of Table 3, which shows the distribution of neighborhoods in which high-income black households reside, the first column provides average household, housing, and neighborhood characteristics for the 10 percent of high-income black households that live in neighborhoods with the lowest fraction of black households, neighborhoods in which less than 2 percent of the population is black. As one reads across the columns, the neighborhoods have a larger fraction of black households by construction; the final column indicates that fully 10 percent of blacks in the top income quartile reside in neighborhoods in which over 76 percent of the population is black.

What emerges from Table 3 is the striking range of neighborhoods in which high-income blacks reside. Comparing the neighborhoods at either end of the spectrum, the levels of school quality, public safety, average neighborhood income, and fraction college-educated are each more than 2 standard deviations greater in the high-income neighborhoods versus the high-minority,

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<sup>13</sup> While not as extreme as for blacks, the average exposure of high-income Asians to other Asians also remains well above the fraction of Asians in the Bay Area as a whole. As Panel C makes clear, however, in the case of high-income Asians, much of this overall exposure to other Asians results from a particularly strong exposure to other high-income Asians rather than to low-income Asians.



low-income neighborhoods. The pattern for high-income Hispanics is remarkably similar to that for black households, as those neighborhoods with the highest fraction of Hispanics also possess substantially lower average incomes, less educated neighbors, worse schools and higher crime rates. For Asians, the pattern is qualitatively similar although much less marked, while for high-income white households, increases in the consumption of local public goods and other neighborhood socioeconomic measures are generally accompanied by an increase in the fraction of white neighbors.

The patterns shown in Table 3 are suggestive of two important aspects of neighborhood choice in the current Bay Area housing market equilibrium. First, the consumption of school quality, public safety, neighborhood income and education is strongly negatively correlated with the fraction of neighbors of the same race for black and Hispanic households. This suggests that these households are partially constrained in the current Bay Area equilibrium, being confronted by a shortage of minority neighborhoods with even moderate levels of desirable neighborhood attributes.<sup>14</sup> It is likely that an improvement in the availability of predominantly black and Hispanic neighborhoods with even moderate levels of average income would be very attractive to these households. This relates directly to our first hypothesis, as we would expect such neighborhoods to form more easily with an increase in the fractions of black and Hispanic households in the upper quartiles of the income distribution.

Second, while the increased consumption of neighborhood amenities comes at the expense of increased housing prices for high-income households of each race, these increases are accompanied by sharp *decreases* in the fraction of households of the same race for black and Hispanic households but *increases* in the fraction of households of the same race for whites. Given segregating racial preferences (as we find below), this implies that black and Hispanic households face a price of consuming these neighborhood amenities that is implicitly higher than the price faced by white households. Thus if race were removed as a consideration in the location decision, along the lines of our second hypothesis, the implicit price that minority households would face in choosing neighborhoods with more neighborhood amenities would fall, leading them to choose neighborhoods more in line with those chosen by high-income black households living in predominantly white neighborhoods.<sup>15</sup>

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<sup>14</sup> In the Bay Area in 2000, while predominantly Asian and white neighborhoods span the spectrum of average income levels, only six of the 659 tracts with income levels above that of the median tract, less than one percent, were more than 20 percent black.

<sup>15</sup> The direct observation that, for instance, fully 30 percent of black households in the top income quartile, with income around \$92,000, live in neighborhoods in which the average household income is less than \$40,000 indicates that this is likely to be the case.

In a similar fashion, Table 4 reveals that black and Hispanic households in the bottom income quartile also face an implicit price of neighborhood amenities that exceeds the direct costs. While not as marked as for households in the top income quartile, the increased consumption of these neighborhood amenities is again accompanied by sharp decreases in the fraction of households of the same race for black and Hispanic households. Thus we anticipate that racial sorting in the housing market also raises the implicit price of neighborhood amenities for low-income black and Hispanic households, although perhaps not as starkly as for high-income households.

An alternative potential explanation for the differences across the neighborhoods shown in Tables 3 and 4 is that, within each of these race-income quartile groups, households have heterogeneous demands for neighborhood characteristics and socioeconomics. This is certainly part of the story.<sup>16</sup> However, a proper test requires one to control directly household sorting on the basis of other factors such as income, wealth, education, household structure, and employment locations. To this end, we now describe a model of residential sorting that explicitly incorporates these factors.

#### **4 A MODEL OF RESIDENTIAL SORTING**

This section sets out the principal analytical tool that we use to explore segregation as a general equilibrium phenomenon - an equilibrium model of a self-contained urban housing market in which households sort themselves among the set of available housing types and locations. The model consists of two key elements: the household residential location decision problem and a market-clearing condition. While it has a simple structure, the model allows households to have heterogeneous preferences defined over housing and neighborhood attributes in a very flexible way; it also allows for housing prices and neighborhood sociodemographic compositions to be determined in equilibrium.

We estimate this model using rich individual data, appealing to the notion of revealed preference - specifically that the residential location decision reveals preferences for a wide range of housing and neighborhood attributes. By examining how location decisions vary, on average, with household characteristics such as income, education, and race, one can learn how preferences for the housing and neighborhood attributes vary with these sociodemographic characteristics. Once the broad set of preference parameters in the model have been estimated,

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<sup>16</sup> For instance, the average income of the high-income black households that reside in the neighborhoods with the fewest black households is in fact larger (\$112,000 on average) than for those that reside in the neighborhoods with the highest fraction of blacks (\$91,000).

we then use the estimates and the equilibrium model to conduct a series of general equilibrium simulations designed to shed new light on the causes and consequences of segregation.

**The Residential Location Decision.** We model the residential location decision of each household as a discrete choice of a single residence from a set of houses available in the market. The utility function specification is based on the random utility model developed in McFadden (1973, 1978) and the specification of Berry, Levinsohn, and Pakes (1995), which includes choice-specific unobservable characteristics.<sup>17</sup> Let  $X_h$  represent the observable characteristics of housing choice  $h$  including characteristics of the house itself (e.g., size, age, and type), its tenure status (rented vs. owned), and the characteristics of its neighborhood (e.g., school, crime, and topography). We use the notation  $\bar{Z}$  to represent the average sociodemographic characteristics of the corresponding neighborhood, writing it separately from the other housing and neighborhood attributes to make explicit the fact that these characteristics are determined in equilibrium.<sup>18</sup> Let  $p_h$  denote the price of housing choice  $h$  and, finally, let  $d_h^i$  denote the distance from residence  $h$  to the primary work location of household  $i$ . Each household chooses its residence  $h$  to maximize its indirect utility function  $V_h^i$ :

$$(1) \quad \underset{(h)}{\text{Max}} \quad V_h^i = \mathbf{a}_X^i X_h + \mathbf{a}_{\bar{Z}}^i \bar{Z}_h - \mathbf{a}_p^i p_h + \mathbf{x}_h + \mathbf{e}_h^i.$$

The error structure of the indirect utility is divided into a correlated component associated with each house that is valued the same by all households,  $\mathbf{x}_h$ , and an individual-specific term,  $\mathbf{e}_h^i$ . A useful interpretation of  $\mathbf{x}_h$  is that it captures the unobserved quality of each house, including any unobserved quality associated with its neighborhood.<sup>19</sup>

Each household's valuation of choice characteristics is allowed to vary with its own characteristics,  $Z^i$ , including education, income, race, employment status, and household composition. Specifically, each parameter associated with housing and neighborhood characteristics and price,  $\mathbf{a}_j^i$ , for  $j \in \{X, \bar{Z}, d, p\}$ , varies with a household's own characteristics according to:

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<sup>17</sup> Discrete choice applications in the urban economics literature include Anas (1982), Quigley (1985), Gabriel and Rosenthal (1989), Nechyba and Strauss (1998), Bajari and Kahn (2001). Only the latter paper includes choice-specific unobservables. Brock and Durlauf (2001) discrete choice models with social interactions.

<sup>18</sup> This component of the utility function allows for endogenous sorting on the basis of race, as in Schelling (1969, 1971), as well as other characteristics such as income and education.

<sup>19</sup> We employ an indirect utility function that is linear in housing prices. Alternative specifications of the indirect utility function could certainly be estimated, as the linear form is not essential to the model.

$$(2) \quad \mathbf{a}_j^i = \mathbf{a}_{0j} + \sum_{r=1}^R \mathbf{a}_{rj} Z_r^i,$$

with equation (2) describing household  $i$ 's preference for choice characteristic  $j$ .

**Characterizing the Housing Market.** As with all models in this literature, the existence of a sorting equilibrium is much easier to establish if the individual residential location decision problem is smoothed in some way. To this end, we assume that the housing market can be fully characterized by a set of housing types that is a subset of the full set of available houses, letting the supply of housing of type  $h$  be given by  $S_h$ .<sup>20</sup>

Given the household's problem described in equations (1)-(2), household  $i$  chooses housing type  $h$  if the utility that it receives from this choice exceeds the utility that it receives from all other possible house choices - that is, when

$$(3) \quad V_h^i > V_k^i \quad \Rightarrow \quad W_h^i + \mathbf{e}_h^i > W_k^i + \mathbf{e}_k^i \quad \Rightarrow \quad \mathbf{e}_h^i - \mathbf{e}_k^i > W_k^i - W_h^i \quad \forall k \neq h$$

where  $W_h^i$  includes all of the non-idiosyncratic components of the utility function  $V_h^i$ . As the inequalities in (3) imply, the probability that a household chooses any particular choice depends in general on the characteristics of the full set of possible house types. Thus the probability  $P_h^i$  that household  $i$  chooses housing type  $h$  can be written as a function of the full vectors of house/neighborhood characteristics (both observed and unobserved) and prices  $\{\mathbf{X}, \mathbf{p}, \mathbf{x}\}$ :

$$(4) \quad P_h^i = f_h(Z^i, \mathbf{X}, \mathbf{p}, \mathbf{x})$$

as well as the household's own characteristics  $Z^i$ .

Aggregating the probabilities in equation (4) over all observed households yields the predicted demand for each housing type  $h$ ,  $D_h$ :

$$(5) \quad D_h = \sum_i P_h^i.$$

In order for the housing market to clear, the demand for houses of type  $h$  must equal the supply of such houses and so:

$$(6) \quad D_h = S_h, \quad \forall h \quad \Rightarrow \quad \sum_i P_h^i = S_h \quad \forall h.$$

Given the decentralized nature of the housing market, prices are assumed to adjust in order to clear the market. The implications of the market clearing condition defined in equation (6) for

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<sup>20</sup> We also assume that each household observed in the sample represents a continuum of households with the same observable characteristics, with the distribution of idiosyncratic tastes  $\mathbf{e}_h^i$  mapping into a set of choice probabilities that characterize the distribution of housing choices that would result for the continuum of households with a given set of observed characteristics. For expositional ease and without loss of generality, we assume that the measure of this continuum is one.

prices are very standard, with excess demand for a housing type causing price to be bid up and excess supply leading to a fall in price. Given the indirect utility function defined in (1) and a fixed set of housing and neighborhood attributes, Bayer, McMillan, and Rueben (2004b) show that a unique set of prices (up to scale) clears the market.

When some neighborhood attributes are endogenously determined by the sorting process itself, we define a sorting equilibrium as a set of residential location decisions and a vector of housing prices such that the housing market clears and each household makes its optimal location decision given the location decisions of all other households. In equilibrium, the vector of neighborhood sociodemographic characteristics along with the corresponding vector of market clearing prices must give rise to choice probabilities that aggregate back up to the same vector of neighborhood sociodemographics.<sup>21</sup>

Whether this model gives rise to multiple equilibria depends on the distributions of preferences and available housing choices as well as the utility parameters.<sup>22</sup> In general, it is impossible to establish that the equilibrium is unique *a priori*. Fortunately, estimation of the model does not require the computation of an equilibrium nor uniqueness more generally, as we describe in the next section. Thus, the primary place where the issue of whether the equilibrium is unique arises is in conducting counterfactual simulations and we discuss this issue in Section 7 below.

## 5 ESTIMATION

Estimation of the model follows a two-step procedure related to that developed in Berry, Levinsohn, and Pakes (1995). A rigorous presentation of the estimation procedure, including a discussion of methods for simplifying the computation and a description of the asymptotic properties of the estimator, is included in a technical appendix. In this section, we outline the estimation procedure, focusing on identification of the model.

It is helpful in describing the estimation procedure to first introduce some notation. In particular, we rewrite the indirect utility function as:

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<sup>21</sup> Bayer, McMillan, and Rueben (2004b) establish the existence of a sorting equilibrium as long as (i) the indirect utility function shown in equation (1) is decreasing in housing prices for all households; (ii) indirect utility is a continuous function of neighborhood sociodemographic characteristics; and (iii)  $\mathbf{e}$  is drawn from a continuous density function.

<sup>22</sup> On the one hand, as described above, when neighborhood sociodemographic characteristics do not enter the utility function, the equilibrium is unique. On the other hand, if households have strong preferences to live with others of the same race and do not value any other housing or neighborhood attributes, multiple equilibria arise, each characterized by complete racial segregation, but with the attachment of a given race to a given neighborhood completely indeterminate. The real world, of course, lies somewhere in between these extreme cases.

$$(7) \quad V_h^i = \mathbf{d}_h + \mathbf{I}_h^i + \mathbf{e}_h^i$$

where

$$(8) \quad \mathbf{d}_h = \mathbf{a}_{0X} X_h + \mathbf{a}_{0\bar{Z}} \bar{Z}_h - \mathbf{a}_{0p} p_h + \mathbf{x}_h$$

and

$$(9) \quad \mathbf{I}_h^i = \left( \sum_{k=1}^K \mathbf{a}_{kX} Z_k^i \right) X_h + \left( \sum_{k=1}^K \mathbf{a}_{k\bar{Z}} Z_k^i \right) \bar{Z}_h - \left( \sum_{k=1}^K \mathbf{a}_{kp} Z_k^i \right) p_h.$$

In equation (8),  $\mathbf{d}_h$  captures the portion of utility provided by housing type  $h$  that is common to all households, and in (9),  $k$  indexes household characteristics. When the household characteristics included in the model are constructed to have mean zero,  $\mathbf{d}_h$  is the *mean indirect utility* provided by housing choice  $h$ . The unobservable component of  $\mathbf{d}_h$ ,  $\mathbf{x}_h$ , captures the portion of unobserved preferences for housing choice  $h$  that is correlated across households, while  $\mathbf{e}_h^i$  represents unobserved preferences over and above this shared component.

The first step of the estimation procedure is equivalent to a Maximum Likelihood estimator applied to the individual location decisions taking prices and neighborhood sociodemographic compositions as given,<sup>23</sup> returning estimates of the heterogeneous parameters in  $\mathbf{I}$  and mean indirect utilities,  $\mathbf{d}_h$ . This estimator is based simply on maximizing the probability that the model correctly matches each household observed in the sample with its chosen house type. In particular, for any combination of the heterogeneous parameters in  $\mathbf{I}$  and mean indirect utilities,  $\mathbf{d}_h$ , the model predicts the probability that each household  $i$  chooses house type  $h$ . We assume that  $\mathbf{e}_h^i$  is drawn from the extreme value distribution, in which case this probability can be written:

$$(10) \quad P_h^i = \frac{\exp(\mathbf{d}_h + \hat{\mathbf{I}}_h^i)}{\sum_k \exp(\mathbf{d}_k + \hat{\mathbf{I}}_k^i)}$$

Maximizing the probability that each household makes its correct housing choice gives rise to the following log-likelihood function:

$$(11) \quad \ell = \sum_i \sum_h I_h^i \ln(P_h^i)$$

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<sup>23</sup> Formally, the validity of this first stage procedure requires the assumption that the observed location decisions are individually optimal, given the collective choices made by other households and the vector of market-clearing prices *and* that households are sufficiently small such that they do not interact strategically with respect to particular draws on  $\mathbf{e}$ . This ensures that no household's particular idiosyncratic preferences affect the equilibrium and the vector of idiosyncratic preferences  $\mathbf{e}$  is uncorrelated with the prices and neighborhood sociodemographic characteristics that arise in any equilibrium. For more discussion, see the Technical Appendix.

where  $I_h^i$  is an indicator variable that equals 1 if household  $i$  chooses house type  $h$  in the data and 0 otherwise. The first step of the estimation procedure consists of searching over the parameters in  $\mathbf{I}$  and the vector of mean indirect utilities to maximize  $\ell$ .

