Essays on Mechanism Choice and Auctions

by

Christoph Bauner

Department of Economics
Duke University

Date: ______________________

Approved:

__________________________
Andrew Sweeting, Supervisor

__________________________
Tracy Lewis

__________________________
Leslie Marx

__________________________
James Roberts

Dissertation submitted in partial fulfillment of the requirements for the degree of Doctor of Philosophy in the Department of Economics in the Graduate School of Duke University

2011
ABSTRACT

Essays on Mechanism Choice and Auctions

by

Christoph Bauner

Department of Economics
Duke University

Date: ______________________

Approved:

__________________________
Andrew Sweeting, Supervisor

__________________________
Tracy Lewis

__________________________
Leslie Marx

__________________________
James Roberts

An abstract of a dissertation submitted in partial fulfillment of the requirements for the degree of Doctor of Philosophy in the Department of Economics in the Graduate School of Duke University 2011
Copyright © 2011 by Christoph Bauner
All rights reserved except the rights granted by the
Creative Commons Attribution-Noncommercial Licence
Abstract

This dissertation consists of three chapters relating to various topics in empirical Industrial Organization. The first two chapters deal with the empirical treatment of sales in online markets. The third chapter explores the level of pass-through for taxes on soft drinks.

In the first chapter I demonstrate that when dealing with online market places it is important to take into account the fact that multiple listings coexist. Traditionally, the economic literature has treated listings as independent. In reality, however, buyers often have the choice between multiple contemporaneous listings. I demonstrate that it is important to take this fact into account since sellers who list their items simultaneously are in direct competition. More specifically, I show that the sale probability of a given item decreases when the number of simultaneous listings increases. Thus, the aforementioned assumption of independence can lead to wrong results.

In the second chapter, I specify and estimate a structural model of mechanism choice in online markets. I consider both sides of the market: On the demand side, buyers’ choices among available listings are equilibrium outcomes of an entry game. On the supply side, sellers take competition into account and make equilibrium decisions when choosing sales mechanisms and prices. I estimate this model using data from sales of baseball tickets on eBay. I find that sellers’ outside options, dynamic incentives, and risk preferences affect mechanism choice. Using the estimation results from
my model I analyze the welfare effects of a hybrid mechanism (buy-it-now auctions) eBay offers. I find that the existence of buy-it-now auctions increases the consumer surplus and reduces the producer surplus. The reason for this is that buy-it-now auctions diminish sellers’ potential for diversification via mechanism choice and thus strengthen competition.

The third and last chapter focuses on the incidence of soda taxes by studying the pass-through level of these taxes. It lays out a framework for thinking about the determinants of the pass-through level. More specifically, it builds theoretical models that examine the pass-through under more complex supply structures with multiple manufactures and retailers. In addition to providing some intuition behind theoretical predictions of the models, this chapter also presents empirical results found in the data along with their implications.
# Contents

Abstract

List of Tables

List of Figures

Acknowledgements

1 Seller Competition in Online Markets: Evidence from eBay
   1.1 Introduction ............................................. 1
   1.2 Market Overview ....................................... 2
   1.3 Data .................................................. 4
   1.4 Empirical Analysis ..................................... 6
   1.5 Conclusion ............................................. 8

2 Mechanism Choice and the Buy-It-Now Auction: A Structural Model of Competing Buyers and Sellers
   2.1 Introduction ............................................. 9
   2.2 Literature Review ...................................... 14
   2.3 Data .................................................. 18
      2.3.1 Market Description ................................. 18
      2.3.2 Primary Data ...................................... 19
      2.3.3 Secondary Data .................................... 20
      2.3.4 Summary Statistics ................................. 22
   2.4 Model ................................................ 24

vi
List of Tables

3.1 Significant Soda Tax by State ........................................ 66
3.2 Small Store Diff-n-Diff Regression Results: ......................... 73
3.3 Large Store Diff-n-Diff Regression Results: ......................... 73
3.4 Simulation Parameters .................................................. 77
3.5 Simulation Results for Different Cases ............................... 78
3.6 Diff-n-Diff Regression Results for Different States: .............. 79
A.1 Regression of Sale for FP Listings ................................... 83
A.2 Regression of Sale for Auctions ....................................... 84
A.3 Regression of Sale for BIN Auctions ................................. 85
A.4 Regression of Revenue for Auctions .................................. 86
A.5 Regression of Revenue for BIN Auctions ............................... 87
B.1 Summary Statistics for listings by mechanism type. ............... 95
B.2 Grouping of rows and row quality index. ............................ 95
B.3 Grouping of sections and section quality index. ..................... 96
B.4 Estimates of demand side parameters. ............................... 101
B.5 Predicted moments for several values of \( N \). ......................... 101
B.6 Predicted and true values for the share of sold items and expected revenue by mechanism. ................................. 102
B.7 Mechanism choice by seller size ..................................... 102
B.8 Risk attitudes by seller size .......................................... 103
B.9 Development of outside options over time . . . . . . . . . . . . . . . . 103
B.10 Development of several measures of ticket quality over time . . . . . 104
B.11 Estimated distributions for sellers’ mechanism costs . . . . . . . . . 104
## List of Figures

<table>
<thead>
<tr>
<th>Figure</th>
<th>Description</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>B.1</td>
<td>Section plan of the Great American Ballpark.</td>
<td>97</td>
</tr>
<tr>
<td>B.2</td>
<td>Average number of available listings over time</td>
<td>98</td>
</tr>
<tr>
<td>B.3</td>
<td>Development of mechanism choice over time</td>
<td>99</td>
</tr>
<tr>
<td>B.4</td>
<td>Timing of bids during the last five days of the auction.</td>
<td>100</td>
</tr>
<tr>
<td>B.5</td>
<td>Distribution of outside option values relative to face value by seller size</td>
<td>102</td>
</tr>
<tr>
<td>B.6</td>
<td>Distribution of small sellers’ outside option values relative to face value</td>
<td>103</td>
</tr>
<tr>
<td></td>
<td>by mechanism.</td>
<td></td>
</tr>
<tr>
<td>B.7</td>
<td>Distribution of large sellers’ outside option values relative to face value</td>
<td>104</td>
</tr>
<tr>
<td></td>
<td>by mechanism.</td>
<td></td>
</tr>
</tbody>
</table>
Acknowledgements

I am deeply indebted to my advisors Andrew Sweeting, Tracy Lewis, Leslie Marx and James Roberts for their invaluable guidance. I also thank Peter Arcidiacono, David Barth, Federico Bugni, Robert Hammond, Kohei Kawamura, Philipp Sadownik, seminar participants at Duke University, HEC Montreal, Universidad Carlos III de Madrid, the University of Massachusetts - Amherst, and particularly Yucai Emily Wang for helpful comments and suggestions. All errors are my own. Finally, I thank Andrew Sweeting who provided the data for chapters 1 and 2 as well as Andrew Sweeting, Carl Mela and Jamie Chriqui who provided the data for chapter 3.
1 Seller Competition in Online Markets: Evidence from eBay

1.1 Introduction

The economic literature on online auctions has traditionally treated all listings as independent. This is at least partly owed to the steep computational burden of considering computation between listings. However, it is clearly an abstraction from reality. In the real world buyers are likely to look at multiple listings before they decide to bid in one of them; and even if that was not the case then a given number of potential buyers splitting up on more listings would reduce the number of bidders per listing and thus the expected revenue.