**The Endogeneity of Neighborhood Sociodemographic Composition.** Having estimated the vector of mean indirect utilities in the first stage of the estimation, the second stage of the estimation involves decomposing  $\mathbf{d}$  into observable and unobservable components according to the regression equation (8).<sup>24</sup> In estimating equation (8), important endogeneity problems need to be confronted. To the extent that house prices partly capture house and neighborhood quality unobserved to the econometrician, so the price variable will be endogenous. Estimation via least squares will thus lead to price coefficients biased towards zero, producing misleading willingness-to-pay estimates for a whole range of choice characteristics. This issue arises in the context of any differentiated products demand estimation and we describe the construction of an instrument for price in the Technical Appendix.

A second identification issue concerns the correlation of neighborhood sociodemographic characteristics in  $\bar{Z}$  (which includes neighborhood race, income and education, as well as school quality) with unobserved housing and neighborhood quality,  $\mathbf{x}_i$  - a correlation that is mechanical given the sorting of households across locations. To properly estimate preferences in the face of this endogeneity problem, we adapt a technique previously developed by Black (1999) when estimating preferences for school quality. Black's strategy makes use of a sample of houses near school attendance zone boundaries, estimating a hedonic price regression that includes boundary fixed effects. Intuitively, the idea is to compare houses in the same local neighborhood but on opposite sides of the boundary, exploiting the discontinuity in the right to attend a given school. For our purposes, boundary fixed effects are likely absorb out differences in many fixed housing and neighborhood attributes, including ones that are unobservable.<sup>25</sup> To the extent that sorting with respect to the school district boundaries that we use is driven by differences in school quality and neighborhood sociodemographics themselves, the use of boundary fixed effects isolates

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<sup>24</sup> Notice that the set of observed residential choices provides no information that distinguishes the components of  $\mathbf{d}$ . That is, however  $\mathbf{d}$  is broken into components, the effect on the probabilities shown in equation (10) is identical.

<sup>25</sup> A number of empirical issues arise in incorporating boundary fixed effects into our analysis. Concerning the choice of jurisdiction for which the boundaries are defined, we use boundaries between school districts in the Bay Area. A central feature of local governance in California helps to eliminate some of the problems that naturally arise with the use of school district boundaries, as Proposition 13 ensures that the vast majority of school districts within California are subject to a uniform effective property tax rate of one percent. Concerning the width of the boundaries, we experimented with a variety of distances and report the results for 0.25 miles, as these were more precise due to the larger sample size.

variation in neighborhood sociodemographics that is uncorrelated with variation in unobserved housing and neighborhood quality. Thus, it provides an appealing way to account for the correlation of school quality with unobservable neighborhood quality as well as the correlation of neighborhood sociodemographics with unobservable neighborhood quality.

Table 1 displays descriptive statistics for various samples related to the boundaries. The first two columns report means and standard deviations for the full sample while the third column reports means for the sample of houses within 0.25 miles of a school district boundary.<sup>26</sup> Comparing the first column to the third column of the table, it is immediately obvious that the houses near school district boundaries are not fully representative of those in the Bay Area as a whole. To address this problem, we create sample weights for the houses near the boundary.<sup>27</sup> Column 7 of Table 1 shows the resulting weighted means, showing that using these weights makes the sample near the boundary much more representative of the full sample, column 7 typically being much closer to column 1 than column 3 is.

Comparing differences across school district boundaries, displayed in columns 4 and 5, the average characteristics of houses with 0.25 miles of the boundary on the high school quality versus low school quality side of each boundary reveals that houses on the high side cost \$53 more per month and are assigned to schools with a 43-point average test score increase.<sup>28</sup> Houses on the high quality side of the boundary are more likely to be inhabited by white households and households with more education and income – this pattern is evident when looking at the difference in means test. These types of across-boundary differences in sociodemographic composition are what one would expect if households sort on the basis of preferences for school quality, thereby leading those with stronger tastes or increased ability to pay for school quality to choose the higher school quality side of the boundary.

**Racial Preferences and Discrimination.** The strategy of using boundary fixed effects is designed to deal with the correlation of neighborhood sociodemographic characteristics with any unobserved component of neighborhood quality valued the same by households of all races. It is

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<sup>26</sup> In addition, the fourth and fifth columns report means on the high versus low average test score side of the school district boundary; the sixth column reports t-tests for difference in means of fourth and fifth columns; and the seventh column reports weighted means for the sample of houses within 0.25 miles of a school district boundary - the weight is described below.

<sup>27</sup> The following procedure is used: we first regress a dummy variable indicating whether a house is in a boundary region on the vector of housing and neighborhood attributes using a logistic regression. Fitted values from this regression provide an estimate of the likelihood that a house is in the boundary region given its attributes. We use the inverse of this fitted value as a sample weight in subsequent regression analysis conducted on the sample of houses near the boundary.



important to point out, however, that this strategy does not help us distinguish the extent to which these estimated racial interactions result from (i) discrimination in the housing market (e.g., centralized discrimination against recent immigrants from China), (ii) direct preferences for the race of one's neighbors (e.g., preferences on the part of a recent immigrant from China to live with other Chinese immigrants), and (iii) preferences for race-specific portions of unobserved neighborhood quality (e.g., preferences for Chinese groceries which are located in neighborhoods with a high fraction of Chinese residents). That is, these underlying explanations are indistinguishable from one another because they give rise to predicted residential location decisions that are observationally equivalent in the data.

Regardless of whether the sizes of the parameters that multiply the interactions of household race and neighborhood racial composition result from preferences or discrimination, these parameters do inform us about the importance of sorting on the basis of race in the housing market. If one thinks of discrimination as an expression of the preferences of the discriminating group concerning the group discriminated against, then our model essentially misassigns these preferences to the group discriminated against. Thus, while our estimate of the preferences of black households to live with other black households may be overstated, the difference between the preferences of white versus black households to live with black households remains informative. Because it is the *differences* in estimated preferences that drive the equilibrium predictions of the model, our inability to distinguish centralized discrimination from decentralized preferences does not seriously affect a key aim of our simulations, namely to gauge the impact of racial factors as a whole on the housing market equilibrium.

## 6 PARAMETER ESTIMATES

Estimation of the full model proceeds in two stages, as noted, the first stage recovering interaction parameters and vector of mean indirect utilities, the second stage returning the components of mean indirect utility. We report the estimates of the interaction parameters in Appendix Table 1. As the table demonstrates, the first stage of the estimation procedure returns 165 parameters on terms that interact individual and household characteristics, permitting great flexibility in preferences across different types of households. In particular, the model includes the following household characteristics: total household income, household income from capital sources (a proxy for wealth), race, education, work status, age, the presence of children, and, importantly, interactions of household income and race. These household characteristics are

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<sup>28</sup> As described in the Data Appendix, we construct a single price vector for all houses, whether rented or owned.

interacted with many housing and neighborhood attributes including house price, owner-occupancy status,<sup>29</sup> number of rooms, the age of the structure, average test score, elevation, population density, crime and eight variables characterizing the neighborhood sociodemographic composition: the fraction of households of each race, the fraction of households college educated, average neighborhood income, and neighborhood income interacted with race. The model also captures the spatial aspect of the housing market by allowing households to have preferences over commuting distance.<sup>30</sup>

This specification is especially flexible from the point of view of the main research questions addressed in the paper, in two key ways. First, it includes a full set of race interactions permitting, for example, black households to have different preferences for Asian versus white neighbors. Second, it includes interactions of race and income both as household and neighborhood characteristics, thereby permitting high-income Asian households, for example, to have different preferences than low-income Asian households for neighborhoods and for these preferences to depend on whether a neighborhood has high- versus low-income Asian neighbors.

The numbers in Appendix Table 1 are not directly interpretable in dollar values and so we discuss the results in terms of marginal willingness-to-pay measures (MWTP); the results for the mean household are shown in Table 5 and results related to heterogeneity in MWTP are shown in Table 6. The first three columns of Table 5 reports the implied measures of the mean MWTP for housing and neighborhood attributes that result for three specifications of the mean indirect utility regressions. These measures are calculated by dividing the coefficient associated with each choice characteristic in these regressions by the coefficient on price.

Results are reported for the full sample and for a sample of houses within 0.25 miles of school district boundaries, with and without including fixed effects. No clear changes emerge when the sample is reduced to only those houses near a school district boundary. Comparing the coefficients on the neighborhood sociodemographic characteristics with and without the inclusion of boundary fixed effects (columns 2 and 3) yields the pattern of results one would expect if the boundary fixed effects control for unobserved components neighborhood quality unrelated to the

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<sup>29</sup> We treat ownership status as a fixed feature of a housing unit in the analysis. Thus, whether a household rents or owns is endogenously determined within the model by its house choice. In the model, we allow households to have heterogeneous preferences for home-ownership (a positive interaction between household wealth and ownership, for example, will imply that wealthier households are more likely to own their housing unit, as we find below). A single price index is used for owner- and renter-occupied units - see the Data Appendix for details.

<sup>30</sup> We treat a household's primary work location as exogenous, calculating the distance from this location to the location of the neighborhood in question. Estimates based on a specification without commuting distance are qualitatively similar.

sorting of households across the boundary.<sup>31</sup> Thus boundary fixed effects seem to be effective in controlling for fixed aspects of unobserved neighborhood quality that are correlated with neighborhood sociodemographics, and thus provide an attractive way of estimating preferences for neighborhood sociodemographic characteristics in the presence of this important endogeneity problem.<sup>32</sup>

Table 6 reports the implied estimates of the heterogeneity in MWTP for selected housing and neighborhood characteristics for the specification associated with column (3) in Table 5, which includes boundary fixed effects. This is our preferred specification. The first row of Table 6 repeats the MWTP of the mean household and then reports the MWTP for households with the characteristic listed in the row heading, holding all other characteristics at the mean. The table reveals strong segregating racial interactions, with households of each race preferring to live near others of the same race. Interpreted literally as preferences, black households with income equal to the mean (\$55,000), for example, are willing to pay \$67 per month on average to live in a neighborhood with 10 percent more black versus white households. White households with mean income, on the other hand, are willing to pay \$38 per month on average to live in a neighborhood that is 10 percent more white versus black.<sup>33</sup> Hispanic and Asian households with mean incomes are willing to pay \$98 and \$72 per month, respectively, to live with others of the same race versus whites. Importantly, the equilibrium predictions of the model concerning segregation patterns are driven by the differences in preferences across households of different races (as discussed above, this is in essence what makes it impossible to distinguish preferences from discrimination in observational data). Looking at the difference between what whites versus households in the other race categories are willing to pay for these changes, Asian-White and Black-White differences come to over \$100 per month for a 10 percent change, while Hispanic-White differences amount to \$70 per month. Table 6 also shows similar figures calculated for households at a higher income level (income=\$120,000) in this case Asian-White, Black-White

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<sup>31</sup> In particular, controlling for fixed effects increases the coefficient on percent black (reported at the mean average neighborhood income) from -\$285 to -\$234; on percent Hispanic from -\$37 to \$104; and on percent Asian from -\$70 to \$150. Doing so also reduces the coefficient on the percent of households with a college degree from \$186 to \$165 and the coefficient on average neighborhood income (/ \$10,000) from \$89 to \$85 per month.

<sup>32</sup> Comparison of our parameter estimates with analogous hedonic price regressions provides further support for their plausibility. We carry out this comparison in a brief Hedonics Appendix.

<sup>33</sup> We discuss the implications of centralized discrimination in the housing market for the interpretation of these estimates in the Hedonics Appendix below.

and Hispanic-White differences each remain near \$90 per month. Thus, strong segregating forces in the housing market are relevant at all income levels.<sup>34</sup>

## 7 GENERAL EQUILIBRIUM SIMULATIONS

We now use the estimated parameters to conduct a series of general equilibrium simulations designed to shed new light on the causes and consequences of segregation. Each simulation begins by changing a key primitive of the model and then calculating a new equilibrium for the model in this counterfactual environment.

The basic structure of the simulations consists of a loop within a loop. The outer loop calculates the sociodemographic composition of each neighborhood, given a set of prices and an initial sociodemographic composition of each neighborhood. The inner loop calculates the unique set of prices that clears the housing market, given an initial sociodemographic composition for each neighborhood. Thus for any change in the primitives of the model, we first calculate a new set of prices that clears the market; as discussed in Section 4, Berry (1994) ensures that there is a unique set of market clearing prices. Using these new prices and the initial sociodemographic composition of each neighborhood, we then calculate the probability that each household chooses each housing type, and aggregating these choices to the neighborhood level, calculate the predicted sociodemographic composition of each neighborhood. We then replace the initial neighborhood sociodemographic measures with these new measures and start the loop again – i.e., calculate a new set of market clearing prices with these updated neighborhood sociodemographic measures. We continue this process until the neighborhood sociodemographic measures converge. The set of household location decisions corresponding to these new measures along with the vector of housing prices that clears the market then represents the new equilibrium.<sup>35</sup>

**Adjusting Crime Rates and Average Test Scores.** Because some neighborhood amenities, such as crime rates and school quality, depend in part on the sociodemographic composition of the

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<sup>34</sup> The strong segregating racial interactions that we estimate are in no way implicitly assumed in writing down the model. As is clear from Table 6, households of every income level prefer to live with higher income neighbors. This makes clear that the model does not in any way force the parameters to yield segregating preferences (i.e., preferences for others like oneself), as both high- and low-income households are willing to pay for higher income neighbors.

<sup>35</sup> While this procedure always converges to an equilibrium, the model does not guarantee that this equilibrium is generically unique. In all of the calculations presented in this paper, we report results that start from the initial equilibrium and follow the procedure summarized here. Experimenting with other starting values led to the same new equilibrium each time.

neighborhood, it is natural to expect these neighborhood characteristics to adjust as part of the movement to a new sorting equilibrium.<sup>36</sup> Accounting for the impact of neighborhood sociodemographic characteristics on crime rates and test scores is a challenging exercise, as selection problems abound. For example, an OLS regression of crime rates on neighborhood sociodemographic characteristics almost certainly overstates the role of these characteristics in producing crime as it ignores the fact that households sort non-randomly across neighborhoods.

In the light of these difficulties, we adopt an approach that seeks to provide simple bounds for the characteristics of the new equilibrium that results for each of our simulations. For one bound, we calculate a new equilibrium without allowing crime rates and average test scores in each neighborhood to adjust. For the other bound, we calculate a new equilibrium, adjusting crime rates and average test scores in each neighborhood according to the adjustments implied by an OLS regression of the crime rate and average test score on neighborhood sociodemographic composition. The first bound will tend to understate the impact of sociodemographic shifts on the implied crime rate and average test score in each neighborhood, while the second bound will tend to overstate the impact of these sociodemographic shifts. As the results below indicate, these bounds provide a reasonable range for the predictions from our simulations.<sup>37</sup>

**Eliminating Racial Interactions in the Location Decision.** We first consider the general equilibrium predictions of counterfactual simulations that eliminate all racial interactions in the location decision – that is, setting all of the utility parameters that govern preferences for neighborhood racial characteristics (including interactions of neighborhood race and neighborhood income) to zero. Table 7 reports the exposure rate measures that arise with the elimination of racial interactions. Not surprisingly, the elimination of racial interactions has an enormous effect in reducing segregation, completely eliminating segregation except for a small portion for black households.

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<sup>36</sup> Such adjustments may arise due to effects that operate through the political system, as in Tiebout (1956), or as the result of productive externalities. The former effects are likely to be limited in our analysis due to nature of the provision of public goods in California, which gives local governments almost no control over taxes or the level of spending.

<sup>37</sup> It is also important to point out that because the model itself does not perfectly predict the housing choices that individuals make, the neighborhood sociodemographic measures initially predicted by model,  $\bar{Z}_n^{PREDICT}$ , will not match the actual sociodemographic characteristics of each neighborhood,  $\bar{Z}_n^{ACTUAL}$ . Consequently, before calculating the new equilibrium for any simulation, we first solve for the initial prediction error associated with each neighborhood  $n$ :  $\mathbf{w}_n = \bar{Z}_n^{ACTUAL} - \bar{Z}_n^{PREDICT}$ . We add this initial prediction error  $\mathbf{w}_n$  to the sociodemographic measures calculated in each iteration before substituting these measures back into the utility function.