In this paper I test empirically whether this intuition holds, that is whether competition from similar items influences success of listings. Specifically I include variables describing number and desirability of opposing listings in regressions of revenue and of sale probability. For my estimations I use data from the sale of Major League Baseball tickets on eBay.

The test gets complicated by an endogeneity issue: Some days might feature
stronger demand and these are likely to attract more sellers. Thus, strong competition might actually be a signal for strong demand. Nonetheless, my findings suggest that competition is an important factor that influences revenues and sale probabilities. More specifically, I find that the number of competing listings has a significantly negative effect on the dependent variables. For the average prices of competing listings the effect is not quite as clear. However, according to my estimations a higher average competing price always increases the revenue and in most cases increases the sale probability. These results are consistent with the findings of Chan, Kadiyali and Park (2007).

This paper proceeds as follows: Section 2 describes the institutional details of the market in consideration, section 3 the data. In section 4 I describe my estimation approach and discuss the results. Section 5 concludes.

1.2 Market Overview

To identify the effects of competition in online markets I use data for sales of Major League Baseball (MLB) tickets from the 2007 regular season on eBay. In this section I give a brief overview over the market.

MLB teams or the league itself do not themselves sell tickets on eBay. Instead, they offer tickets for instance through the official MLB website (http://mlb.mlb.com) or at ticket kiosks. These tickets are purchased by fans as well as ticket brokers and scalpers. Offers on eBay come from fans who no longer wish to use previously purchased tickets and from professional resellers. This market is particularly thick for MLB tickets since few holders of season tickets are able to attend all 81 home games.

However, eBay is by no means to only source of tickets in the secondary market. Buyers can buy from scalpers or from professional ticket brokers. Even among online trading platforms there exists a large quantity of competing sites, like eBid, uBid or
onlineauction.com. The largest of these markets is StubHub, an online sale platform specialized on event tickets.

eBay allows private users and small businesses to sell items to each other. Several sales mechanisms are offered; the three most common ones are FP sales, standard auctions and BIN auctions. All three are used for single unit sales. In FP listings, items are available at posted prices. The first buyer who presses the buy button receives the item and has to pay the seller’s price.\(^1\) Auction participants can bid either like in English auctions or like in second-price sealed bid auctions (SPA). The similarity to English auctions comes from the fact that bidders successively raise their bids. The connection to SPAs is two-fold: First, eBay features an automatic bidding system (“proxy bidding”) which allows bidders to enter the maximum amount they are willing to bid and then automatically raises the bid whenever necessary to remain the high bidder. This is continued until the maximum amount indicated is reached. Second, eBay auctions have a pre-specified end time (“hard close”) and most bids tend to be submitted close to that time (“sniping”).\(^2\) BIN auctions are a hybrid between auction and FP sale. The first bidder is given the choice between buying for a posted “buy-it-now” price and submitting a bid in the auction setting. In the former case, the buyer receives the item exactly as he would in FP listings. In the latter case, the BIN option disappears and the listing turns into a standard eBay auction.

Since buyers and sellers in online market places do not usually interact repeatedly, fraud is a major concern on the websites of eBay and its competitors. To address this issue, eBay uses a reputation system. After each transaction, both the buyer and the

\(^1\) eBay does not speak of fixed price listings on their website. Instead, these listings are called “Buy-It-Now”, but no auction option is offered. In contrast, BIN auctions feature both the Buy-It-Now option and the auction alternative.

\(^2\) Roth and Ockenfels (2002) and Ockenfels and Roth (2006) among others provide evidence for the existence of sniping.
seller have the opportunity to indicate their satisfaction with their counterparty’s conduct. Feedback consists of a positive, neutral, or negative rating and a short comment. Buyers’ comments often include remarks about the seller’s communication style, shipping speed, and accuracy of description. Buyers observe a feedback score and all feedbacks from the last twelve months before they submit a bid. As previous researchers have shown, sellers’ feedback scores are an important determinant of the sale price achieved and thus provide an incentive against fraudulent behavior.⁴

1.3 Data

For the estimation I use data from eBay. The data was acquired through Advanced E-Commerce Research Systems. It consists of listings for tickets of the 2007 regular season. There are listings for most regular season games in the dataset; however three home games of the Tampa Bay Rays which were played in Orlando are excluded. I also exclude home games of the Colorado Rockies since these are the only games for which I do not observe the face value of these tickets. In addition for each listing I see the mechanism chosen, the seller’s identification number, the auction start and end time, the start price (auction start price or fixed price) and the BIN price if applicable. I further observe the number of seats available, the row and section of the seats and the game (home team, away team and game date). Additionally, my data has flags that indicate whether a secret reserve price was set⁴ as well as whether the seller used certain options that are meant to advertise listings to buyers like using bold text, including photographs and so on. For each bid⁵ I observe the listing it pertains to, the time and date of submission, a bidder identification number, the

---

⁴ See for instance Lucking-Reiley et. al. (2007).

⁵ In eBay auctions, sellers can set up to two different reserve prices. The first one is public and is called the “start price”. The second one is secret. Bids below the start price are not accepted. Bids above the start price but below the secret reserve price are accepted, but the item will not be sold unless at least one bid exceeds the secret reserve price.

⁶ In this context I use the word “bid” rather loosely both for auction bids and for FP purchases.
bid type, the bid amount, an indicator for whether the bid was successful, the final price extended to this bidder (0 if the bid was not successful), the bidder feedback score and the seller feedback score.

In order to get a more homogeneous dataset I drop multi-unit listings and items listed as personal offers, accounting for 1.29% and 1.25% of listings, respectively. The remaining listings are FP listings (28.24%), auctions (38.04%) or BIN auctions (33.51%). I also remove some outliers in my data. In particular, I drop listings which apparently achieved prices of more than $500 per ticket (0.05%) and listings that start more than 300 days before the game (0.01%).

In the final dataset 62.74% of listings start within one month of the game day and 86.59% within 100 days. The overwhelming majority of listings is for pairs of tickets (87.36%). The next most frequent number of tickets is four (8.89%) followed by three tickets (1.75%).

Average fixed prices are about 2.16 times the face value of the tickets; naturally, the average reserve prices are much lower at .76 times the face value. However, both of these values vary significantly. Listings of the different types fare very differently. Auctions are most likely to result in a sale (61.2%) followed by BIN auctions (44.0%) and FP listings (18.0%). However, revenue in case of sale shows the opposite ordering: FP listings achieve the highest revenue relative to face values (2.12), BIN auctions come in second (1.64) and auctions are last (1.41).

Every seller in my dataset has a feedback score assigned. This is a number that sums up how many positive and negative reviews the seller received. As the results in the next section will show, the feedback score significantly influences sale probabilities and expected revenues.\textsuperscript{7} 99.99% of sellers have positive feedback scores and for

\textsuperscript{6} This shows categories like “Valid Bid”, “Fixed Priced Item Purchase”, and “Auto Retracted Bid”.

\textsuperscript{7} Lucking-Reiley, Prasad and Reeves (2007) find that feedback scores are important determinants of revenue; negative feedback scores have a much stronger impact than positive ones.
94.08% the value is above 10; the median is 435 and the maximum is 109990.

For an extra fee, the so-called listing upgrade fee, sellers on eBay can make their listing stand out by having it highlighted, adding pictures, etc. Sellers used one of these measures for 29.4% of listings; two for 8.3% of listings and more than two for 1.7% of listings. The most popular ways to increase the attractiveness of a listing is the gallery feature, which allows adding pictures, one of which is shown in the list of search results. Sellers used this feature in 24.4% of listings. The second most popular listing upgrade (used in 13.0% of cases) is scheduling a listing in advance. This allows a seller to have his listing end during desirable times when more buyers log into eBay; presumably this is particularly useful for auctions since many bids are submitted during the last hour of the listing. As the next section will show using these features significantly improves sale probabilities and expected revenues.