The elimination of racial interactions in the location decision also has important consequences for the consumption of households of each race. Table 8 reports a number of consumption measures before and after the simulation, the rows of the table reporting the home-ownership rate, average monthly house price, average commuting distance, and the average consumption of house size, school quality, crime, neighborhood income and education for each racial group.<sup>38</sup> The most striking results for this simulation pertain to the consumption of local public goods. In this case, the black-white gap in school quality consumption is reduced by 55%-65% and the Hispanic-white gap by 65-66%. Likewise, the black-white gap in exposure to crime is reduced by 55%-65% and the Hispanic-white gap is reduced by 84-85%. Again, the ranges for these estimates reflect the results of two simulations that differ in the manner school quality and crime are adjusted with the changing neighborhood sociodemographic composition. The striking feature of these results is that substantial reductions in racial differences in consumption come about simply by eliminating racial interactions in the housing market - that is, without changing household income, wealth, education, etc.

To provide more perspective on these results, Table 9 breaks out the results of Table 8 by income, reporting results for households in the top and bottom quartiles of the income distribution. Focusing on the results for black households, these numbers reveal that black households in the top income quartile experience increased consumption of every type of neighborhood and housing amenity, including house size and home ownership. Black households in the bottom income quartile also experience increased consumption of each neighborhood amenity, but actually experience a decline in housing consumption. Importantly, black households at all income levels also spend a considerable amount more on housing in the new equilibrium in which sorting for race-related reasons has been eliminated.

These results imply that race plays a profound role in shaping the equilibrium matching of households to neighborhoods in an urban housing market. As the consumption patterns of Tables 3 and 4 have already suggested, because black households make up only about 8 percent of the population of the Bay Area, consumption decisions regarding neighborhood race and other neighborhood amenities are not separable; increases in these other neighborhood amenities typically mean a decline in the fraction of racial minorities in a neighborhood. This affects the implicit price that blacks versus whites pay for neighborhood amenities, thereby accentuating racial differences in consumption. This point is underscored by the fact that black households

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<sup>38</sup> We also note that the elimination of racial interactions leads to an overall reduction in commuting distances for all households except Asians; without needing to adjust their location decisions for race-related reasons, households are able to more easily find suitable locations in other dimensions.

spend a good deal more on housing in the new equilibrium in which race-related reasons for sorting have been eliminated compared with the initial equilibrium.

Taken together, the results of Table 9 imply that racial sorting in the housing market serves to accentuate racial differences in the consumption of neighborhood goods throughout the income distribution. While racial differences in income, wealth, and education would give rise to differences in the consumption of neighborhood amenities even in the absence of racial sorting, as can be seen in the consumption figures for the new equilibrium, racial sorting tends to widen these underlying differences, leading to even lower levels of consumption though at cheaper housing prices for black households. While the corresponding changes in housing prices make the welfare implications of this lower consumption unclear, these results imply that racial sorting in the housing market works in general to strengthen the persistence of intergenerational racial differences in educational attainment, income, and wealth.

**Eliminating Racial Differences in Income and Wealth.** We next consider the impact of eliminating racial differences in both non-capital income and capital income, which we assume throughout this discussion to be a good proxy for household wealth.<sup>39</sup> Operationally, we do this by assigning to a household at the  $p^{th}$  percentile of the income distribution within its own race the income and wealth (capital income) of the  $p^{th}$  percentile household in the income distribution of the Bay Area as a whole. This method equalizes income and wealth across races and has the advantage of preserving income rank within race.

Table 10 summarizes the impact of this change on segregation patterns, reporting three sets of exposure rate measures. Panel A reports the measures based on data for the full sample, while Panels B-D report the partial and general equilibrium predictions.<sup>40</sup> The partial equilibrium predictions of the model imply a reduction in segregation of 13-22% for black, Hispanic, and white households (as measured by the over-exposure to households of the same race) and of 4% for Asian households. These predictions mirror those generally found in the previous literature, which indicate that differences in income explain only a modest amount of the observed pattern of racial segregation.<sup>41</sup> In essence, the partial equilibrium predictions reflect the fact that

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<sup>39</sup> Note that even though we do not control directly for property wealth in our analysis, the estimated coefficients associated with income from capital sources will do a good job of capturing a wealth effect as long as property and non-property wealth are sufficiently correlated.

<sup>40</sup> As described above, it is important to note that measurement error is built into the measures reported in Panels B and C to reflect the fact that the model does not perfectly predict actual neighborhood sociodemographic compositions. Thus, the results presented in these three panels are directly comparable to one another.

<sup>41</sup> See, for example, Bayer, McMillan, and Rueben (2004a) and, for a more complete summary of results, Massey and Denton (1993).

eliminating racial differences in income and wealth leads to more similar demands for housing and neighborhood attributes across race. The partial equilibrium predictions do not move even further in the direction of reducing segregation primarily because racial interactions in the housing market dampen the propensity of high-income black and Hispanic household to move into houses in what had been high-income neighborhoods with high fractions of white households.

The general equilibrium predictions of the model imply a significant *increase* in the segregation of Asian and Hispanic households, increasing the over-exposure of households of each race to households of the same race by 15-20 percent. Moreover, the general equilibrium predictions imply a reduction in segregation of only 5-9 percent for black households (as measured by the over-exposure to households of the same race). Thus, in direct contrast to the previous literature, our results imply that segregation may very well increase with the elimination of racial differences in important sociodemographic characteristics. Importantly, it is the fact that our model allows for the set of neighborhoods themselves to change that is critical. The partial equilibrium approaches previous used in the literature essentially constrain their analyses to imply that reducing racial differences in socioeconomic characteristics would reduce segregation.

To provide a fuller picture of the impact of eliminating racial differences in income and wealth, Table 11 reports a series of consumption measures for households in the top and bottom quartiles of the income distribution, analogous to those reported in Table 9 for our previous counterfactual simulation. In essence, this simulation puts each race on equal footing in terms of ability to pay for housing and neighborhood attributes, leaving any race-related reasons for sorting in place. As Table 10 makes clear, these strong segregating preferences continue to lead to substantial amounts of racial segregation, but the implications of racial sorting for consumption are very different when households of each race have equal versus unequal spending power. In particular, in the new equilibrium described in Table 11, while blacks in each income quartile continue to consume slightly lower levels of neighborhood amenities, (school quality, public safety, etc.), they also consume higher levels of housing amenities, home-ownership and house size than whites. More generally, while there is variation in the types of houses and neighborhoods chosen by each race, there is very little variation in the total amount spent on housing. In this way, racial sorting in a world with equal spending power likely continues to accentuate underlying differences in preferences across race, due to the small numbers of Asians, blacks, and Hispanics in the population. As the previous simulation demonstrates, however, in a world without equal spending power, racial sorting works to widen differences that arise initially



due to differences in the ability to pay, thereby potentially greatly slowing and perhaps even preventing racial convergence in education, income, and wealth over time.

## 8 LOOKING ACROSS METROPOLITAN AREAS

The general equilibrium approach that forms the basis for the main analysis presented in this paper has two potential limitations. First, the analysis has been conducted for a single metropolitan area, which brings into question whether the population and neighborhoods of this metropolitan area are sufficiently representative of those in other metropolitan areas. This is a particular concern to the extent that the process through which neighborhood compositions adjust with an equalization of important sociodemographic characteristics may be a function of the underlying sizes of minority population in the metro area. Second, the counterfactual simulations hold the general structure of racial preferences unchanged by the elimination of racial differences in income or education. While we are careful to allow preferences to vary distinctly by race and income categories, it is still possible that major changes in the distribution of income or education across race might affect preferences.

To address these potential shortcomings, we provide additional descriptive evidence based on an analysis of segregation patterns across the 330 US metropolitan areas for the year 2000. First, we demonstrate that the short supply of neighborhoods with even moderate education levels and a high fraction of minority households is a general feature of metropolitan areas throughout the United States. We then examine how segregation patterns vary with the sociodemographic composition of a metropolitan area. The resulting regressions provide evidence that, in many instances, overall segregation and especially the segregation of highly-educated households of a given race are increasing in the education level of that race.

The data used in this section were compiled from the Summary Files that provide information on the distribution of education by race for each Census tract for the year 2000.<sup>42</sup> As before, households are assigned to one of four mutually exclusive categories of race/ethnicity on the basis of the race/ethnicity of the householder.<sup>43</sup> We then construct exposure rate measures for

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<sup>42</sup> It would obviously have been preferable to use information on the joint distribution of race and income rather than education to make the results most comparable to those presented above. Unfortunately, the corresponding Census data, which we downloaded at the time of writing, had clear and serious errors. Also, Census tracts versus block groups are used in this portion of the analysis as that is the level at which the joint distribution of education and race is available in the Census Summary files.

<sup>43</sup> The vast majority of households that checked two races can be characterized as either Hispanic or non-Hispanic Asian or Pacific Islander. Other households that checked two or more races, a very small fraction overall, were dropped from this analysis.

a variety of race and education categories for each US primary metropolitan statistical area (PMSA).

The upper panel of Table 12 documents the number of tracts in the United States by the percentage of households with a college degree and the percentage of households that are black.<sup>44</sup> The first row describes the number of tracts in which more than 0, 20, 40, 60, and 80 percent of head of households are college-educated, respectively. The subsequent rows report the number of tracts in each of these categories with increasing fractions of black households. As the table shows, a much smaller fraction of the tracts with a high fraction of black households have a high fraction of households with a college degree. For example, while 23 percent of all tracts are at least 40 percent college educated, only 2.5 percent of tracts that are at least 40 percent black are at least 40 percent college educated, and only 1.1 percent of tracts that are at least 60 percent black are at least 40 percent college educated.<sup>45</sup>

The lower panel of Table 12 shows the locations of the tracts in the US that contain both a high fraction of black and a high fraction of college-educated households. It makes clear that the availability of neighborhoods containing a high fraction of both black and highly-educated households is extremely limited outside a handful of metro areas throughout the US. Of the 44 tracts (less than 0.1 percent of all tracts) that are at least 60 percent black and 40 percent college-educated, 13 are in the Washington, DC PMSA, 8 in Detroit, 6 in Los Angeles, and 5 in Atlanta. Thus, almost 75 percent of these tracts can be found in one of only four PMSAs. Of the 142 tracts that are at least 40 percent black and 40 percent college-educated, almost two-thirds are in the PMSAs listed above as well as Chicago and New York.

To explore the effect of a metropolitan area's population on segregation itself, Table 13 reports the results of a series of 27 regressions that relate measures of own-race exposure to the underlying sociodemographic characteristics of the metropolitan area for black, Asian, and Hispanic households, respectively. For each race, we report results for three exposure measures: the average exposure of (i) all, (ii) college-educated, and (iii) non-college-educated households of this race to others of the same race. Results are reported for samples based on all PMSAs and PMSAs where the fraction of the given race is above the median, and twice the median, respectively. In these regressions, a coefficient greater than one implies that the segregation of the group in question increases with an increase in the given population, while coefficients less than one imply a decrease. Consequently, we denote coefficients that are statistically different

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<sup>44</sup> In the interest of brevity, we limit the description of neighborhood in Table 12 to black households. Comparable tables are available upon request for the other races/ethnicities.

<sup>45</sup> In this sample, 47 percent of Asian, 16 percent of black, 14 percent of Hispanic, and 33 percent of white householders have a 4-year college degree.

from one rather than zero. We also report the results of a test of the hypothesis that an increase in the fraction of households of a given race that are college-educated has no effect on the own-race exposure of households in the associated education category.<sup>46</sup> This test reveals whether segregation is an increasing or decreasing function of the average education level of the race in question.

Focusing first on black households, the descriptive patterns presented in Table 13 imply that segregation of both college- and non-college-educated black households is increasing at a similar (and greater than one-to-one rate) in both the fraction of college- and non-college-educated black households in the PMSA. Thus, in general, an increase in the average education level of black households in a PMSA has no effect on the level of black segregation. In PMSAs in which at least 12.5 percent of the population is black, on the other hand, the regression coefficients imply that black segregation is increasing in the average education level of blacks in the PMSA. Taken together, the results suggest that an increase in black education levels is likely to have opposite effects on black segregation depending on whether the overall size of the population is large (increasing) versus small (decreasing). Interestingly, the fraction of households in the San Francisco Bay Area falls fairly close to the median fraction and, consequently, the analysis presented here would likely suggest that an increase in black education would have very little impact on black segregation, which is what our simulations reveal.

The results for Asian households imply that Asian segregation is an increasing function of the average education level of Asians in the metropolitan area, no matter how large the Asian population is (although one should note that very few metropolitan areas have a significant fraction of Asians). The results for Hispanic households imply that the segregation of college-educated Hispanics is an increasing function of the average education level of Hispanics in the metropolitan area.<sup>47</sup>

It is important to recognize that the analysis presented in Table 13 is descriptive. With around 300 observations, it is impossible to control properly for other factors that differ across metropolitan areas, especially if one considers that the effect of education on segregation may vary according to the size of the minority population in the metropolitan area. Moreover, these regressions do not control in any way for potential differences in the individuals of a given race

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<sup>46</sup> The appropriate test in this case is to compare the coefficient on the fraction of the PMSA that is of the corresponding race with a college degree to the coefficient on the fraction of the PMSA that is of the corresponding race without a college degree.

<sup>47</sup> The segregation of Hispanic households without a college degree, on the other hand, is a decreasing function of the average education level of Hispanics in the PMSA. Because Hispanic households without a college-degree represent over 85 percent of the population, overall Hispanic segregation is also generally a decreasing function of education.

that reside in metropolitan areas with a high versus low fraction of others of the same race.<sup>48</sup> That said, the resulting regressions suggest that, in many instances, overall segregation and especially the segregation of highly-educated households of a given race is an increasing function of the education level of that race. This possibility has been largely ignored by the previous literature, which has typically taken a more partial equilibrium view of the problem. Given the limitations of the across-metropolitan area analysis of the type used here, a fruitful direction for future research would be to apply the general equilibrium analysis developed in this paper to metropolitan areas throughout the country with different underlying populations.

## 9 CONCLUSION

This paper has studied the causes and consequences of residential segregation from a new general equilibrium perspective, one that recognizes that the types of neighborhoods available in a metropolitan housing market are endogenously determined, governed by the characteristics and preferences of households that reside in the metropolitan area. The paper has advanced two new hypotheses regarding the causes and consequences of segregation. According to the first, eliminating differences in income, wealth, or education across race would be unlikely to reduce segregation significantly, and could actually increase segregation as new minority neighborhoods form. According to the second, racial sorting in the housing market serves to lower the consumption of neighborhood amenities by minority households, especially those with moderate to high incomes.

Both hypotheses are motivated by the empirical regularity that in many US cities, neighborhoods combining a high fraction of minority households and even moderate levels of average income and education are in short supply. This has the effect of raising the implicit price that minority households pay for school quality, public safety, neighborhood education and income, given that in order to consume more of these other important neighborhood attributes, households are typically required to live in a neighborhood with fewer minorities. In turn, many high-income minority households live in neighborhoods with high fractions of other households

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<sup>48</sup> If one ranks PMSAs by the difference between the own-race exposure of Asian households and the fraction of Asians in the PMSA (i.e., the 'over-exposure' of Asians to one another), the following PMSAs are in the Top 10: Lafayette, IN (1); Bloomington, IN (3); Champaign, IL (6); State College, PA (7); Ann Arbor, MI (8); Lansing-East Lansing, MI (9); Lexington, KY (10), all university towns in the Midwest. This list highlight the concern with the types of regressions reported in Table 13, namely that the individuals of each race that live in metropolitan areas with, for example, a high fraction of college-educated members of that race may be systematically different than those who live in metro areas with a smaller fraction.

of the same race, giving up substantial amounts of consumption of local public goods and average neighborhood socioeconomic characteristics to do so.

The primary evidence that we present relating to these hypotheses is based on simulations of an equilibrium model of residential sorting, estimated using data on almost a quarter of million households in the San Francisco Bay Area. In estimating the model, we are careful to use reasonable variation in the data that addresses the correlation of neighborhood sociodemographic characteristics with unobserved housing and neighborhood quality. The equilibrium model in combination with the estimated preference structure then provides a powerful analytical tool for carrying out general equilibrium counterfactual exercises that shed light on our two central hypotheses.

The results of these general equilibrium counterfactuals provide clear support for both hypotheses. First, we find that the elimination of racial differences in income (or education) would lead to an increase in the segregation of the high-income members of each major racial group in the Bay Area and to an increase in the overall segregation of Asian and Hispanic households. The partial equilibrium predictions of the model, which do not account for the formation of new neighborhoods, lead to the opposite conclusion for Asians and Hispanics and, in the case of overall black segregation, overstate the decrease that would follow the elimination of racial differences in income. This underlines the value of our GE approach. The results are bolstered by descriptive evidence based on an analysis of segregation patterns across metropolitan areas; this analysis shows that the segregation of highly-educated, minority households, and in many instances minority households in general, is an increasing function of the fraction of minority households with a college degree in the metropolitan area.

Our general equilibrium analysis has also provided evidence that racial sorting in the housing market (whether driven by preferences directly or discrimination) leads to large reductions in the consumption of neighborhood amenities by all black and Hispanic households, and large reductions in the consumption of housing amenities by high-income black and Hispanic households. In doing so, racial sorting in the housing market accentuates differences in the consumption of neighborhood amenities that arise as the result of racial differences in income and wealth, thereby potentially slowing racial convergence in education, income, and wealth over time.

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**Table 1. Overall Sample and Sub-Sample Near School District Boundaries**

Sample Boundary/Weights Observations	full sample		within 0.25 miles of boundaries				t-test for difference in means ((4) versus (5))	weighted sample 27,958 (6) Mean
	242,100		actual sample 27,958	high test score side* 13,348	low test score side* 14,610			
	(1) Mean	(2) S.D.	(3) Mean	(4) Mean	(5) Mean			
<b><u>Housing/Neighborhood Characteristics</u></b>								
monthly house price	1,087	755	1,130	1,158	1,105	5.71	1,098	
average test score	527	74	536	558	515	50.96	529	
1 if unit owned	0.597	0.491	0.629	0.632	0.626	1.04	0.616	
number of rooms	5.114	1.992	5.170	5.207	5.134	3.13	5.180	
1 if built in 1980s	0.143	0.350	0.108	0.118	0.099	5.09	0.148	
1 if built in 1960s or 1970s	0.391	0.488	0.424	0.412	0.437	4.22	0.406	
elevation	210	179	193	194	192	1.14	212	
population density	0.434	0.497	0.352	0.349	0.355	2.08	0.374	
crime index	8.184	10.777	6.100	6.000	6.192	2.36	7.000	
% Census block group white	0.681	0.232	0.704	0.712	0.686	9.62	0.676	
% Census block group black	0.081	0.159	0.071	0.065	0.076	6.21	0.080	
% Census block group Hispanic	0.110	0.114	0.113	0.107	0.119	8.62	0.117	
% Census block group Asian	0.122	0.120	0.112	0.110	0.113	2.50	0.121	
% block group college degree or more	0.438	0.196	0.457	0.463	0.451	5.14	0.433	
average block group income	54,744	26,075	57,039	58,771	55,457	10.23	55,262	
<b><u>Household Characteristics</u></b>								
household income	54,103	50,719	56,663	58,041	55,405	4.20	55,498	
1 if children under 18 in household	0.333	0.471	0.324	0.322	0.325	0.54	0.336	
1 if black	0.076	0.264	0.066	0.062	0.070	2.69	0.076	
1 if Hispanic	0.109	0.312	0.111	0.102	0.119	4.54	0.115	
1 if Asian	0.124	0.329	0.112	0.114	0.110	1.06	0.121	
1 if white	0.686	0.464	0.706	0.717	0.696	3.86	0.682	
1 if college degree or more	0.438	0.497	0.460	0.467	0.454	2.64	0.441	
age (years)	47.607	16.619	47.890	48.104	47.699	1.99	47.660	
1 if working	0.698	0.459	0.705	0.702	0.709	1.28	0.701	
distance to work (miles)	8.843	8.597	8.450	8.412	8.492	0.82	8.490	

\* the closest Census block on the other side of the boundary is assigned to. Hence we determine whether it is on the 'high' versus 'low' side of the boundary.

**Table 2: Segregation Patterns for the San Francisco Bay Area**

**Panel A: Overall Exposure Rates**

	Asian	Black	Hispanic	White
Asian	<b>0.233</b>	0.072	0.115	0.573
Black	0.118	<b>0.384</b>	0.113	0.377
Hispanic	0.130	0.078	<b>0.218</b>	0.558
White	0.103	0.042	0.089	<b>0.760</b>
Composition of Bay Area	0.124	0.076	0.109	0.686

**Panel B: Exposure Rates of Households in Top Income Quartile**

	Asian	Black	Hispanic	White
Asian-q4	<b>0.211</b>	0.047	0.096	0.641
Black-q4	0.139	<b>0.240</b>	0.098	0.516
Hispanic-q4	0.136	0.051	<b>0.162</b>	0.644
White-q4	0.097	0.026	0.065	<b>0.807</b>

**Exposure Rates of Households in Bottom Income Quartile**

	Asian	Black	Hispanic	White
Asian-q1	<b>0.256</b>	0.101	0.122	0.499
Black-q1	0.116	<b>0.490</b>	0.115	0.302
Hispanic-q1	0.130	0.098	<b>0.246</b>	0.519
White-q1	0.106	0.058	0.099	<b>0.734</b>

**Panel C: Exposure Rates of Households in Top Income Quartile to Households of Same Race in Each Income Quartile**

	q1	q2	q3	q4	Total
Asian-q4	0.031	0.040	0.063	0.076	0.211
Black-q4	0.098	0.060	0.046	0.035	0.240
Hispanic-q4	0.045	0.048	0.043	0.026	0.162
White-q4	0.119	0.158	0.202	0.328	0.807

*Note:* Each entry in the table shows the average exposure of households of the race or race-income category shown in the row heading to households in the race or race-income category shown in the column heading. Panel C reports the average exposure of households of each race to others of the same race in each income quartile.

**Table 3: Neighborhood Consumption Patterns for Households in Top Income Quartile**

<b>Decile</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>	<b>7</b>	<b>8</b>	<b>9</b>	<b>10</b>
<b>Panel A: Asian households - Ranked by percent Asian in neighborhood</b>										
<i>% Asian in Neighborhood</i>	0-6	6-9	9-12	12-15	15-18	18-22	22-28	28-33	33-43	43-100
<i>Avg. Income - Top Quartile Asians</i>	109,100	108,600	104,000	108,300	107,000	101,200	104,500	101,800	98,900	96,100
<i>Neighborhood Characteristics</i>										
Average Test Score	566	559	556	555	556	544	535	543	527	522
Crime Rate	3.9	4.6	4.5	4.4	4.4	6.6	7.1	7.0	8.3	10.4
Avg. Income	72,200	70,200	65,500	73,300	71,000	62,300	64,700	63,600	56,500	59,000
% College Degree of More	54	54	50	54	53	50	46	49	45	47
Avg House Price	1,709	1,645	1,563	1,679	1,580	1,459	1,454	1,412	1,379	1,381
Avg. Number of Rooms	6.4	6.2	6.1	6.1	6.0	6.0	5.8	5.7	5.6	5.7
% Home Ownership	89	89	89	86	88	90	89	85	88	89
<b>Panel B: Black households - Ranked by percent Black in neighborhood</b>										
<i>% Black in Neighborhood</i>	0-2	2-4	4-6	6-8	8-12	12-20	20-33	33-54	54-76	76-100
<i>Avg. Income - Top Quartile Blacks</i>	112,300	103,200	96,700	99,600	96,800	93,800	97,200	95,500	91,400	91,100
<i>Neighborhood Characteristics</i>										
Average Test Score	565	552	529	527	507	508	465	453	429	407
Crime Rate	3.6	4.8	5.4	6.9	8.0	7.8	14.1	20.1	19.2	25.0
Avg. Income	73,500	68,800	57,900	57,000	56,400	54,000	51,500	43,100	42,100	31,200
% College Degree of More	56	52	47	46	43	43	45	37	31	18
Avg House Price	1,655	1,512	1,297	1,343	1,228	1,262	1,264	1,062	885	743
Avg. Number of Rooms	7.0	6.5	6.1	6.3	6.2	6.4	6.1	6.1	6.3	6.0
% Home Ownership	82.5	77.7	70.3	72.3	72.5	78.9	74.7	79.5	89.1	84.3
<b>Panel C: Hispanic households - Ranked by percent Hispanic in neighborhood</b>										
<i>% Hispanic in Neighborhood</i>	0-4	4-6	6-8	8-10	10-12	12-15	15-19	19-27	27-40	40-100
<i>Avg. Income - Top Quartile Hisp.</i>	118,000	109,000	105,000	96,600	92,700	95,700	91,600	92,500	90,600	94,200
<i>Neighborhood Characteristics</i>										
Average Test Score	593	568	550	539	518	512	505	499	476	452
Crime Rate	3.9	4.3	4.1	4.2	4.7	5.9	6.5	8.0	11.3	21.5
Avg. Income	85,100	73,100	65,000	59,900	55,700	53,600	51,800	49,100	43,900	41,300
% College Degree of More	64	58	52	47	42	39	35	31	24	16
Avg House Price	1,883	1,682	1,447	1,446	1,263	1,245	1,275	1,143	1,011	892
Avg. Number of Rooms	6.8	6.3	6.4	6.2	6.0	6.0	5.9	5.7	5.4	5.0
% Home Ownership	86	82	84	78	78	80	78	77	76	70
<b>Panel D: White households - Ranked by percent White in neighborhood</b>										
<i>% White in Neighborhood</i>	0-60	60-71	71-77	77-82	82-84	84-87	87-90	90-92	92-95	95-100
<i>Avg. Income - Top Quartile Whites</i>	99,400	107,100	107,000	111,100	118,300	115,800	119,700	130,000	128,700	143,400
<i>Neighborhood Characteristics</i>										
Average Test Score	505	530	540	555	574	580	583	604	593	611
Crime Rate	10.6	5.9	5.2	4.2	3.6	3.6	2.8	3.3	2.9	2.1
Avg. Income	52,400	60,100	62,400	67,100	79,300	73,300	75,500	86,800	87,200	102,800
% College Degree of More	41	48	51	52	58	56	61	63	64	67
Avg House Price	1,221	1,380	1,450	1,542	1,699	1,669	1,689	1,882	1,953	2,121
Avg. Number of Rooms	6.1	6.2	6.4	6.5	6.6	6.7	6.7	6.9	7.0	7.0
% Home Ownership	79	78	81	83	86	86	87	87	90	92

*Notes:* Each panel reports statistics for the neighborhoods in which households of the race shown and in the top income quartile reside. In each case, households are first ranked according to the fraction of households of the same race in their neighborhood and the deciles of that distribution are shown. In all cases, 'neighborhood' refers to the corresponding Census block group. The first income measure reported in each case corresponds to households of the given race in the top income quartile. The second income measure is the average income of the neighborhood.

**Table 4: Neighborhood Consumption Patterns for Households in Bottom Income Quartile**

Decile	1	2	3	4	5	6	7	8	9	10
<b>Panel A: Asian households - Ranked by Percent Asian in neighborhood</b>										
<i>% Asian in Neighborhood</i>	0-6.5	6.5-10	10-14	14-17	17-21	21-27	27-32	32-40	40-66	67-100
<i>Avg. Income - Bottom Quart. Asians</i>	12,600	12,300	11,900	12,200	12,200	12,400	12,000	12,600	12,300	10,400
<i>Neighborhood Characteristics</i>										
Average Test Score	505	502	498	501	495	497	506	504	493	467
Crime Rate	9.9	11.5	11.0	13.4	17.4	20.2	19.5	16.9	22.6	38.0
Avg. Income	44,600	44,600	41,700	43,000	39,300	37,300	36,300	39,000	40,200	23,000
% College Degree of More	38	39	39	42	40	35	38	39	35	16
Avg House Price	770	754	720	733	690	679	619	698	710	389
Avg. Number of Rooms	3.7	3.5	3.4	3.4	3.3	3.2	3.0	3.4	3.5	2.1
% Home Ownership	34	29	27	29	25	30	20	24	31	5
<b>Panel B: Black households - Ranked by Percent Black in neighborhood</b>										
<i>% Black in Neighborhood</i>	0-7	7-14	14-26	26-37	37-49	49-65	65-74	74-82	82-88	88-100
<i>Avg. Income - Bottom Quart. Blacks</i>	12,900	12,200	12,100	11,400	11,800	11,400	109,000	11,100	10,300	10,500
<i>Neighborhood Characteristics</i>										
Average Test Score	516	488	466	458	436	443	429	404	409	387
Crime Rate	10.8	15.0	18.5	20.6	23.9	21.6	25.5	23.8	30.9	27.4
Avg. Income	45,200	39,500	34,700	33,200	30,200	28,900	26,500	25,900	23,100	23,100
% College Degree of More	42	35	35	34	26	22	20	16	12	12
Avg House Price	722	667	601	524	504	498	474	471	446	432
Avg. Number of Rooms	3.7	3.7	3.7	3.8	3.6	4.0	4.2	4.1	4.2	4.3
% Home Ownership	19	22	19	21	20	31	34	33	29	35
<b>Panel C: Hispanic households - Ranked by Percent Hispanic in neighborhood</b>										
<i>% Hispanic in Neighborhood</i>	0-6	6-9	9-12	12-15	15-20	20-28	28-33	33-43	43-57	57-100
<i>Avg. Income - Bottom Quart. Hisp</i>	13,200	13,100	13,200	13,800	13,400	13,500	13,400	13,000	13,200	13,000
<i>Neighborhood Characteristics</i>										
Average Test Score	526	513	502	495	484	470	458	456	445	441
Crime Rate	12.3	11.3	10.0	8.5	10.3	10.9	13.3	15.4	23.1	23.3
Avg. Income	47,800	41,600	41,300	41,400	40,400	36,900	36,400	34,700	34,700	32,600
% College Degree of More	48	41	35	34	31	26	24	20	18	11
Avg House Price	736	700	669	678	670	620	614	597	600	629
Avg. Number of Rooms	3.7	3.7	3.8	3.7	3.8	3.6	3.5	3.6	3.4	3.5
% Home Ownership	30	25	28	31	34	24	26	23	20	23
<b>Panel D: White households - Ranked by Percent White in neighborhood</b>										
<i>% White in Neighborhood</i>	0-44.5	44.5-57	57-65	65-71	71-76	76-80	80-84	84-88	88-92	92-100
<i>Avg. Income - Bottom Quart. A55 Wl</i>	12,500	12,800	13,100	13,700	13,600	13,500	13,800	13,600	13,700	13,500
<i>Neighborhood Characteristics</i>										
Average Test Score	454	492	499	502	511	524	539	543	572	576
Crime Rate	20.5	15.1	12.4	10.4	8.5	5.0	5.0	4.0	4.3	2.6
Avg. Income	33,700	36,500	38,900	42,300	44,700	47,400	51,200	51,200	62,100	64,100
% College Degree of More	24	35	37	40	42	42	44	44	53	52
Avg House Price	609	648	664	724	757	820	883	838	987	1034
Avg. Number of Rooms	3.9	3.7	3.8	3.9	4.0	4.3	4.4	4.3	4.6	4.7
% Home Ownership	40	34	36	39	41	43	48	48	54	66

*Notes:* Each panel reports statistics for the neighborhoods in which households of the race shown and in the bottom income quartile reside. In each case, households are first ranked according to the fraction of households of the same race in their neighborhood and the deciles of that distribution are shown. In all cases, 'neighborhood' refers to the corresponding Census block group. The first income measure reported in each case corresponds to households of the given race in the bottom income quartile. The second income measure is the average income of the neighborhood.