1.4 Empirical Analysis

In this section I describe the strategy employed to uncover the effect of competition. If competition does not play a major role in online markets then sale probabilities and revenues should not significantly change in with variables such as number and price of competing listings. In order to determine these effects I regress variables describing the success of a listing (for instance revenue) on listing and item characteristics and variables measuring competition from other listings. It is worth noting that there exists an endogeneity problem: If sellers know which games and which days are likely to feature high demand it is to be expected that profitable game/day combinations attract many listings and therefore show a strong competition. If this effect is not sufficiently accounted for the coefficients on competition variables might show the wrong sign. In order to avoid this problem I include try to control for game and day effects: I use a model with game fixed effects; I also include variables accounting for the time from the listing start to the game day.
In these regressions I use the number of competing listings as well as the average price of the competing listings of each type as explanatory variables. This poses the problem to define which listings are in direct competition. For FP listings this is relatively easy. Since buyers have the possibility to buy at any given time I assume that all FP listings that have any overlap are in direct competition. For auction listings this is not as clear since, as noted above, most bids are submitted in the closing hours of auctions. Therefore I take auctions only only on their last day into account.

Tables A.1 to A.3 show regressions of a dummy that indicates whether an item was sold on item, listing and seller characteristics as well as on variables capturing the intensity of competition. The regressions were performed separately for FP listings, auctions and BIN auctions.

Relative price refers to the fixed price or reserve price, respectively, divided by the face value and the number of tickets. As mentioned earlier, eBay allows sellers to “advertise” for their product through measures intended to increase visibility of the listing such as bold print or including their listing among “featured” items. eBay charges extra fees for these services. Fee dummy measures whether any such fee has been incurred by the seller.

In all three cases most coefficients have the expected sign: A higher relative price significantly reduces the sale probability, visibility increases it. Sellers with low feedback scores (defined as feedback score smaller than 10) are significantly less likely to sell.

The regressions also provide robust support for competition between listings. The more listings are held simultaneously the lower the sale probability. However, the effect of competing listings’ prices is less clear: The average competing fixed price and the average competing reserve price in BIN auctions have the expected sign in all regressions. The coefficient on the average reserve price in competing auctions,
however, comes out negative in the regression for FP listings and even significantly negative in the one for auctions.

Tables A.4 and ?? report similar regressions of the revenue in auctions and BIN auctions. In these regressions the evidence for competition is even stronger: The coefficients on all competition variables have the expected sign and all but one are significant. The effects of average relative prices are surprisingly large, too. If for instance the average relative fixed price increases by one the revenue in increases by $13.61 in auctions and by $18.56 in BIN auctions.

Taken together these five regressions show that competition is an important factor in the success of eBay listings. An item sells with significantly lower probability and achieves significantly lower revenue if many similar items are offered simultaneously. These effects tend to be the stronger the cheaper the opposing items are sold. The latter is particularly true for revenues, which strongly react to fixed or reserve prices of opposing listings.

1.5 Conclusion

In this paper I study competition in online markets. I find that both sale probability and revenue of listings are significantly affected by the existence of simultaneous listings for similar items. This has implications for how we should model online markets. The commonly used technique of assuming a monopolistic seller who faces multiple buyers might not always be appropriate and results based on this simplification might be questionable when the interaction between listings matters. It is therefore desirable to develop models of online markets that take competition into account. Modelling competition increases the computational burden of estimations and reduce the tractability of models. Therefore, researchers often avoid this in favor of simplicity. However, the results in this paper indicate that this shortcut might be problematic.
Mechanism Choice and the Buy-It-Now Auction: A Structural Model of Competing Buyers and Sellers

2.1 Introduction

Online sales platforms have grown to be a major part of the US and world economy. Goods worth close to 60 billion dollars were sold on the websites of market leader eBay alone in 2009.\footnote{eBay Annual Report. San Jose: eBay Inc., 2009.} The rise of these platforms has brought us an abundance of new sale mechanisms. Particularly popular are mechanisms which incorporate features of both auctions and posted prices, like eBay’s buy-it-now (BIN) auction.

In a buy-it-now auction, the seller sets two prices: A reserve price and a posted so-called “buy-it-now” price. The first arriving bidder has the option to either purchase the good at the buy-it-now price or to submit an auction bid greater than or equal to the reserve price. In the former case, the listing disappears as the item is sold. In the latter case, the listing turns into a standard eBay auction in which anyone can participate. The buy-it-now auction was introduced by eBay in 2000. Many of eBay’s competitors now offer similar mechanisms; examples include eBid’s “Buy
Now” facility and uBid’s “u Buy It” feature. Despite their success, little is known so far about revenue and efficiency implications of these mechanisms.

Besides these questions of mechanism design, online sale platforms also highlight a puzzle of mechanism choice: Why is it that similar or identical goods are sold in so many different ways? This is particularly surprising since one might think that an auction with reserve price \( r \) creates weakly more revenue than a posted price sale with price \( r \). While numerous authors have shown that this naive intuition fails in many settings and showed that simple auctions are not always optimal\(^2\) the question remains why multiple mechanism can coexist in one market.

In this paper, I use sales data from eBay to examine both of these questions. I develop and estimate a model of supply and demand in online markets and investigate the factors that drive mechanism choice. Based on my estimation results I then simulate a counterfactual market in which only auctions and fixed price (FP) listings are available, but no hybrid form of the two. This allows me to gain insight into the effects BIN auctions have on consumer and producer surplus.

My main result sheds light on the welfare effects of BIN auctions. One might think that sellers necessarily benefit from the BIN option. After all, both FP listings and auctions are incorporated into BIN auctions by setting appropriate BIN prices equal to the reserve or to infinity, respectively. That is to say that BIN auctions weakly dominate both other mechanisms in my study. Contrary to this intuition, I find that sellers achieve lower revenues when BIN auctions are available, compared to a situation in which they can choose only between auctions and FP listings. That is, while it is individually optimal to choose a BIN auction these devices strengthen competition so that the new equilibrium is less attractive to sellers. Instead, buyers

\(^2\) Standard auctions have been shown not to be optimal when bidders are asymmetric (Myerson 1981); when bidders have information about other bidders’ valuations (Crémer and McLean 1985 and 1988); when auctions are costly (Wang 1993); or when buyers have interdependent valuations (Campbell and Levin 2006).
benefit from the additional mechanism.

Intuitively, the availability of a hybrid mechanism makes competition between sellers fiercer. Assume there are two sellers, who simultaneously offer their items. Further assume, that some buyers ("FP lovers") prefer to buy at posted prices\(^3\), while others ("neutrals") only care about the price and the quality of the good. Then one seller can list his item at a fixed price, while the other one can target neutrals by offering an auction. In this case, demand should not be very elastic. FP lovers are unlikely to enter the auction, since they prefer posted prices. Neutrals are not prone to enter the FP listings as auctions yield a more efficient outcome: A high value bidder might not receive the item at a posted price because someone else might beat him to it. In the auction however, he has a much higher chance of winning and obtaining the product.