**Table 5: Implied Mean MWTP Measures**

Sample	Residential Sorting Model			Hedonic Price Regressions		
	full sample	within .25 mile of boundaries		full sample	within .25 mile of boundaries	
	No	No	Yes	No	No	Yes
<b>Boundary Fixed Effects</b>						
<b>Observations</b>	242,100	27,958	27,958	242,100	27,958	27,958
	(1)	(2)	(3)	(1)	(2)	(3)
% Black*	-316.00 (9.80)	-285.46 (32.06)	-233.94 (38.87)	-101.92 (10.78)	-94.96 (35.28)	-40.46 (42.74)
% Hispanic*	-9.72 (13.59)	-37.19 (46.83)	104.11 (59.01)	142.64 (14.95)	106.60 (51.54)	254.31 (64.88)
% Asian*	-48.97 (11.40)	-69.84 (45.68)	149.77 (55.21)	67.84 (12.54)	-1.69 (50.27)	241.13 (60.71)
% College Degree or More	249.63 (9.19)	185.74 (25.96)	164.78 (39.42)	303.16 (10.11)	235.04 (28.57)	177.11 (43.34)
Average Income*	83.15 (0.74)	89.48 (2.18)	85.44 (2.64)	107.98 (0.82)	113.26 (2.40)	109.22 (2.90)
Average Test Score (in s.d.'s)	18.40 (1.53)	16.69 (4.23)	21.46 (5.29)	24.19 (1.68)	19.01 (4.66)	23.67 (5.81)
Owner-Occupied	154.93 (2.66)	141.08 (7.40)	148.15 (7.38)	133.56 (2.93)	117.59 (8.14)	125.63 (8.12)
Number of Rooms	111.71 (0.69)	111.67 (1.95)	109.28 (1.96)	122.29 (0.76)	123.91 (2.15)	121.72 (2.16)
Built in 1980s	99.60 (3.36)	71.36 (9.29)	87.40 (10.00)	101.88 (3.69)	80.58 (10.23)	108.57 (10.99)
Built in 1960s or 1970s	20.52 (2.41)	1.32 (6.86)	2.48 (7.47)	15.98 (2.65)	-4.40 (7.55)	4.87 (8.21)
Elevation (/100)	-1.70 (0.68)	-14.57 (2.18)	6.15 (3.99)	1.75 (0.75)	-14.08 (2.40)	6.51 (4.39)
Population Density	20.16 (3.23)	40.88 (13.87)	23.12 (17.31)	35.86 (3.56)	49.13 (15.27)	14.65 (19.04)
Crime Index	-0.39 (0.16)	-0.49 (0.65)	-1.02 (1.60)	0.38 (0.18)	0.94 (0.71)	0.36 (1.76)
F-statistic for boundary fixed effects			4.162			8.754

Notes: All neighborhood attributes are measured using the corresponding Census block group. Specifications shown in the table also include controls for interactions between neighborhood racial composition variables and average income as well as land use (% industrial, % residential, % commercial, % open space, % other) in 1, 2, 3, 4, and 5 mile rings around location and six variables that characterize the housing stock in each of these rings. \*Coefficients for % Asian, % Black, % Hispanic, Average Income reported at mean.

**Table 6. Heterogeneity in Marginal Willingness to Pay for Selected Neighborhood and Housing Attributes**

	Neighborhood Sociodemographics					House Characteristics		
	+10% Asian vs. White (at mean)	+10% Black vs. White (at mean)	+10% Hisp vs. White (at mean)	+10% College Educated	Blk Group Avg Income + \$10,000	Own vs. Rent	+1 Room	Built in 1980s vs. pre-1960
<b>Mean MWTP</b>	10.4 (5.9)	-23.4 (3.9)	15.0 (5.5)	16.5 (3.9)	85.4 (2.6)	148.2 (7.4)	109.3 (2.0)	87.4 (10.0)
<b>Race (at mean income=\$54,755)</b>								
Asian	97.9	-10.5	25.0	10.3	86.9	253.3	78.8	118.3
Black	38.5	66.6	44.1	35.9	65.8	80.3	117.4	96.9
Hispanic	8.7	-9.3	71.1	17.5	91.0	130.7	96.8	73.9
White	-8.1	-37.8	1.1	14.8	86.5	139.5	115.8	82.9
<b>Race (at income=\$120,000)</b>								
Asian	83.2	-31.7	-0.1	18.4	100.2	394.1	120.2	182.1
Black	37.5	28.6	19.0	41.3	79.2	221.4	159.0	160.8
Hispanic	7.7	-30.6	64.4	22.9	107.1	276.4	141.9	140.5
White	-9.1	-58.9	-23.9	20.1	98.0	277.2	155.0	144.9
<b>Education</b>								
less than college degree	15.6	-26.0	17.4	-9.1	87.5	134.5	107.0	69.8
college degree	3.8	-20.1	11.9	49.4	82.7	165.6	112.2	110.0

*Notes:* All figures are estimates of marginal willingness to pay for the change shown in the column heading. Figures are reported in terms of a monthly rent - see Data Appendix for a discussion of corresponding price is created for owner-occupied housing units in the sample. The first row of the table reports the

in the row heading and mean attributes for all other characteristics. All estimates are based on specification that includes boundary fixed effects and all neighborhood variables are measured using the corresponding Census block group.

**Table 7: Counterfactual - Eliminating Racial Interactions in Location Decision: Exposure Rates**

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*Panel A: Pre-Experiment*

	Asian	Black	Hispanic	White
Asian	<b>0.233</b>	0.072	0.115	0.573
Black	0.118	<b>0.384</b>	0.113	0.377
Hispanic	0.130	0.078	<b>0.218</b>	0.558
White	0.103	0.042	0.089	<b>0.760</b>

*Panel B: General Equilibrium - Unadjusted*

	Asian	Black	Hispanic	White
Asian	<b>0.111</b>	0.067	0.114	0.700
Black	0.110	<b>0.147</b>	0.088	0.646
Hispanic	0.129	0.061	<b>0.105</b>	0.690
White	0.126	0.071	0.110	<b>0.687</b>

*Panel C: General Equilibrium - Adjusted*

	Asian	Black	Hispanic	White
Asian	<b>0.111</b>	0.068	0.114	0.700
Black	0.110	<b>0.146</b>	0.089	0.645
Hispanic	0.129	0.062	<b>0.104</b>	0.690
White	0.126	0.071	0.110	<b>0.687</b>

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*Note:* Each entry in the table shows the average exposure of households of the race shown in the row heading to households of the race shown in the column heading. Figures are reported for a counterfactual simulation that sets all preference parameters associated with neighborhood racial composition to zero.

**Table 8: Counterfactual - Eliminating Racial Interactions in Location Decision: Consumption Measures**

	<b>Asian</b>	<b>Black</b>	<b>Hispanic</b>	<b>White</b>
	Ownership Rates			
<i>Pre-Experiment</i>	0.64	0.40	0.46	0.63
<i>General Equilibrium - Unadjusted</i>	0.67	0.35	0.46	0.63
<i>General Equilibrium - Adjusted</i>	0.67	0.35	0.46	0.63
	House Size			
<i>Pre-Experiment</i>	4.68	4.50	4.49	5.36
<i>General Equilibrium - Unadjusted</i>	4.76	4.53	4.67	5.31
<i>General Equilibrium - Adjusted</i>	4.76	4.53	4.67	5.31
	Average Math Scores			
<i>Pre-Experiment</i>	521	458	491	541
<i>General Equilibrium - Unadjusted</i>	528	502	514	531
<i>General Equilibrium - Adjusted</i>	529	496	515	531
	Average Crime Rates			
<i>Pre-Experiment</i>	10.33	18.73	11.50	6.14
<i>General Equilibrium - Unadjusted</i>	8.04	12.11	8.65	7.75
<i>General Equilibrium - Adjusted</i>	7.89	13.01	8.58	7.71
	Average House Rental Value			
<i>Pre-Experiment</i>	1092	740	882	1160
<i>General Equilibrium - Unadjusted</i>	1134	868	962	1126
<i>General Equilibrium - Adjusted</i>	1138	846	964	1127
	Average Commutes			
<i>Pre-Experiment</i>	10.17	9.89	11.07	10.28
<i>General Equilibrium - Unadjusted</i>	10.23	9.15	10.22	9.86
<i>General Equilibrium - Adjusted</i>	10.28	9.05	10.24	9.88
	Average Neighborhood Income			
<i>Pre-Experiment</i>	52,551	37,377	44,622	57,624
<i>General Equilibrium - Unadjusted</i>	54,364	44,711	49,814	55,665
<i>General Equilibrium - Adjusted</i>	54,381	44,356	49,848	55,696
	Percent College Educated			
<i>Pre-Experiment</i>	0.43	0.31	0.31	0.47
<i>General Equilibrium - Unadjusted</i>	0.44	0.38	0.38	0.45
<i>General Equilibrium - Adjusted</i>	0.44	0.37	0.38	0.45

*Note:* This table reports the consumption of housing and local public goods by households of each race. Numbers are reported for a counterfactual simulation that sets all preference parameters associated with neighborhood racial composition to zero.



**Table 9: Counterfactual - Eliminating Racial Interactions in Location Decision: Consumption Measures by Race and Income**

	Bottom Income Quartile				Top Income Quartile			
	Asian	Black	Hispanic	White	Asian	Black	Hispanic	White
	Ownership Rates				Ownership Rates			
<i>Pre-Experiment</i>	0.42	0.31	0.31	0.46	0.89	0.72	0.78	0.87
<i>General Equilibrium - Unadjusted</i>	0.45	0.22	0.28	0.45	0.91	0.76	0.83	0.87
<i>General Equilibrium - Adjusted</i>	0.45	0.22	0.28	0.45	0.91	0.76	0.83	0.87
	House Size				House Size			
<i>Pre-Experiment</i>	3.62	4.08	3.85	4.36	5.95	5.96	5.84	6.56
<i>General Equilibrium - Unadjusted</i>	3.67	3.94	3.87	4.31	6.07	6.27	6.24	6.50
<i>General Equilibrium - Adjusted</i>	3.67	3.94	3.87	4.30	6.07	6.26	6.25	6.51
	Average Test Score				Average Test Score			
<i>Pre-Experiment</i>	499	445	479	521	547	502	519	565
<i>General Equilibrium - Unadjusted</i>	505	490	498	508	556	535	548	559
<i>General Equilibrium - Adjusted</i>	505	482	498	506	557	533	549	559
	Average Crime Rate				Average Crime Rate			
<i>Pre-Experiment</i>	15.09	21.29	13.45	8.42	5.96	11.53	8.16	4.18
<i>General Equilibrium - Unadjusted</i>	11.13	14.06	10.92	10.78	4.93	6.98	5.24	5.03
<i>General Equilibrium - Adjusted</i>	11.11	15.30	11.03	10.95	4.78	7.29	5.09	4.93
	Average Monthly Rental Value				Average Monthly Rental Value			
<i>Pre-Experiment</i>	753	612	695	838	1,580	1,261	1,408	1,607
<i>General Equilibrium - Unadjusted</i>	742	689	698	788	1,678	1,490	1,632	1,585
<i>General Equilibrium - Adjusted</i>	743	661	696	786	1,683	1,477	1,636	1,586
	Average Commute				Average Commute			
<i>Pre-Experiment</i>	9.59	9.76	11.49	9.88	11.06	10.00	11.37	11.16
<i>General Equilibrium - Unadjusted</i>	9.72	8.94	10.42	9.46	11.09	10.09	11.13	10.71
<i>General Equilibrium - Adjusted</i>	9.76	8.82	10.42	9.47	11.15	10.02	11.18	10.73
	Average Neighborhood Income				Average Neighborhood Income			
<i>Pre-Experiment</i>	41,823	33,093	39,587	46,710	66,603	53,053	57,669	71,805
<i>General Equilibrium - Unadjusted</i>	43,754	39,858	42,645	44,893	68,061	60,295	66,433	69,319
<i>General Equilibrium - Adjusted</i>	43,662	39,258	42,494	44,732	68,084	60,365	66,567	69,387
	Percent College Educated				Percent College Educated			
<i>Pre-Experiment</i>	0.35	0.28	0.28	0.40	0.51	0.43	0.40	0.56
<i>General Equilibrium - Unadjusted</i>	0.36	0.34	0.33	0.37	0.53	0.50	0.50	0.55
<i>General Equilibrium - Adjusted</i>	0.36	0.32	0.33	0.36	0.53	0.50	0.50	0.55

*Note:* This table reports the consumption of housing and neighborhood amenities by households of each race in the bottom and top quartile of the overall income distribution, respectively. Numbers are reported for a counterfactual simulation that sets all preference parameters associated with neighborhood racial composition to zero.

**Table 10: Counterfactual - Equalizing Income and Wealth Across Race: Exposure Rates***Panel A: Pre-Experiment*

	Asian	Black	Hispanic	White
Asian	<b>0.233</b>	0.072	0.115	0.573
Black	0.118	<b>0.384</b>	0.113	0.377
Hispanic	0.130	0.078	<b>0.218</b>	0.558
White	0.103	0.042	0.089	<b>0.760</b>

*Panel B: Partial Equilibrium*

	Asian	Black	Hispanic	White
Asian	<b>0.228</b>	0.076	0.116	0.573
Black	0.123	<b>0.342</b>	0.100	0.426
Hispanic	0.131	0.069	<b>0.194</b>	0.590
White	0.103	0.047	0.094	<b>0.749</b>

*Panel C: General Equilibrium - Unadjusted*

	Asian	Black	Hispanic	White
Asian	<b>0.251</b>	0.070	0.089	0.584
Black	0.115	<b>0.355</b>	0.100	0.422
Hispanic	0.100	0.069	<b>0.229</b>	0.586
White	0.105	0.047	0.094	<b>0.749</b>

*Panel D: General Equilibrium - Adjusted*

	Asian	Black	Hispanic	White
Asian	<b>0.255</b>	0.070	0.088	0.580
Black	0.115	<b>0.367</b>	0.103	0.407
Hispanic	0.099	0.071	<b>0.237</b>	0.577
White	0.104	0.045	0.092	<b>0.752</b>

*Note:* Each entry in the table shows the average exposure of households of the race shown in the row heading to households of the race shown in the column heading. Numbers are reported for a counterfactual simulation that eliminates racial differences in income and wealth by replacing the income and wealth of the household in the p-th percentile of the income distribution within its own race with the income and wealth of the household in the p-th percentile of the overall income distribution.

**Table 11: Counterfactual - Equalizing Income and Wealth Across Race: Consumption Measures**

	Bottom Income Quartile				Top Income Quartile			
	Asian	Black	Hispanic	White	Asian	Black	Hispanic	White
	Ownership Rates				Ownership Rates			
<i>Pre-Experiment</i>	0.42	0.31	0.31	0.46	0.89	0.72	0.78	0.87
<i>General Equilibrium - Unadjusted</i>	0.59	0.50	0.45	0.43	0.90	0.89	0.88	0.83
<i>General Equilibrium - Adjusted</i>	0.63	0.49	0.45	0.42	0.90	0.89	0.88	0.84
	House Size				House Size			
<i>Pre-Experiment</i>	3.62	4.08	3.85	4.36	5.95	5.96	5.84	6.56
<i>General Equilibrium - Unadjusted</i>	3.88	4.44	4.01	4.32	5.99	6.79	6.53	6.32
<i>General Equilibrium - Adjusted</i>	3.84	4.34	3.94	4.31	6.02	6.79	6.52	6.36
	Average Math Scores				Average Math Scores			
<i>Pre-Experiment</i>	499	445	479	521	547	502	519	565
<i>General Equilibrium - Unadjusted</i>	506	453	484	519	549	533	542	557
<i>General Equilibrium - Adjusted</i>	504	449	480	518	550	533	541	559
	Average Crime Rates				Average Crime Rates			
<i>Pre-Experiment</i>	15.09	21.29	13.45	8.42	5.96	11.53	8.16	4.18
<i>General Equilibrium - Unadjusted</i>	11.74	18.91	12.39	9.19	5.55	7.89	5.88	5.03
<i>General Equilibrium - Adjusted</i>	12.38	19.99	13.05	9.16	5.43	7.93	5.99	4.71
	Average Monthly Rental Value				Average Monthly Rental Value			
<i>Pre-Experiment</i>	753	612	695	838	1,580	1,261	1,408	1,607
<i>General Equilibrium - Unadjusted</i>	770	798	784	788	1,561	1,580	1,550	1,555
<i>General Equilibrium - Adjusted</i>	771	783	776	789	1,567	1,563	1,556	1,556
	Average Commutes				Average Commutes			
<i>Pre-Experiment</i>	9.59	9.76	11.49	9.88	11.06	10.00	11.37	11.16
<i>General Equilibrium - Unadjusted</i>	10.01	9.83	11.21	9.80	11.34	11.03	12.03	10.64
<i>General Equilibrium - Adjusted</i>	9.92	9.70	11.22	9.80	11.37	11.02	11.99	10.67
	Average Neighborhood Income				Average Neighborhood Income			
<i>Pre-Experiment</i>	41,823	33,093	39,587	46,710	66,603	53,053	57,669	71,805
<i>General Equilibrium - Unadjusted</i>	46,916	38,212	43,040	47,613	66,621	55,194	60,229	66,229
<i>General Equilibrium - Adjusted</i>	46,689	38,177	42,405	47,241	67,162	55,765	60,561	66,615
	Percent College Educated				Percent College Educated			
<i>Pre-Experiment</i>	0.35	0.28	0.28	0.40	0.51	0.43	0.40	0.56
<i>General Equilibrium - Unadjusted</i>	0.37	0.27	0.29	0.41	0.49	0.43	0.40	0.53
<i>General Equilibrium - Adjusted</i>	0.42	0.34	0.33	0.47	0.49	0.43	0.41	0.54

Note: This table reports the consumption of housing and neighborhood amenities by households of each race in the bottom and top quartile of the overall income distribution, respectively. Numbers are reported for a counterfactual simulation that eliminates racial differences in income and wealth by replacing the income and wealth of the household in the p-th percentile of the income distribution within its own race with the income and wealth of the household in the p-th percentile of the overall income distribution.

**Table 12: Number of Tracts in United States in 2000 by Race and Education**

<b>Percent Black</b>	<b>Percent College Degree or More</b>				
	<i>0%</i>	<i>20%</i>	<i>40%</i>	<i>60%</i>	<i>80%</i>
<i>at least 0%</i>					
Number	49,021	26,351	11,094	3,005	203
Fraction of tracts at least 0% black	100.0%	53.8%	22.6%	6.1%	0.4%
<i>at least 20%</i>					
Number	9,149	2,567	641	59	0
Fraction of tracts at least 20% black	100.0%	28.1%	7.0%	0.6%	0.0%
<i>at least 40%</i>					
Number	5,657	1,164	142	14	0
Fraction of tracts at least 40% black	100.0%	20.6%	2.5%	0.2%	0.0%
<i>at least 60%</i>					
Number	3,921	623	44	5	0
Fraction of tracts at least 60% black	100.0%	15.9%	1.1%	0.1%	0.0%
<i>at least 80%</i>					
Number	2,559	271	21	1	0
Fraction of tracts at least 80% black	100.0%	10.6%	0.8%	0.0%	0.0%
<hr/>					
<b>PMSA Locations of Tracts</b>					<i>Average</i>
<i>Percentage black</i>	<i>&gt;80%</i>	<i>&gt;60%</i>	<i>&gt;40%</i>	<i>Percent</i>	<i>Black-Black</i>
<i>Percentage w/ college degree</i>	<i>&gt;40%</i>	<i>&gt;40%</i>	<i>&gt;40%</i>	<i>Black</i>	<i>Exposure*</i>
Washington, DC	5	13	29	25%	58%
Detroit, MI	5	8	17	21%	78%
Chicago, IL		3	16	17%	72%
New York, NY		4	12	23%	61%
Los Angeles, CA	4	6	10	10%	38%
Atlanta, GA	5	5	8	26%	60%
Cleveland, OH		1	6	16%	70%
Philadelphia, PA		1	5	18%	62%
Oakland, CA			5	12%	35%
Baltimore, MD			4	25%	64%
Raleigh-Durham, NC		1	3	12%	31%
Indianapolis, IN			3	12%	51%
Newark, NJ			3	20%	66%
Jackson, MS	1	1	2	25%	58%
Houston, TX	1	1	2	17%	48%
Columbia, SC			2	17%	43%
Ann Arbor, MI			2	7%	27%
New Orleans, LA			2	33%	67%
<b>Total</b>	<b>21</b>	<b>44</b>	<b>142</b>		

Notes: Tracts considered have a minimum of 800 households (the average tract in the US has almost 3,000 households) Exposure measures reported in fifth column of lower panel are the average fraction of black households in the Census tracts in which black households reside.

**Table 13: Segregation Across Metropolitan Areas**

Sample:	% Black > 0% in PMSA (n=330)			% Black > 6.2% in PMSA (n=165)			% Black > 12.5% in PMSA (n=77)		
	Own-Race Exposure of Black Hhlds with Education			Own-Race Exposure of Black Hhlds with Education			Own-Race Exposure of Black Hhlds with Education		
	Any	College Degree	Less than College	Any	College Degree	Less than College	Any	College Degree	Less than College
Fraction PMSA - Black w/ Col. Deg. ( $\beta^1$ )	1.43 (1.12)	1.93 (0.81)	1.90 (1.16)	2.21 (1.18)	2.40 (0.95)	2.69 (1.22)	3.75** (1.35)	3.23** (1.10)	4.20*** (1.39)
Fraction PMSA - Black w/out Col. Deg. ( $\beta^2$ )	1.98*** (0.18)	1.62*** (0.13)	1.95*** (0.18)	0.97 (0.21)	1.00 (0.17)	0.90 (0.21)	0.39** (0.29)	0.53* (0.24)	0.31** (0.30)
Test: $\beta^1 - \beta^2 = 0$							++	++	++
Sample:	% Asian > 0% in PMSA (n=330)			% Asian > 1.4% in PMSA (n=165)			% Black > 2.8% in PMSA (n=69)		
	Own-Race Exposure of Asian Hhlds with Education			Own-Race Exposure of Asian Hhlds with Education			Own-Race Exposure of Asian Hhlds with Education		
	Any	College Degree	Less than College	Any	College Degree	Less than College	Any	College Degree	Less than College
Fraction PMSA - Asian w/ Col. Deg. ( $\beta^1$ )	3.11*** (0.15)	3.55*** (0.16)	2.34*** (0.13)	2.95*** (0.21)	3.37*** (0.21)	2.24*** (0.19)	2.78*** (0.30)	3.11*** (0.31)	2.20*** (0.28)
Fraction PMSA - Asian w/out Col. Deg. ( $\beta^2$ )	0.80 (0.13)	0.24*** (0.13)	1.50*** (0.11)	0.74 (0.17)	0.19*** (0.18)	1.46*** (0.15)	0.56* (0.25)	0.06*** (0.23)	1.28 (0.23)
Test: $\beta^1 - \beta^2 = 0$	+++	+++	+++	+++	+++	++	+++	+++	++
Sample:	% Hispanic > 0% in PMSA (n=330)			% Hispanic > 3.2% in PMSA (n=165)			% Hispanic > 6.4% in PMSA (n=103)		
	Own-Race Exposure of Hispanic Hhlds w/ Education			Own-Race Exposure of Hispanic Hhlds w/ Education			Own-Race Exposure of Hispanic Hhlds w/ Education		
	Any	College Degree	Less than College	Any	College Degree	Less than College	Any	College Degree	Less than College
Fraction PMSA - Hispanic w/ Col. Deg. ( $\beta^1$ )	-0.65*** (0.51)	1.49** (0.24)	-0.55*** (0.55)	-0.46** (0.60)	1.54* (0.31)	-0.35* (0.64)	0.03 (0.61)	1.74** (0.36)	0.17 (0.65)
Fraction PMSA - Hispanic w/out Col. Deg. ( $\beta^2$ )	1.40*** (0.06)	0.92*** (0.03)	1.41*** (0.06)	1.22*** (0.07)	0.86*** (0.04)	1.22*** (0.08)	1.06 (0.08)	0.81*** (0.05)	1.05 (0.08)
Test: $\beta^1 - \beta^2 = 0$	---	++	---	--	++	--		++	

Note: This table reports the results of 27 regressions that relate various average exposure rates at the PMSA level to variables that characterize the sociodemographic characteristics of the PMSA's population. Results are reported separately for Black, Asian, and Hispanic households. For each race results are reported for the own-race exposure of all households and households with and without a college degree, respectively. Results are reported for (i) all PMSAs; (ii) PMSAs with the fraction of each race above the median fraction for all PMSAs in the US; (iii) PMSAs with the fraction of each race above twice the median fraction. Standard errors are in parentheses. \*\*\*, \*\*, \* denote that the coefficient is statistically different from 1.0 at 1%, 5%, and 10% confidence levels, respectively. +++, ++, + denotes that difference is positive and statistically significant at 1%, 5%, and 10% confidence levels, respectively. ---, --, - denotes that difference is negative and statistically significant at 1%, 5%, and 10% confidence levels, respectively.

**Appendix Table 1: Interaction Parameter Estimates**

Housing/Neighborhood Attribute	Household Characteristic												
	Hhld Income	Children Under 18	Black	Hispanic	Asian	Some College	College Degree or More	Working	Age	Hhld Capital Income	Black* Hhld Income	Hispanic* Hhld Income	Asian* Hhld Income
Monthly House Price	0.071 (0.003)	0.071 (0.023)	0.087 (0.051)	-0.244 (0.048)	0.208 (0.056)	0.285 (0.068)	0.400 (0.042)	0.197 (0.062)	0.007 (0.001)	0.013 (0.002)	0.030 (0.015)	0.082 (0.025)	0.034 (0.013)
Owner-Occupied	0.142 (0.005)	-0.050 (0.025)	-0.427 (0.058)	-0.046 (0.036)	0.851 (0.058)	0.027 (0.051)	0.191 (0.038)	0.303 (0.065)	0.046 (0.004)	0.094 (0.007)			
Number of Rooms	0.151 (0.005)	0.522 (0.027)	0.010 (0.034)	-0.521 (0.052)	-1.223 (0.071)	0.085 (0.047)	0.036 (0.031)	0.011 (0.043)	0.007 (0.001)	-0.060 (0.005)			
Built in 1980s	0.045 (0.004)	-0.064 (0.021)	0.065 (0.046)	-0.040 (0.030)	0.184 (0.045)	0.192 (0.062)	0.196 (0.037)	0.337 (0.068)	-0.011 (0.001)	0.019 (0.003)			
Built in 1960-79	0.013 (0.003)	0.023 (0.018)	0.315 (0.054)	-0.139 (0.045)	0.221 (0.057)	0.163 (0.065)	0.044 (0.029)	0.209 (0.060)	-0.005 (0.001)	0.002 (0.001)			
Average Test Score	0.001 (0.002)	0.056 (0.023)	-0.229 (0.056)	-0.077 (0.039)	0.086 (0.043)	0.186 (0.066)	0.206 (0.040)	0.141 (0.057)	0.011 (0.002)	0.056 (0.002)			
Elevation	0.019 (0.002)	0.038 (0.013)	-0.097 (0.038)	-0.134 (0.044)	0.006 (0.036)	0.141 (0.064)	0.090 (0.036)	-0.018 (0.042)	0.006 (0.001)	-0.039 (0.006)			
Population Density	0.017 (0.004)	-0.216 (0.024)	-0.561 (0.062)	-0.030 (0.031)	0.004 (0.032)	-0.006 (0.036)	0.159 (0.037)	-0.253 (0.063)	-0.006 (0.001)	0.042 (0.005)			
Crime Index	-0.016 (0.003)	0.010 (0.021)	0.491 (0.065)	0.045 (0.038)	0.017 (0.038)	-0.044 (0.044)	0.235 (0.041)	-0.164 (0.059)	0.014 (0.002)	0.066 (0.010)			
% Black	-0.073 (0.005)	0.114 (0.023)	1.700 (0.069)	0.697 (0.052)	0.680 (0.060)	-0.089 (0.054)	0.145 (0.037)	-0.114 (0.056)	-0.003 (0.001)	-0.110 (0.015)	-0.032 (0.019)		
% Hispanic	-0.063 (0.006)	0.125 (0.019)	0.700 (0.063)	0.891 (0.055)	0.425 (0.058)	-0.192 (0.062)	-0.094 (0.032)	-0.015 (0.043)	-0.010 (0.002)	-0.076 (0.012)		0.126 (0.030)	
% Asian	-0.003 (0.005)	0.088 (0.024)	0.799 (0.061)	0.311 (0.053)	1.708 (0.063)	-0.064 (0.059)	-0.215 (0.040)	-0.056 (0.047)	0.001 (0.001)	-0.079 (0.013)			-0.036 (0.021)
% College Degree or More	0.022 (0.006)	-0.200 (0.025)	0.574 (0.054)	0.080 (0.047)	-0.052 (0.043)	0.375 (0.070)	1.681 (0.058)	-0.338 (0.065)	-0.006 (0.002)	0.093 (0.014)			
Average Income	0.045 (0.006)	0.048 (0.018)	-0.808 (0.057)	0.245 (0.045)	-0.053 (0.041)	-0.028 (0.049)	-0.313 (0.053)	0.100 (0.056)	0.003 (0.001)	0.020 (0.006)			
% Black*Average Income	0.054 (0.009)		0.674 (0.078)								-0.026 (0.032)		
% Hispanic*Average Income	0.067 (0.010)			0.340 (0.067)								-0.081 (0.039)	
% Asian*Average Income	0.010 (0.009)				0.282 (0.071)								-0.003 (0.027)
Distance to Work	-0.022 (0.002)	0.156 (0.023)	-0.272 (0.043)	0.189 (0.035)	0.221 (0.039)	-0.093 (0.058)	0.160 (0.032)	-13.765 (0.056)	-0.010 (0.001)	-0.468 (0.019)			

Note: Parameter estimates reported with all variables normalized to have mean zero, standard deviation one. Standard errors are in parentheses.

## APPENDICES FOR “RESIDENTIAL SEGREGATION IN GENERAL EQUILIBRIUM” by Patrick Bayer, Robert McMillan, and Kim Rueben

This document contains three appendices for the paper “Residential Segregation in General Equilibrium.” The *Data Appendix* documents the sources for the data and the construction of variables used in the analysis. The *Estimation Appendix* provides a full description of the estimation procedure used in our analysis, discussing a number of important details that we abstract from in the main text in to streamline that presentation. The *Results Appendix* relates the main parameter estimates presented in the paper to analogous estimates from a series of hedonic price regressions.

### DATA APPENDIX

#### 1. Census Variables

**House Prices.** Because house values are self-reported, it is difficult to ascertain whether these prices represent the current market value of the property, especially if the owner purchased the house many years earlier. Fortunately, the Census contains other information that helps us to examine this issue and correct house values accordingly. In particular, the Census asks owners to report a continuous measure of their annual property tax payment. The rules associated with Proposition 13 imply that the vast majority of property tax payments in California should represent exactly 1 percent of the transaction price of the house at the time the current owner bought the property or the value of the house in 1978. Thus, by combining information about property tax payments and the year that the owner bought the house (also provided in the Census in relatively small ranges), we are able to construct a measure of the rate of appreciation implied by each household’s self-reported house value. We use this information to modify house values for those individuals who report values much closer to the original transaction price rather than current market value. In our study most households list the purchase price of their house rather than an estimated market value for their house. Thus if two identical houses were found in the census data but one was last sold in 1989 and one was last sold in 1969 we find on average the listed market price of the more recently sold house is on average 15 percent higher than the other house.

A second deficiency of the house values reported in the Census is that they are top-coded at \$500,000, a top-code that is often binding in California. Again, because the property tax payment variable is continuous and not top-coded, it provides information useful in distinguishing the values of the upper tail of the value distribution. We find that top-coding was fairly predominant in the Bay Area and that higher top-codes may be useful to gain a better understanding of house prices in expensive markets like California or New York.