Now compare this to a setting where BIN auctions do exist. We can think of the separation strategy as one seller setting the BIN price equal to the reserve price while the other sets the BIN price equal to infinity. However, now the sellers have incentives to deviate. For instance, the seller with BIN price of infinity (previously the auction seller) will now prefer to reduce the BIN price to a high but finite level. This gives him a chance to sell at a very high price, benefiting from buyers preference for FP purchases. That is, now both sellers will compete for both types of entrants and thus they’ll drive each other’s prices down much more than before.

This result is reminiscent of two papers from the marketing literature: Lal and Matutes (1989) consider a setting in which two stores each offer two goods. Buyers of two types (rich and poor) want to purchase one unit of each good, where rich

\(^3\) There are several reasons why buyers might prefer posted prices over auctions. For instance, risk averse buyers might choose to buy at fixed prices because this allows them to secure a surplus at a certain level, while in auctions they face the risk of competing with a high-value bidder and thus not winning the auction or paying a very high price. Another factor in favor of fixed prices is impatience. Auctions on eBay run for a pre-specified time, while fixed price listings end as soon as a buyer purchases the item. Thus, fixed price listings often allow buyers to receive the item several days earlier than auctions listings.
buyers have higher transportation costs than their poor counterparts. When the sellers split the market, so that each store charges a high price for one and a low price for the other good, they are better off than in an alternative equilibrium where they compete in both goods. This is because in the former case the stores are able to extract the total rent from rich buyers, who are unwilling to drive from one store to the other in order to get the low prices on both goods. Contrary to that, in the latter equilibrium rich buyers benefit from the stores’ competition over poor customers and pay lower aggregate prices. Similarly, Bakos and Brynjolfsson (2000) find that the possibility to bundle goods hurts sellers in a competitive market place. This seems to be the case because by bundling the sellers make their goods more similar to each other and thus increase the substitutability between the two.

To study these effects, I develop a structural model of supply and demand. On both sides of the market, agents make equilibrium decisions. Buyers make purchases based on item and mechanism characteristics. When evaluating the listings offered, they take other buyers’ expected decisions into account; thus, a buyer might be hesitant to enter a listing which he deems particularly popular. So far, this equilibrium approach has to my knowledge not been used; instead, previous authors postulated random arrival or reduced the listing choice on the demand side to a single agent problem by ignoring the interdependence with other agents. The advantage of my approach is that it allows us to gain a deeper insight into competition among sellers.

Sellers, on the other hand, set mechanisms and (reserve) prices based on their revenue expectations, their outside options for the tickets, and their listing costs associated with the mechanisms. They also have expectations over buyers’ and other sellers’ behavior and adjust their decisions accordingly. I contribute to the growing literature of mechanism choice by incorporating BIN auctions into sellers’ mechanism options. BIN auctions account for a large share of eBay sales; ignoring them therefore leads to a misspecified model and thus misestimated welfare implications,
as demonstrated by my counterfactual result.

I estimate this model using sales data on Major League Baseball Tickets on eBay. On the demand side, I specify an equilibrium entry model with random coefficients. This allows me to uncover the distribution of valuations as a function of item characteristics. On the supply side, I back the outside options out of the first-order condition from the sellers’ price-setting problem. My model allows sellers to be heterogeneous with respect to mechanism costs as well as their risk preferences. I assume that sellers’ preferences display either risk-neutrality or constant absolute risk aversion. These two parameters together with revenue expectations explain sellers’ mechanism choices. I estimate the respective distributions of mechanism costs and risk attitudes by a probit approach.

Event tickets are a particularly interesting target of attention because of the dynamics involved. Intuitively, as the game day draws near, the seller’s opportunity costs of sale should fall, since there are fewer possibilities of relisting unsold items. Indeed, I find that the mean outside option decreases over time. This development is reflected in sellers’ mechanism choices, as sellers with more valuable outside options are more likely to sell their items in FP listings, while those with relatively poor outside options prefer auctions. This is because in my data auction listings sell with a higher probability, while FP listings achieve a greater revenue if a sale does occur. I also find evidence for significant levels of risk aversion among sellers and show that this, too, is reflected in their mechanism choice.

The estimation of the structural model allows me to understand how sellers’ make their listing decisions and how buyers’ make entry and purchase decisions. Armed with this information I can uncover the welfare effects of BIN auctions by comparing actual outcomes with those from a simulated marketplace in which only FP listings and auctions exist. I find that buyers benefit from the existence of hybrid mechanisms. The introduction of BIN auctions increases their consumer
rents between 0.55% and 5.78%. Sellers, on the other hand, would prefer a situation without BIN auctions. Their utilities would be between 11.91% and 15.84% higher if only posted prices and auctions would exist. eBay itself also would be better off without BIN auctions, earning almost 11% higher revenues from fees.4

This paper proceeds as follows. Section 2 places this work into the context of the literature. In section 3, I discuss the institutional background and introduce the data. Section 4 presents the structural model. In section 5, I discuss the modeling assumptions in detail. Section 6 explains the estimation strategy. Section 7 discusses the estimation results. In section 8, I study the welfare effects of BIN auctions. Section 9 concludes.

2.2 Literature Review

Ever since its introduction by eBay in 2000, the buy-it-now auction and similar mechanisms have captured the attention of researchers. At first many economists focused on the question of why a finite buy-it-now price might be beneficial to sellers compared to standard auctions. Several reasons have been proposed for why sellers might achieve a higher revenue or higher utility when using hybrid mechanisms:

- risk aversion by buyers or sellers (Reynolds and Wooders (2009), Zhang (2009), Budish and Takeyama (2001), Hidvégí, Wang and Whinston (2006), Ackerberg, Hirano and Shariar (2006, henceforth AHS))

- impatience by buyers or sellers (Matthews (2003), Gallien and Gupta (2007), AHS)

---

4 It is worth noting, however, that this analysis does not take competition effects between different online sales platforms into account. It is possible that buyers, realizing their benefit, are keen to have the BIN option; thus, abandoning the BIN auctions might reduce eBay’s buyer base. If this effect is strong enough, it might offset the calculated revenue loss and make offering BIN auctions an optimal strategy for eBay.
attracting buyers in a model with endogenous entry (Wang, Montgomery and Srinivasan (2004)).

- BIN prices can serve as focal points for buyers’ bidding strategies and thus lead to more aggressive bidding (Yoo, Ho, Tam (2006)).

- In common value settings, buyers tend to put too much weight on their private information which might cause them to buy at inflated BIN prices (Shahriar and Wooders (2007)).

These papers generally treat auctioneers as monopolists. To my knowledge the only work that considers the effects of buy prices in a setting of competing auctions is Kirkegaard and Overgaard (2008). In a theoretical model, Kirkegaard and Overgaard investigate BIN auctions in a setting in which two auctioneers compete for buyers in a sequential game. They show that allowing the first auctioneer to set a BIN price increases this seller’s revenue. However, total revenue is reduced because of the inefficiency introduced by the BIN auction: since a buyer with a low valuation might arrive first it is not clear anymore that the two bidders with the highest valuations are served. In contrast, I consider a much richer setting: in my model, sellers start simultaneous listings and compete with each other for the available demand at any given time. Also, I give sellers the choice between auctions, FP listings and BIN auctions, whereas all papers mentioned above ignore the existence of FP listings.

In my model, buyers actively decide which listing to enter. This is in contrast to the large array of empirical papers which assume random arrival. Several authors before me have dealt with entry problems in similar contexts. Athey, Levin and Seira (2011), Li and Zheng (2009), and Roberts and Sweeting (2010) present models of entry in auctions. In their models auctions are taken individually and the motivation not to participate comes from a monetary cost associated with entry. In contrast,
I allow buyer to choose which listing to enter; that is, there is an opportunity cost of entry since entry in one listing prevents the buyer from entering other concurrent listings. Seim (2006) investigates how firms, upon entering a market, endogenously make a location choice. Similarly, I let buyers choose endogenously among listings; sellers set mechanisms and prices. Agents in both papers face incomplete information when making the entry decision. One important difference between my model and Seim’s is that in her model the expected profits of firms come out of a reduced form assumption, while in mine I calculate buyers’ expected profits according to the actual bidding process they go through. The advantage of the latter approach is that it allows me to more accurately capture the effect of competition.

Finally, and most closely, my work is related to the literature on mechanism choice. On the theoretical side, a number of authors have studied which mechanisms might arise from competition between sellers. Various settings have been studied. Some authors find a multiplicity of equilibria (Coles and Eeckhout (2003), Kultti (1997)). Others argue that auctions might arise naturally from competition between sellers. They show that auctions form the only symmetric (Virag (2007) and Peters (2001)) or stable equilibrium (Lu and McAfee (1996)) in the respective mechanism choice games studied. Similarly, Julien, Kennes and King (2002) find that when sellers play a sequential game in which they first commit to mechanisms and then set prices, auction arise as the only equilibrium strategy.

In terms of empirics, Zeithammer and Liu (2006) consider several explanations for mechanism multiplicity on eBay. They argue that seller heterogeneity, for instance with respect to inventories, at least partially account for the use of different mechanisms. Similarly, Hammond (2010b) presents evidence that seller’s mechanism choices in online markets for compact discs depend on their inventory. Sellers with larger inventory tend to prefer FP sales.
AHS concentrate on the BIN option in eBay auctions. Their agents might choose to purchase at the BIN price rather than bidding in an auction because it allows them to receive the item earlier and with certainty while otherwise they have to go through the auction process. Using data from auctions of different length, AHS are able to separately identify the CARA risk parameter and a discount factor. There are two major differences between their paper and this one: First, in AHS buyers arrive randomly in given auctions while in my model entry in listings is an equilibrium outcome. Second, AHS concentrate on buyers’ behavior while I am mainly interested in sellers’ mechanism choices. The two groups have very different problems to solve. Buyers choose between two pre-determined alternatives, while sellers face a jointly discrete and continuous problem: They simultaneously choose among three mechanisms and set the optimal price. In addition, sellers have to take buyers’ reactions into account, while buyers can maximize as single agents.

Probably most closely related to my work is Hammond (2010a). Hammond uses a data set of compact disc sales on eBay; the mechanisms in the data set include auction and FP listing. Hammond builds a structural model of mechanism choice by buyers and sellers and shows that sellers with better outside options prefer fixed prices while those with low value outside options prefer auctions. Both Hammond and I develop models which allow buyers to choose among listings and sellers among mechanisms. However, my work differs from his in several ways: First, Hammond models buyers’ entry decisions as a single agent problem. In contrast, in my model buyers find an entry equilibrium, taking other buyers’ expected choices into account. This adds insight to the effect of competition among sellers. Second, Hammond ignores BIN auctions; by explicitly modeling them I’m able to study the welfare effects of the introduction of BIN auction.
2.3 Data

In this section, I first give a brief description of the institutional details of the market. I then describe my primary data. Afterwards I introduce two supplementary datasets I use.

2.3.1 Market Description

eBay is a major online sales platform, allowing private users and small businesses to sell items to each other. Several sales mechanisms are offered; the three most common ones are FP sales, standard auctions and BIN auctions. All three are used for single unit sales. In FP listings, items are available at posted prices. The first buyer who presses the buy button receives the item and has to pay the seller’s price.\(^5\) Auction participants can bid either like in English auctions or like in second-price sealed bid auctions (SPA). The similarity to English auctions comes from the fact that bidders successively raise their bids. The connection to SPAs is two-fold: First, eBay features an automatic bidding system ("proxy bidding") which allows bidders to enter the maximum amount they are willing to bid and then automatically raises the bid whenever necessary to remain the high bidder. This is continued until the maximum amount indicated is reached. Second, eBay auctions have a pre-specified end time ("hard close") and most bids tend to be submitted close to that time ("sniping").\(^6\) The aim of sniping is to bid so late that no other bidder has a chance to react by submitting a new, higher bid. As long as other bidders do not bid their valuations, a successful sniper can therefore receive the item at a price significantly below the outcome of a standard English auction. BIN auctions are a hybrid between

\(^5\) eBay does not speak of fixed price listings on their website. Instead, these listings are called “Buy-It-Now”, but no auction option is offered. In contrast, BIN auctions feature both the Buy-It-Now option and the auction alternative.

\(^6\) Roth and Ockenfels (2002) and Ockenfels and Roth (2006) among others provide evidence for the existence of sniping.
auction and FP sale. The first bidder is given the choice between buying for a posted “buy-it-now” price and submitting a bid in the auction setting. In the former case, the buyer receives the item exactly as he would in FP listings. In the latter case, the BIN option disappears and the listing turns into a standard eBay auction.

Since buyers and sellers in online market places do not usually interact repeatedly, fraud is a major concern on the websites of eBay and its competitors. To address this issue, eBay uses a reputation system. After each transaction, both the buyer and the seller have the opportunity to indicate their satisfaction with their counterparty’s conduct. Feedback consists of a positive, neutral, or negative rating and a short comment. Buyers’ comments often include remarks about the seller’s communication style, shipping speed, and accuracy of description. Buyers observe a feedback score and all feedbacks from the last twelve months before they submit a bid. As previous researchers have shown, sellers’ feedback scores are an important determinant of the sale price achieved and thus provide an incentive against fraudulent behavior.\(^7\)

For the estimation I use sales data for Major League Baseball Tickets for home games of the Cincinnati Reds on eBay. The Cincinnati Reds do not themselves sell tickets on eBay. Instead, they offer tickets for instance through their own website (http://cincinnati.reds.mlb.com) or at ticket kiosks. These tickets are purchased by fans as well as ticket brokers and scalpers. Offers on eBay come from fans who no longer wish to use previously purchased tickets and from professional resellers. This market is particularly thick for MLB tickets since few holders of season tickets are able to attend all 81 home games.

2.3.2 Primary Data

My primary dataset contains sales of Major League Baseball tickets on eBay. Particularly, I use sales of tickets for home game of the Cincinnati Reds in the 2007 regular

\(^7\) See for instance Lucking-Reiley et. al. (2007).
season. The data was provided to me by Andrew Sweeting who originally acquired it from Advanced E-Commerce Research Systems, eBay’s official data reseller.\textsuperscript{8} For each listing I see the mechanism chosen, the seller’s identification number, the auction start and end time, the start price (auction start price or fixed price) and the BIN price if applicable. I further observe the number of seats available, the row and section of the seats and the game (home team, away team and game date). Additionally, my data has flags that indicate whether a secret reserve price was set\textsuperscript{9} as well as whether the seller used certain options that are meant to advertise listings to buyers like using bold text, including photographs and so on. For each bid\textsuperscript{10} I observe the listing it pertains to, the time and date of submission, a bidder identification number, the bid type\textsuperscript{11}, the bid amount, an indicator for whether the bid was successful, the final price extended to this bidder (0 if the bid was not successful), the bidder feedback score and the seller feedback score.