The exact procedure that we use to adjust self-reported house values is as follows. We first regress the log of self-reported house value on the log of the estimated transaction price (100 times the property tax payment), and a series of dummy variables that characterize the tenure of the current owner:

$$(A1) \quad \log(V_j) = \mathbf{a}_1 \log(T_j) + \mathbf{a}_2 y_j + \mathbf{w}_j$$

where  $V_j$  represents the self-reported house value,  $T_j$  represents the estimated transaction price, and  $y_j$  represents a series of dummy variables for the year that the owner bought the house. If owner-estimated house values were indeed current market values and houses were identical except for owner tenure, this regression would return an estimate of 1 for  $\hat{\mathbf{a}}_1$  and the estimated  $\hat{\mathbf{a}}_2$  coefficients would indicate the appreciation of house values in the Bay Area over the full period of analysis. If owners tend to underreport house values, especially when they have lived in the house for a long time, the estimated  $\hat{\mathbf{a}}_2$  parameters will likewise underreport appreciation in the market. In this way, the estimated  $\hat{\mathbf{a}}_2$  parameters represent a conservative estimate of appreciation. Given the estimates of equation (2), we construct a predicted house value for each house in the sample and replace the owner-reported value with this measure when this predicted measure exceeds the owner-reported value. In practice, in order to allow for different rates of appreciation in different regions of the housing market, we conduct these regressions separately for each of the 45 Census PUMA (areas with

at least 100,000 people) in our sample and allow appreciation to vary with a small set of house characteristics within each PUMA. In this way, the first adjustment that we make to house prices is to adjust owner-reported values for likely under-reporting.

The adjustment to top-coded house prices uses the same approach, using the information on property taxes that are continuous and not top-coded. Using estimates of equation (2) based on a sample of houses that does not include the top-coded house values, we construct predicted house values for all top-coded houses. This allows us to assign continuous house values for top-coded measures.

**Reported Rental Value.** We next examined questions of reported monthly rents. While rents are presumably not subject to the same degree of misreporting as house values, it is still the case that renters who have occupied a unit for a long period of time generally receive some form of tenure discount. In some cases, this tenure discount may arise from explicit rent control, but implicit tenure discounts generally occur in rental markets even when the property is not subject to formal rent control. Thus while, this will not lead to errors in the answering of the listed census question it may lead to an inaccurate comparison of rents faced by households if they needed to move. In order to get a more accurate measure of the market rent for each rental unit, we utilize a series of locally based hedonic price regressions in order to estimate the discount associated with different durations of tenure in each of over 40 sub-regions within the Bay Area.

In order to get a better estimate of market rents for each renter-occupied unit in our sample, we regress the log of reported rent  $R_j$  on a series of dummy variables that characterize the tenure of the current renter,  $y_j$ , as well as a series of variables that characterize other features of the house and neighborhood  $X_j$ :

$$(A2) \quad \log(R_j) = \mathbf{b}_1 y_j + \mathbf{b}_2 X_j + \mathbf{u}_j$$

again running these regressions separately for each of the 45 PUMAs in our sample. To the extent that the additional house and neighborhood variables included in equation (3) control for differences between the stock of rental units with long-term vs. short-term tenants, the  $\hat{\mathbf{a}}_1$  parameters provide an estimate of the tenure discount in each PUMA.<sup>1</sup> In order to construct estimates of market rents for each rental unit in our sample, then, we inflate rents based on the length of time that the household has occupied the unit using the estimates of  $\hat{\mathbf{a}}_1$  from equation (2). In this way, these three price adjustments bring the measures for rents and house values reported in the Census reasonably close to market rates.

**Calculating Cost Per Unit of Housing Across Tenure Status.** Finally, in order to make owner- and renter-occupied housing prices comparable in our analysis we need to calculate a current rental value for housing. Because house prices reflect the expectations about the future rents for the property they incorporate beliefs about future housing appreciation. To appropriately deflate housing values – and especially to control for differences in expectations about appreciation in different segments of the Bay Area housing market – we regress the log of house price (whether monthly rent or house value)  $\Pi_j$  on an indicator for whether the housing unit is owner-occupied  $o_j$  and a series of additional controls for features of the house including the number of rooms, number of bedrooms, types of structure (single-family detached, unit in various sized buildings, etc.), and age of the housing structure as well as a series of neighborhood controls  $X_j$ :

$$(A3) \quad \log(\Pi_j) = \mathbf{g}_1 o_j + \mathbf{g}_2 X_j + \mathbf{h}_j$$

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<sup>1</sup> Interestingly, while we estimate tenure discounts in all PUMAs, the estimated tenure discounts are substantially greater for rental units in San Francisco and Berkeley, the two largest jurisdictions in the Bay Area that had formal rent control in 1990.



We estimate these hedonic price regressions for each of 40 sub-regions (Census Public Use Microdata Areas - PUMAs) of the Bay Area housing market. These regressions return an estimate of the ratio of house values to rents for each of these sub-regions and we use these ratios to convert house values to a measure of current monthly rent.

## **2. External Data**

We next discuss the additional variables we have added to the Census data to provide a more nuanced understanding of the neighborhood characteristics that affect house prices and residential location decisions. These data sets are linked to census blocks and can be used to determine the appropriateness of the questions and sampling techniques used. This additional data includes:

**School and School District Data.** The Teale data center in California provided a crosswalk that matches all Census blocks in California to the corresponding public school district. We have further matched Census blocks to particular schools using a variety of procedures that takes account of the location (at the block level) of each Census block within a school district and the precise location of schools within the district using information on location from the Department of Education. Other school information in these data include:

- 1992-93 CLAS dataset provides detailed information about school performance and peer group measures. The CLAS was a test administered in the early 1990s that will give us information on student performance in math, literature and writing for grades 4, 8 and 10. This dataset presents information on student characteristics and grades for students at each school overall and across different classifications of students, including by race and education of parents.
- 1991-2 CBEDS (California Board of Education data sets) datasets including information from the SIF (school information form) which includes information on the ethnic/racial and gender make-up of students, PAIF – which is a teacher based form that provides detailed information about teacher experience, education and certification backgrounds and information on the classes each teacher teaches, and (LEP census) a language census that provides information on the languages spoken by limited-English speaking students.

**Procedures for Assigning School Data.** While we have an exact assignment of Census blocks to school districts, we have only been able to attain precise maps that describe the way that city blocks are assigned to schools in 1990 for Alameda County. In the absence of information about within-district school attendance areas, we employ the alternative approaches for linking each house to a school. The crudest procedure assigns average school district characteristics to every house falling in the school district. A refinement on this makes use of distance-weighted averages. For a house in a given Census block, we calculate the distance between that Census block and each school in the school district. We have detailed information characterizing each school and construct weighted averages of each school characteristic, weighting by the reciprocal of the distance-squared as well as enrollment.

As a third approach we simply assign each house to the closest school within the appropriate school district. Our preferred approach (which we use for the results reported in the paper) refines this closest-school assignment by using information about individual children living in each Census block - their age and whether they are enrolled in public school. In particular, we modify the closest-school assignment technique by attempting to match the observed fourth grade enrollment for every school in every school district in the Bay Area. Adjusting for the sampling implicit in the long form of the Census, the 'true' assignment of houses to schools must give rise to the overall fourth grade enrollments observed in the data.

These aggregate numbers provide the basis for the following intuitive procedure: we begin by calculating the five closest schools to each Census block. As an initial assignment, each Census block and all the fourth graders in it are assigned to the closest school. We then calculate the total predicted enrollment in each school, and compare this with the actual enrollment. If a school has

excess demand, we reassign Census blocks out of its catchment area, while if a school has excess supply, we expand the school's catchment area to include more districts.

To carry out this adjustment, we rank schools on the basis of the (absolute value of) their prediction error, dealing with the schools that have the greatest excess demand/supply first. If the school has excess demand, we reassign the Census block that has the closest second school (recalling that we record the five closest schools to each Census block, in order), as long as that second school has excess supply. If a school has excess supply, we reassign to it the closest school district currently assigned to a school with excess demand. We make gradual adjustments, reassigning one Census block from each school in disequilibrium each iteration. This gradual adjustment of assignments of Census blocks to schools continues until we have 'market clearing' (within a certain tolerance) for each school. Our actual algorithm converges quickly in practice, and produces plausible adjustments to the initial, closest-school assignment.

**Land use.** Information on land use/land cover digital data is collected by USGS and converted to ARC/INFO by the EPA available at: <http://www.epa.gov/ost/basins/> for 1988. We have calculated for each Census block, the percentage of land in a 1/4, 1/2, 2, 3, 4 and 5 -mile radii that is used for commercial, residential, industrial, forest (including parks), water (lakes, beaches, reservoirs), urban (mixed urban or built up), transportation (roads, railroad tracks, utilities) and other uses.

**Crime data.** Information on crime was drawn from the rankings of zipcodes on a scale of 1-10 on the risk of violent crime (homicide, rape or robbery). A score of 5 is the average risk of violent crime and a score of 1 indicates a risk 1/5 the national average and a 10 is 10 or more times the national average. These ratings are provided by CAP index and were downloaded from APBNews.com.

**Geography and Topography.** The Teale data center in California provided information on the elevation, latitude and longitude of each Census block.

## ESTIMATION APPENDIX

**Introduction.** This appendix provides a full description of the estimation procedure used in our analysis, discussing a number of important details that we abstract from in the main text in to streamline that presentation. As described in the text, we assume that the housing market can be characterized by a set of housing types that is a subset of the full set of available houses, letting the supply of housing of type  $h$  be given by  $S_h$ . Moreover, we assume that each household observed in the sample represents a continuum of households with the same observable characteristics. In turn, the distribution of idiosyncratic tastes  $\mathbf{e}_h^i$  maps into a set of choice probabilities that characterize the distribution of housing choices that would result for the continuum of households with a given set of observed characteristics.

**Estimation.** Estimation of the model follows a two-step procedure closely related to that developed in Berry, Levinsohn, and Pakes (1995). As in the text, we rewrite the indirect utility function as:

$$(7) \quad V_h^i = \mathbf{d}_h + \mathbf{I}_h^i + \mathbf{e}_h^i$$

where

$$(8) \quad \mathbf{d}_h = \mathbf{a}_{0X} X_h + \mathbf{a}_{0Z} \bar{Z}_h - \mathbf{a}_{0p} p_h + \mathbf{x}_h$$

and

$$(9) \quad \mathbf{I}_h^i = \left( \sum_{k=1}^K \mathbf{a}_{kX} Z_k^i \right) X_h + \left( \sum_{k=1}^K \mathbf{a}_{kZ} Z_k^i \right) \bar{Z}_h - \left( \sum_{k=1}^K \mathbf{a}_{kp} Z_k^i \right) p_h.$$

In equation (8),  $\mathbf{d}_h$  captures the portion of utility provided by housing type  $h$  that is common to all households, and in (9),  $k$  indexes household characteristics. When the household characteristics included in the model are constructed to have mean zero,  $\mathbf{d}_h$  is the *mean indirect utility* provided by

housing choice  $h$ . The unobservable component of  $\mathbf{d}_h, \mathbf{x}_h$ , captures the portion of unobserved preferences for housing choice  $h$  that is correlated across households, while  $\mathbf{e}_h^i$  represents unobserved preferences over and above this shared component.

The estimator is a two-step procedure. The first step selects the heterogeneous parameters  $\mathbf{I}_h$  and mean indirect utilities  $\mathbf{d}_h$  that maximize the probability that the model correctly predicts each individual's location decision conditional on the full set of observed housing and neighborhood attributes, including those endogenously determined. Formally, the validity of this first step requires two assumptions: that the observed location decisions are individually optimal, given the collective choices made by other households and the vector of market-clearing prices, *and* that households are sufficiently small such that they do not interact strategically with respect to particular draws on  $\mathbf{e}$ . This latter assumption ensures that households can each effectively integrate out the idiosyncratic preferences of all others when making their own location decisions and so that no household's particular idiosyncratic preferences affect the equilibrium. In this way, the vector of idiosyncratic preferences  $\mathbf{e}$  is uncorrelated with the prices and neighborhood sociodemographic characteristics that arise in any equilibrium.

The first-stage of the estimation procedure is equivalent to a Maximum Likelihood procedure that treats housing prices and neighborhood sociodemographic characteristics as exogenous from the individual's point-of-view. Importantly, the assumption that prices and neighborhood sociodemographic characteristics are uncorrelated with the vector of idiosyncratic preferences  $\mathbf{e}$  does not imply that they are uncorrelated with the full error term, as we explicitly allow for a portion of unobserved preferences,  $\mathbf{x}$ , that is correlated with price and endogenous neighborhood characteristics in equilibrium. This correlation is addressed in the second stage of the estimation procedure, in which the vector  $\mathbf{d}$  estimated in the first stage is decomposed into components.

Operationally, then, for any combination of the heterogeneous parameters in  $\mathbf{I}$  and mean indirect utilities,  $\mathbf{d}_h$ , the model predicts the probability that each household  $i$  chooses house type  $h$ . We assume that  $\mathbf{e}_h^i$  is drawn from the extreme value distribution, in which case this probability can be written:

$$(10) P_h^i = \frac{\exp(\mathbf{d}_h + \hat{\mathbf{I}}_h^i)}{\sum_k \exp(\mathbf{d}_k + \hat{\mathbf{I}}_k^i)}$$

Maximizing the probability that each household makes its correct housing choice gives rise to the following log-likelihood function:

$$(11) \ell = \sum_i \sum_h I_h^i \ln(P_h^i)$$

where  $I_h^i$  is an indicator variable that equals 1 if household  $i$  chooses house type  $h$  in the data and 0 otherwise. The first step of the estimation procedure consists of searching over the parameters in  $\mathbf{I}$  and the vector of mean indirect utilities to maximize  $\ell$ . Notice that the likelihood function developed here is based solely on the notion that each household's residential location is optimal given the set of observed prices and the location decisions of other households.

**The Mechanics of the First Step of the Estimation.** Intuitively, it is easy to see how this first step of the estimation procedure ties down the heterogeneous parameters – those involving an interaction of household characteristics with housing and neighborhood characteristics. If more educated households are more likely to choose houses near better schools in the data for instance, a positive interaction of education and school quality will allow the model to fit the data better than a negative interaction would.

What is less intuitive is the way the vector of mean indirect utilities is determined. To better understand the mechanics of the first step of the estimation, it is helpful to write the derivative of the log-likelihood function with respect to  $\mathbf{d}_h$ :

$$(A4) \quad \frac{\partial \ell}{\partial \mathbf{d}_h} = \sum_{i \in h} \frac{\partial \ln(P_h^i)}{\partial \mathbf{d}_h} + \sum_{i \notin h} \frac{\partial \ln(P_h^i)}{\partial \mathbf{d}_h} = \sum_{i \in h} (1 - P_h^i) + \sum_{i \notin h} (-P_h^i) = S_h - \sum_i (P_h^i) = 0$$

In this way, the likelihood function is maximized at the vector  $\mathbf{d}$  that forces the sum of the probabilities that each observed individual chooses each house type to equal the total supply of such houses:  $\sum_i (P_h^i) = S_h \forall h$ . That this condition must hold for all house types results from a

fundamental trade-off in the likelihood function. In particular, an increase in any particular  $\mathbf{d}_h$  raises the probability that each household in the sample chooses house type  $h$ . While this increases the probability that the model correctly predicts the choice of the households that actually reside in houses of type  $h$ , it decreases the probability that all of the other households in the sample make the correct choice. Thus the first step of the estimation consists of choosing the interaction parameters that best match each individual with their chosen house, while ensuring that total predicted demand equals supply for each house type.