After some cleaning, which is described in detail in appendix B, my data holds 7,430 bids and 7,382 listings for pairs of tickets for 78 games. In subsection 3.4 I will further discuss this data and provide some summary statistics.

\textit{2.3.3 Secondary Data}

A problem with any estimation of demand for baseball tickets is that these tickets are highly differentiated. Buyers’ willingness to pay depends on the specific seat location in the stadium as well as the day and opponent of the associated game. In order to address this problem I generate quality indices for games, rows, and sections

\textsuperscript{8} See Sweeting (2010) for an excellent description of his data from which mine is derived.

\textsuperscript{9} In eBay auctions, sellers can set up to two different reserve prices. The first one is public and is called the “start price”. The second one is secret. Bids below the start price are not accepted. Bids above the start price but below the secret reserve price are accepted, but the item will not be sold unless at least one bid exceeds the secret reserve price.

\textsuperscript{10} In this context I use the word “bid” rather loosely both for auction bids and for FP purchases.

\textsuperscript{11} This shows categories like “Valid Bid”, “Fixed Priced Item Purchase”, and “Auto Retracted Bid”.

20
using two sets of secondary data.

First, I have listing data from StubHub.com, an online sales platform specialized on event tickets. Contrary to eBay, on StubHub buyers do not see who they buy from. However, StubHub guarantees that the buyer receives tickets no worse than the ones purchased. For 680,495 listings on StubHub I observe home team, away team and game date, number, row and section of tickets and sale price.

Secondly, I have attendance data for all 81 Cincinnati Reds home games of the 2007 regular season. I collected these from www.baseball-reference.com, a website that provides a variety of baseball statistics for past seasons as well as the current one.

I use these data to generate quality indices for games, rows, and sections. This is based on the idea that StubHub users are representative of the total baseball fan population, so that tickets listed for high prices on StubHub are generally more desirable. For the game quality index I also use attendance data, which should give a good indication of how popular certain games are.

For the generation of the game quality index I proceed as follows: For each game I calculate attendance as a percentage of average attendance. Further, I calculate the mean sale price of tickets for this game and divide by the average mean sale price across all games. Both of these numbers should be a fair measure for the relative desirability of games. I then define the game quality index to be the average of the two measures and normalize it to take values between zero and one only.

For row and section quality I first group rows and sections into clusters of rows and sections, respectively\(^{12}\). I do this because for some rows or sections I only have few observations in the StubHub data, so that I would not have accurate information for them otherwise. Then I regress prices paid on a constant, the newly created game quality index and dummies for each row and section cluster. I take the coefficients

\(^{12}\) In Appendix C I give a detailed description of how I group rows and sections.
on the dummies as measures of seat quality. As last step I normalize the coefficients to be between zero and one.

My indices pass a few sanity checks: In all cases rows have (weakly) higher index values if they are closer to the field. Sections closer to the infield tend to have higher index values than those at the outfield and those on lower ranks have higher values than the “nose-bleed seats” far from the field. Finally, my two measures of game quality are highly correlated, suggesting that they are both decent predictors for ticket prices.

2.3.4 Summary Statistics

Table B.1 provides some basic summary statistics for the remaining data. The first four rows show different measures of ticket desirability. Tickets sold in the three different formats are relatively similar in terms of quality; however, the items in BIN auctions tend to be slightly more attractive while those in standard auction are slightly less attractive than average.

The following four rows show additional measures which can influence a listing’s success. The line “low seller score” refers to a dummy which takes the value one if the seller feedback score is below 10, and zero otherwise. As can be seen, sellers with a low feedback score are more prone to using auction mechanisms than FP listings. One explanation for this might be that inexperienced sellers find auctions a better option, since they do not have the expertise to correctly calculate the optimal posted price. At the same time, being new to selling they have not yet had the time to develop a favorable reputation, so that their feedback scores are lower on average.

“Advertising” measures each sellers’ use of measures to increase the visibility or attractiveness of his listing. Among these are bold font, the inclusion of pictures, and others. I report total number of advertising features used per sellers.

The following lines show measures of listing success. Particularly interesting is
the difference between auction and FP listings. Auctions sell with higher probability; this holds even accounting for listing length. In fact, the average FP listing in my sample is online for a slightly longer time than the average auction. However, if a sale does occur the generated revenue is greater in FP listings. In this sense, FP listings are riskier mechanisms than auctions.

Figure B.2 shows how the number of listings available on eBay develops over time. Not surprisingly, there is a steep upwards trend; the number of listings available at the peak, around one week before the game, is almost ten times as high as five weeks earlier. Trading picks up as eBay users get more information about their valuation for the game. In the last few days before the game, the number of listings decreases significantly. Presumably, the reason for this phenomenon is that it often takes some time to finalize plans: unless seller and buyer live in the same town tickets have to be mailed; also, some buyers need to make travel arrangements; and finally they might already have alternative plans.

In the introduction I hinted at how mechanism choice evolves over time. Figure B.3 shows this in more detail. The share of auctions is relatively constant, while the share of BIN auctions increases and the share of FP listings decreases. Remember from above that FP listings are riskier than auctions; they sell with lower probability but achieve a higher price if a sale occurs. Intuitively then, early on sellers are more inclined to choose FP listings; if no sale occurs they can just relist. However, in later periods the sale probability becomes more important. When there is no time to list a ticket again, auctions and BIN auctions become more attractive since they provide at least some revenue with high probability; obviously this can be achieved in FP listings, too, by setting the price sufficiently low. However, this also limits the maximum revenue the seller can earn, while auctions leave open the possibility of sales for high prices. Of course other factors influence mechanism choice; I will examine some of these when I discuss the estimation results.
2.4 Model

I model trade in a discrete time setting. In each period $t = 1, ..., T$ and for each market $g = 1, ..., G$, there is a set $\mathcal{N}$ of $N$ risk-neutral, short-lived buyers with unit demand. Buyers arrive randomly in the marketplace with probability $\alpha^g$. The arriving buyers observe listings $l = (l_1^g, ..., L^g)$ which from their perspective are exogenous. Each buyer $i$ enters exactly one listing in which he will bid. Before he makes his entry decision he observes listing shocks $\varepsilon_{il}$ and calculates expected profits $u_{il}$ for each available listing. After the entry decisions are made buyers observe their own valuations. That is, their entry decisions are based on expected valuations, while their bids reflect the actual valuations. This assumption is necessary to ensure tractability of the model; in the next section I discuss its justification in detail.

Once buyers have learned their valuations, they submit bids in their chosen listings. After that, winners and prices are determined according to rules which depend on the exact mechanism chosen, and trades are finalized. All buyers leave the market permanently, independent of whether or not they received an item, and new buyers join the pool, thus keeping its size $N$ constant.

There is also a set of sellers, each of whom has exactly one item for sale. Each seller $l$ arrives in the marketplace with probability 1; that is, I do not model sellers’ arrival but instead take sellers’ presence as exogenous. Each seller observes expected demand and supply; to be more precise, sellers know the distribution of valuations as a function of item characteristics; they also correctly predict prices, mechanisms, and item characteristics of competing listings; and finally they know the number of potential buyers. From these pieces of information sellers can determine the probability distribution over revenues for their items.

---

13 Note that I use the same subscript to denote both sellers and listings. I do so in an effort to simplify notation. This approach is valid because of the assumption that each seller offers exactly one item.
Having calculated this, each seller observes two more pieces of information: her opportunity costs of sale $v_l^0$ and her costs associated with each mechanism $m, \omega_{lm}$. The opportunity costs depend on the seller’s outside option. They capture the value the seller associates with retaining her tickets. The mechanism costs, on the other hand, have the function of a random shock in sellers’ mechanism choice. They represent disutility a seller gets from offering a certain mechanism. After the seller observes both types of costs, $v_l^0$ and $\omega_{lm}$, she can find the optimal mechanism and price to sell her item.

The table below summarizes the timing of the model. I discuss the demand side and supply side, respectively, of the model in more detail in the following two subsections.

<table>
<thead>
<tr>
<th>Stage</th>
<th>Description</th>
</tr>
</thead>
</table>
| 1     | Sellers observe  
|       | - expected demand and supply  
|       | - their outside options $v_l^0$  
|       | - their mechanism costs $\omega_{lm}$ |
| 2     | Sellers simultaneously list their items choosing  
|       | - mechanisms $m_l$  
|       | - prices $p_l$ and/or reserve prices $r_l$ |
| 3     | Buyers arrive in the market and observe  
|       | - item characteristics $X_l$  
|       | - mechanisms $m_l$  
|       | - prices $p_l$ and/or reserve prices $r_l$ |
| 4     | Buyers enter exactly one listing irreversibly. |
| 5     | Buyers observe valuations $v_{il}$ and submit bids $b_{il}$. |
| 6     | Winners are determined, payments made and utilities realized. |
| 7     | All agents leave the market. |

2.4.1 Demand Side

After buyers arrive in the market place they decide to enter exactly one listing. To do so, each buyer $i$ calculates his expected utility from entering listing $l$, $U_{il}$. $U_{il}$ consists of two parts: the expected utility from the possibility of buying item $l$ ($u_{il}$) and a shock associated with the listing ($\varepsilon_{il}$). I will discuss below how the $u_{il}$ are calculated.
For now, all we need to know is that $u_{il}$ depends on item characteristics ($X_l$), the mechanism ($m_l$) and the posted price and/or reserve price ($p_l$ and $r_l$ respectively). To simplify notation I define:

$$\theta_l = (X_l, m_l, p_l, r_l)$$

Thus, the listing utility is given by

$$U_{il} = E(u_{il} | \theta_l) + \varepsilon_{il}$$

(2.1)

where the expectation is taken with respect to the number of entrants as well as the buyer’s own valuation. The listing shocks $\varepsilon_{il}$ capture buyer’s idiosyncratic preferences over listings. They are i.i.d. draws according to a type I extreme value distribution.

All buyers simultaneously make their entry decisions based on these expected utilities. From buyer $i$’s perspective this is a standard multinomial choice problem so that his probability of entry in listing $i$, $q_{il}$, can be written as follows:

$$q_{il} = \frac{\exp(E(u_{il} | \theta_l))}{\sum_{j=1}^{L_{il}} \exp(E(u_{ij} | \theta_j))}$$

(2.2)

It is important to note that $q_{il}$ depends on the entry probabilities of other buyers. This is because more bidders in one listing make it less likely to receive the item and might also increase the expected payment. For this reason buyers do not act as single agents but instead follow equilibrium strategies.

Once the entry decisions have been made buyer $i$ perfectly observes his valuation for item $l$ purchased through mechanism $m$, $v_{ilm}$. Buyers have independent private valuations distributed according to the cdf $F_{ilm}(v)$ and its associated pdf $f_{ilm}(v)$. This formulation is very flexible. It allows buyers valuations to depend on item characteristics as well as the relevant sale mechanism. In addition, two buyers can
react in different ways to specific listing features. However, this leads to extremely complicated expressions. In order to simplify I assume that the distributions of valuations are normal: $F_{ilm}(v) = N(\mu_{ilm}, \sigma)$. I also put more structure on buyer heterogeneity by considering two types of buyers: Some buyers (“neutrals”) are indifferent between mechanisms; the others (“FP lovers”) prefer fixed price purchases over auctions. The distribution of valuation then depends on a seller’s type as well as the method of purchase.\footnote{Recall that there are several reasons why buyers might prefer posted prices over auctions. For instance, risk averse buyers might choose to buy at fixed prices because this allows to secure a surplus at a certain level, while in auctions they face the risk of competing with a high-value bidder and thus not winning the auction or paying a very high price. Another factor in favor of fixed prices is impatience. Auctions on eBay run for a pre-specified time, while fixed price listings end as soon as a buyer purchases the item. Thus, fixed price listings often allow buyers to receive the item several days earlier than auctions listings.} I denote neutrals by a subscript $N$ and FP lovers by $FP$, posted price purchases by a subscript $P$ and auction purchases by $A$. I assume that for neutrals $f_{NIA}(v) = f_{NIP}(v)$ holds; this allows me to simplify notation by dropping the mechanism subscript, writing $f_{NI}(v)$. FP lovers receive a constant utility $c$ from buying at posted prices, thus $f_{FPLA}(v) = f_{FPPL}(v + c)$. Whenever possible without creating confusion I will drop the mechanism subscript and use $f_{FP}(v)$ in order to avoid unnecessarily cluttered notation. I denote the number of FP lovers by $N_{FP}$, the number of neutrals by $N_N = N - N_{FP}$ and the share of FP lovers in the whole population of buyers by $\lambda = \frac{N_{FP}}{N}$.

After all buyers learn their valuations, bidding starts. The details of the bidding process depend on the specific mechanism $m_l$. In FP listings, the seller sets a price $p_l$ for the item. Each buyer can submit a bid $b_{il}$ and indicate his willingness to pay the asking price by bidding $b_{il} \geq p_l$. If multiple bidders want to purchase the item, they all obtain the product with equal probability. The randomization is necessary due to the discrete time feature of the model, which establishes a positive probability that multiple buyers try to buy an item simultaneously. Hence, buyer $i$’s expected utility from entering listing $l$ is...
\[ E(U_d|\theta_l, m_l = FP) = \int_{\theta_l}^\infty \sum_{\kappa_l=0}^\infty \frac{v - p_l}{\kappa_l + 1} \rho_l(\kappa_l) f_{dFP}(v)dv + \varepsilon_d \quad (2.3) \]

where \( \kappa_l \) is the number of opponents in listing \( l \) who submit a bid and

\[ \rho_l(\kappa_l) = \sum_{j_1 \in \mathbb{N}} \sum_{j_2 \in \mathbb{N}\{j_1\}} \ldots \sum_{j_{\kappa_l} \in \mathbb{N}\{j_1, \ldots, j_{\kappa_l-1}\}} (\alpha^q)^{\kappa_l} (q_{j_1}q_{j_2}\ldots q_{j_{\kappa_l}}) \quad (2.4) \]

\( \left(1 - F_{j_1lP}(p)\right)\left(1 - F_{j_2lP}(p)\right)\ldots \left(1 - F_{j_{\kappa_l}lP}(p)\right) \)

\( \left(\prod_{k \neq j_1, \ldots, j_{\kappa_l}} (1 - \alpha^q q_{kl}(1 - F_{klP}(p)))\right) \)

is the probability that exactly \( \kappa_l \) want to buy the item.