For any set of interaction parameters (those in  $\lambda$ ), a simple contraction mapping can be used to calculate the vector  $\mathbf{d}$  that solves the set of first order conditions:  $\sum_i (P_h^i) = S_h \forall h$ . For our application, the contraction mapping is simply:

$$(A5) \quad \mathbf{d}_h^{t+1} = \mathbf{d}_h^t - \ln \left( \sum_i \hat{P}_h^i / S_h \right)$$

where  $t$  indexes the iterations of the contraction mapping. Using this contraction mapping, it is possible to solve quickly for an estimate of the full vector  $\hat{\mathbf{d}}$  even when it contains a large number of elements, thereby dramatically reducing the computational burden in the first step of the estimation procedure.<sup>2</sup>

Notice that while we have not explicitly enforced the market clearing conditions derived above, the conditions that result from maximizing the likelihood with respect to  $\mathbf{d}$  are identical to the market-clearing conditions shown in equation (6). Thus, there is a clear duality between the equilibrating role of prices in our characterization of equilibrium in the housing market and the way that the vector of mean indirect utilities is determined as a result of maximizing the likelihood that each household chooses its appropriate house. In the context of the model itself, we provide intuition below as to why the level of mean indirect utility varies across houses in equilibrium.

**Forming an Instrument for Price.** The second step of the estimation procedure is described in detail in the text except for a discussion of how we form an instrument for price. Having estimated the vector of mean indirect utilities in the first step, the second step of the estimation procedure concerns the estimation of the mean preferences parameters shown in equation (8). For general forms of the utility function, both housing price,  $p_h$ , and mean utility,  $\mathbf{d}_h$ , will be correlated with the unobserved housing/neighborhood quality,  $\mathbf{x}_h$ , in equilibrium. In this case, the estimation of equation (8) requires an additional variable that is correlated with  $p_h$  but not with unobserved housing/neighborhood quality,  $\mathbf{x}_h$  – that is, an instrument for price.

The type of price instrument we propose rises naturally out of the sorting model when households value only the features of their own house and attributes of the surrounding neighborhood, where the size of this neighborhood could be potentially quite large. That is, as long as households do not value the features of housing and neighborhoods beyond some threshold distance from their own

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<sup>2</sup> It is worth emphasizing that a separate vector  $\mathbf{d}$  is calculated for each set of interaction parameters – and at the optimum, this procedure returns the ML estimates of the interaction parameters and the vector of mean indirect utilities  $\mathbf{d}$ .

home when making their residential location decision, the exogenous attributes of houses and neighborhoods that are located beyond this threshold serve as suitable instruments. In developing this type of instrument, we exploit an inherent feature of the sorting process – that the overall demand for houses in a particular neighborhood is affected not only by the features of the neighborhood itself but also by the way these features relate to the broader landscape of houses and neighborhoods in the region. Thus we assume that the exogenous attributes of houses and neighborhoods a sizeable distance away from a house influence the equilibrium in the housing market, thereby affecting prices, but have no direct effect on utility.

In practice, the precision of the estimation is improved significantly when the logic of this IV strategy is used to construct a single instrument for price that approximates the optimal instrument. The optimal instrument for  $p_h$  in the mean indirect utility regression is given by:

$$(A6) \quad E\left(\frac{\partial \mathbf{x}_h}{\partial \mathbf{a}_{0,p}}\right) = E(p_h | \Omega)$$

- that is, the expected value of  $p_h$  conditional on the information set  $\Omega$ , which contains the full distribution of *exogenous* choice characteristics ( $X_h$ ) and individual characteristics ( $Z^i$ ). Notice that this instrument implicitly incorporates the impact of the full distribution of the set of choices in exogenous characteristic space as well as information on the full distribution of observable household characteristics into a single instrument for price.

For computational purposes, we use a well-defined instrument that maintains the inherent logic of this optimal instrument while being straightforward to compute. This ‘quasi-’ optimal instrument is based on the predicted vector of market-clearing prices calculated for an initial estimate of the parameter values with the vector of unobserved characteristics  $\xi$  set identically equal to zero and using only the exogenous features of locations.<sup>3</sup> Operationally, the estimation proceeds as follows:

1. Include a full set of variables in the model that account for housing and neighborhood attributes in the region that households value directly when making their location decision – for the analysis conducted below, we assume households care about the housing stock and land use within five miles of their house.
2. Using a conjecture of the model’s parameters, setting  $\mathbf{x}_h=0$  for all  $h$ , and including only *exogenous* choice characteristics in  $X$ , calculate the vector of housing prices that clears the market,  $\hat{p}^*(X_h, Z^i)$ . In practice, we make a reasonable conjecture as to the price coefficient and then simply run equation (12), which brings price to the left hand side of equation (8), via OLS. In calculating the vector of market clearing prices, we use only variables that describe housing and land use – not those related to neighborhood sociodemographic composition, tests scores, or crime.
3. Using  $\hat{p}^*$  as an instrument for  $p$ , estimate the mean indirect utility regression.<sup>4</sup>

Like the optimal instrument, the instrument that we propose provides a measure of the way that the full landscape of possible choices affects the demand for each house/neighborhood. In essence, this instrument extracts additional information from  $\Omega$  than that which is contained in the vectors of choice characteristics  $X$  already appearing in estimating equation (8). In the regressions reported in the main text, we include a full set of controls for the characteristics of the house itself and

<sup>3</sup> This condition corresponds to using the prediction at the mean instead of the expected value.

<sup>4</sup> In practice, we repeat Steps 2 and 3 of this procedure using the estimated parameters from step 3 to construct a new price instrument in step 2 for the next iteration. While this iterative process is not necessary to ensure consistency, it does ensure that the final estimates are not sensitive to our initial conjecture of the coefficient on price. For this reason, we believe that this iterative procedure is likely to be more efficient than applying the procedure once, but do not have a proof of this.

its neighborhood as well as five variables that described land use<sup>5</sup> and six variables that describe the housing stock<sup>6</sup> in each of the 1, 2, 3, 4, and 5 mile rings around the house. In sum, the additional information embedded in our instrument derives from the exogenous features of the housing stock and land use in a region beyond five miles from the house in question. Importantly, this information is collapsed into a single instrument that uses this information in a concise manner consistent with the logic of the sorting model.

In regressions that correspond to the hedonic price regressions reported in Table 4, the price instrument, which is derived entirely from the exogenous characteristics of the alternatives and the distribution of household characteristics in the population, adds significantly to the predictive power of these regressions. In each specification, the optimal price instrument is strongly predictive of price, over and above the set of variables included in  $\mathbf{X}$ , increasing the  $R^2$  of each regression by approximately 2-4 percentage points.

**Characterizing the Housing Market – A Practical Issue.** A final practical issue for estimation concerns the way the choices that characterize the housing market should be defined. This modeling decision essentially corresponds to an assumption as to the way demand for particular houses in the market is determined. The trade-offs implicit in the required assumption can be seen using a simple example. Consider a city neighborhood with two types of housing structures, one of which is more prevalent than the other, with all houses in the neighborhood selling for the same price. Also, to simplify this discussion, assume that households have identical tastes. In this case, if we characterized the choice set as the two types of structures, we would infer that the more prevalent structure provided higher mean direct utility; this is necessary to explain why more households choose that structure given equal prices. If, on the other hand, we characterized the housing market by randomly drawing a subset of the houses in the neighborhood, we would infer that all of the houses in the neighborhood offered the same utility. We do not see any strong *a priori* for making one of these choices versus the other. Moreover, given that any definition of ‘type’ would be based only limited characteristics observed in the data, we elect the second option described above, simply characterizing housing types as the 1-in-7 random sample of the houses observed in our Census dataset. This characterization also facilitates comparisons with the hedonic price regression literature; with this characterization of the choice set, a hedonic price regression corresponds to estimating mean preferences under the assumption of no heterogeneity in household tastes.<sup>7</sup>

**Asymptotic Properties of the Estimator.** As described in McFadden (1978), an attractive aspect of the underlying IIA property for each individual is that we can estimate the model using only a sample of the alternatives not selected by the individual. This permits estimation despite having many alternatives – i.e., many distinct house types. More generally, our problem fits within a class of models for which the asymptotic distribution theory has been developed. In this section, we summarize the requirements necessary for the consistency and asymptotic normality of our estimates and provide some intuition for these conditions.

In general, there are three dimensions in which our sample can grow large, namely as  $H$  (number of housing types),  $N$  (number of individuals in the sample), or  $C$  (number of non-chosen alternatives drawn for each individual) grow large. For any set of distinct housing alternatives of size  $H$  and any random sampling of these alternatives of size  $C$ , the consistency and asymptotic normality of the first-stage estimates  $(\delta, \mathbf{q}_I)$  follows directly as long as  $N$  grows large. This is the central result of McFadden (1978), justifying the use of a random sample of the full census of alternatives. Intuitively, even if each household is assigned only one randomly drawn alternative in addition to its

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<sup>5</sup> That is: percent industrial, percent commercial, percent residential, percent open space, and percent other.

<sup>6</sup> Percent owner-occupied single family homes with 7 rooms or more; Percent owner-occupied single family homes with less than 7 rooms; Percent renter-occupied single family homes; Percent renter-occupied units in large apartment buildings; Percent of units in small apartment buildings; Percent other.

<sup>7</sup> Nothing theoretically prevents estimation of the model under an alternative assumption concerning housing choices.

own choice, the number of times that each house is sampled (the dimension in which the choice-specific constants are identified) grows as a fixed fraction of  $N$ .

If the true vector  $\mathbf{d}$  were used in the second stage of the estimation procedure, the consistency and asymptotic normality of the second-stage estimates  $\mathbf{q}_d$  would follow as long as  $H \rightarrow \infty$ .<sup>8</sup> In practice, ensuring the consistency and asymptotic normality of the second-stage estimates is complicated by the fact the vector  $\mathbf{d}$  is estimated rather than known. Berry, Linton, and Pakes (2002) develop the asymptotic distribution theory for the second stage estimates  $\mathbf{q}_d$  for a broad class of models that contains our model as a special case and, consequently, we employ their results. In particular, the consistency of the second-stage estimates follows as long as  $H \rightarrow \infty$  and  $N$  grows fast enough relative to  $H$  such that  $H \log H / N$  goes to zero, while asymptotic normality at rate  $\sqrt{H}$  follows as long as  $H^2 / N$  is bounded. Intuitively, these conditions ensure that the noise in the estimate of  $\mathbf{d}$  becomes inconsequential asymptotically and thus that the asymptotic distribution of  $\mathbf{q}_d$  is dominated by the randomness in  $\mathbf{x}$  as it would be if  $\mathbf{d}$  was known.

**A Final Clarification.** As just described, the consistency and asymptotic normality of the second stage estimates requires the number of individuals in the sample to go to infinity at a faster rate than the number of distinct housing units. In light of this requirement, it is important to be clear about the implications of the way that we characterize the housing market in the paper. In particular, we characterize the set of available housing types using the 1-in-7 random sample of the housing units in the metropolitan area observed in our Census dataset. Superficially, this characterization seems to imply that the number of housing types is as great as the number of households in the sample, which appears at odds with the requirements for the establishing the key asymptotic properties of our model.

Importantly, however, the housing market may in fact be characterized by a much smaller sample of houses, with each ‘true’ house type showing up many times in our large sample. Consider, for example, using a large choice set of 250,000 housing units, when the market could be fully characterized by 25,000 ‘true’ house types, with each ‘true’ house type showing up an average of 10 times in the larger choice set. On the one hand, the 250,000 observations could be used to calculate the market share of each of the 25,000 ‘true’ house types, with market shares averaging 1/25,000 and the second stage  $\mathbf{d}$  regressions based on 25,000 observations. On the other hand, separate market shares equal to 1/250,000 could be attributed to each house observed in the larger sample and the second stage regression based on the larger sample of 250,000. These regressions would return exactly the same estimates, as the former regression is a direct aggregation of the latter regression. What is important from the point-of-view of the asymptotic properties of the model is not that the number of individuals increases faster than the number of housing types used in the analysis, but rather that the number of individuals increases fast enough relative to the number of truly distinct housing types in the market. That the number of distinct housing types in the market grows at a rate slower than the number of households certainly seems a very reasonable assumption.

## RESULTS APPENDIX

In order to judge whether our parameter estimates are reasonable, it is helpful to compare them to analogous hedonic price regressions. This Appendix carries out such a comparison, complementing the discussion in Section 6.

Hedonic price regressions arise as a direct restriction on our residential sorting model when there is no heterogeneity in household preferences for each house.<sup>9</sup> Equation (8), which describes mean preferences in the general case where preferences are heterogeneous, can be re-written:

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<sup>8</sup> This condition requires certain regularity conditions. See Berry, Linton, and Pakes (2002) for details.

<sup>9</sup> See Bayer, Ferreira and McMillan (2003) for more details. For a more careful discussion as to how the discrete choice model described here relates to continuous choice models commonly used in the hedonics literature (including Rosen (1974), Brown and Rosen (1982), Epple (1987), Bartik (1987), and Ekeland, Heckman, and Nesheim (2002), Bajari and Benkhard (2002)), see Bayer, McMillan, and Rueben (2004b).

$$(12) \quad p_h + \frac{1}{a_{0p}} \mathbf{d}_h = \frac{a_{0x}}{a_{0p}} X_h + \frac{1}{a_{0p}} \mathbf{x}_h$$

This bears more than a passing resemblance to a hedonic price regression. It makes clear that, in the presence of heterogeneous preferences, the mean indirect utility  $\mathbf{d}_h$  estimated in the first stage of the estimation procedure provides an adjustment to the hedonic price equation so that the price regression accurately returns mean preferences.

It is useful to spell out the significance of (12). We can distinguish the willingness to pay of the *marginal* household, setting the equilibrium price of a given attribute, and that of the *mean* household. The equilibrium price function, approximated by a hedonic price regression, measures the marginal willingness to pay (MWTP) of the marginal household, and in the presence of heterogeneity, this may differ markedly from the MWTP of the mean household. The sorting model controls for which individual in the distribution of tastes sets the price of a given attribute given the supply of that attribute. This provides an adjustment that reflects the difference between this household's valuation and that of the mean household so that the adjusted hedonic price regression accurately reflects mean preferences.

The final three columns of Table 5 present the results from three hedonic price regressions analogous to those reported in the first three columns for the full sorting model. Comparing the hedonic price regressions to the mean MWTP estimates derived from the sorting model reveals that while the estimates related to housing characteristics, school quality, and crime remain similar in the hedonic price regression, those related to neighborhood sociodemographic composition and race in particular change dramatically. To explain the results, consider the estimated mean coefficient on percent black, which is -\$234 in the full sorting model as opposed to only -\$40 for the hedonic price regression. For simplicity, assume that neighborhoods are completely segregated, so that the equilibrium price of a black neighborhood is driven by the MWTP of the black household with the least MWTP for a black neighborhood (or, alternatively, the white household with the greatest MWTP). Here, the hedonic price regression returns the MWTP of the household on the *margin* between choosing a black versus white neighborhood, which in this case is substantially greater than the MWTP of the *mean* household, which is estimated in the more general sorting model. Put another way, a much lower differential in price between black and white neighborhoods is required to equilibrate the housing market than would be required to make the mean household indifferent between these neighborhoods.

This discussion also makes clear that the racial coefficients in a hedonic price regression do not, in and of themselves, inform us as to whether racial segregation is driven by decentralized preferences or centralized discrimination in the housing market, at least without imposing *a priori* assumptions about the distributions of preferences. In essence, the racial coefficients in the hedonic price regression are determined by the preferences of individuals on the margin between choosing neighborhoods with different racial compositions. If black households all had strong preferences for living with other black households and at least some white households preferred to live with black households, the resulting equilibrium would result in a premium for black neighborhoods *ceteris paribus*. If, on the other hand, white households all had strong preferences for living with other white households and at least some black households preferred to live with white households, the resulting equilibrium would result in a premium for white neighborhoods. Thus, in the absence of centralized discrimination, both positive and negative price differences between black and white neighborhoods may result in equilibrium. This is not to say that centralized discrimination does not have an effect on the coefficients of a hedonic price regression. In fact, the presence of centralized discrimination, which essentially makes it more costly for black households to choose white neighborhoods, is observationally equivalent to stronger preferences among blacks to live with black versus white households. Thus, the presence of centralized discrimination will in general increase the estimated coefficient on percent black in the hedonic price regression as well as the estimated preferences of black households to live with other black households in our model. The *difference* between our estimates of what white versus black households are willing to pay for neighborhoods with varying racial compositions remains informative as to the overall role of race in the housing market, combining the effect of decentralized racial preferences and centralized discrimination.