In auction listings items are sold in a procedure similar to a standard second price sealed-bid auction (SPA). I assume that buyers sequentially have the opportunity to submit bids, but can only do so once. Whoever submits the highest bid wins the item and pays an amount equal to the second highest bid. This structure ensures that, like in SPAs, truthful bidding is a weakly dominant strategy. It also allows me to form expectations over the number of bidders I observe in auctions, a fact that I will use in the estimation.\(^\text{15}\) Buyer \( i \)'s expected profit from auction listing \( l \) is

\[ E(U_d|\theta_l, m_l = A) = \int_{\theta_l}^\infty \sum_{\kappa_l=0}^\infty \int_{-\infty}^v (v - \max(r_l, b)) g^\kappa_l(b)db \rho_l(\kappa_l) f_{dA}(v)dv + \varepsilon_d. \quad (2.5) \]

\(^\text{15}\) Canals-Cerdá and Pearcy (2008) and following literature put less structure on bidding in a fashion that is similar to Haile and Tamer (2003). Their assumptions are strong enough to ensure truthful bidding at least for the bidder with the second-highest valuation. I choose not to follow their approach since it does not give me information on the expected number of bidders observed in the auction.
\(g'_{\kappa_l}(b)\) denotes the probability density function of the highest opposing bid given \(\kappa_l\) opposing bidders. Buyer \(i\) always receives utility at least as big as his listing shock \(\varepsilon_{il}\). In addition, if \(v_{il} \geq r_l\) he wins the item as long as no other bidder has a higher valuation and pays the maximum of reserve price and second highest bid. The sum over the number of opponents is necessary since buyer \(i\) does not know the number of opposing bidders when he makes his entry decision.

BIN auctions are more complicated. After observing his valuation, each buyer decides whether he wants to buy the item or not. There are two conditions under which buyers might want to buy: If the value from buying in an auction is above the reserve price (\(v_{ilA} \geq r_l\)) or if the value from purchasing at a posted price is above the BIN price (\(v_{ilP} \geq p_l\)). As above in the FP listing, if multiple buyers want to purchase the item one of them is randomly selected (“bidder 1”). This buyer is now given a choice between buying at the BIN price or bidding in the auction. In the former case, the buyer receives the item and the listing closes. In the latter case, the listing turns into a standard eBay auction and every buyer who entered can submit a bid. Proposition 1 shows that bidders’ make this BIN choices depending on their valuation: bidders with high valuations choose to buy at the BIN price while bidders with low valuations start the auction.

**Proposition 1.** Assume that the distribution of the highest opposing bid from bidder 1’s perspective is continuous and that \(p_l > v_l\). Then for neutrals there exists a cutoff valuation \(\tilde{v}\) such that bidder 1 chooses the auction for all \(v_{il} < \tilde{v}\) and the BIN purchase for all \(v_{il} \geq \tilde{v}\). For FP lovers there exists a cutoff valuation \(\tilde{v}_{FP}\) such that bidder 1 chooses the auction for all \(v_{ilA} < \tilde{v}_{FP}\) and the BIN purchase for all \(v_{ilA} \geq \tilde{v}_{FP}\). If instead \(p_l = v_l\) then bidder 1 always chooses the BIN purchase.

**Proof.** See Appendix A.

To get some intuition assume \(p_l > r_l\). Then any neutral’s expected profit from
the auction is clearly greater than the one from buying now as long as \( v_{NI} \leq p_i \). Now note that the buy-it-now profit follows a 45°-line since the buy-it-now price is constant. Contrary to that, the expected profit from the auction increases more slowly in \( v_{NI} \) because a win occurs with a probability strictly less than one. That is, in the buy-it-now situation a valuation increase by one unit leads to exactly one unit in higher profits (assuming the original valuation was at least as great as the BIN price). In the auction setting the higher valuation leads to a higher profit of approximately one times the probability of winning.

The expected profit in a buy-it-now auction is given by the following expression:

\[
E(U_i|\theta_i, m_i = BIN) = \sum_{\kappa_{FPi}} \sum_{\kappa_{NI}} \int_{v_i}^{v} \left( \int_{v_i}^{v} (v - \max(r_i, b_i)) g_i(b|\kappa_{FPi}, \kappa_{NI}) db f_{ilAdv} - v_i + p_i f_{ilPdv} \right) \\
+ \left( 1 - \frac{1}{\kappa_{FPi} + \kappa_{NI} + 1} \right) \\
\left( \frac{\kappa_{FPi}}{\kappa_{FPi} + \kappa_{NI}} \frac{F_{FPi}(\tilde{v}_{FP})}{1 - F_{FPi}(\min(r_i, p_i - c))} \right) \\
+ \left( 1 - \frac{\kappa_{FPi}}{\kappa_{FPi} + \kappa_{NI}} \frac{F_{NI}(\tilde{v})}{1 - F_{NI}(r_i)} \right) \\
\int_{r_i}^{v} \int_{r_i}^{v} (v - \max(r_i, b_i)) g_i(b|\kappa_{FPi}, \kappa_{NI}) db f_{ilAdv} dv \right) + \varepsilon_{il}
\]

The first part of equation (2.6) is reminiscent of the related expression for FP listings.
and gives the probability that buyer $i$ has the opportunity to make a BIN purchase. In this case, he receives the expected surplus from the auction if his valuation is below the cutoff or the payoff from the BIN purchase if the opposite is true. If another buyer is drawn as bidder 1, then $i$’s utility is zero unless an auction is chosen. This happens with probability $\frac{\kappa_{FPi}}{\kappa_{FPi} + \kappa_{Ni}} \frac{F_{FPi}(\hat{v}_{FP})}{1 - F_{FPi}(\min(r_1, p_l - c))} + \left(1 - \frac{\kappa_{FPi}}{\kappa_{FPi} + \kappa_{Ni}}\right) \frac{F_{IN}(\hat{v})}{1 - F_{IN}(r_1)}$, where $\frac{\kappa_{FPi}}{\kappa_{FPi} + \kappa_{Ni}}$ is the probability that bidder 1 is an FP lover. The final term is again familiar: Independent of whether and how he buys the item, bidder $i$ always receives at least a listing shock equal to $\varepsilon_{il}$.

I am now in a position to define an equilibrium in this model:

**Definition 1**

A symmetric Perfect Bayesian Equilibrium on the demand side in period $t$ is for each buyer $i$ entry decisions $\xi_i$, bidding strategies $b_{il}$ and beliefs over the number of market participants $\phi_i(k)$ and beliefs over other buyer’s strategies $\tilde{q}_{jli}$ and $\tilde{b}_{jli}$ such that:

- Bidding behavior is optimal given beliefs: $u_{il}(b_{il}) \geq u_{il}(b') \forall l, i, b'$.
- Entry decisions are optimal: For each buyer $i$, $U_{i\xi_i} \geq U_{il} \forall l$ given equations (2.3), (2.5), (2.6) and $i$’s beliefs.
- Beliefs are consistent with the arrival probability, i.e. $\phi_i(k) = \binom{N}{k} (\alpha^\theta)^k (1 - \alpha^\theta)^{N-k}$ for all buyers $i$.
- Beliefs are consistent with entry decisions: For all buyers $i, j$ and listing $l$, $\tilde{q}_{jli} = q_{jl}$.
- Beliefs are consistent with bidding behavior: For all buyers $i, j$ and listing $l$, $\tilde{b}_{jli} = b_{jl}$.
- Buyers of the same type make identical entry decisions: \( q_{il} = q_{FPi} \) if \( i \) is an FP lover and \( q_{il} = q_{NI} \) if \( i \) is a neutral.

The key issue in the equilibrium is to find entry probabilities which are consistent with other buyers’ entry choices. This will be done numerically in the estimation procedure.

2.4.2 Supply Side

Sellers choose mechanisms and set prices for their listings. They need to form expectations over supply and demand before they can make meaningful decisions. While they do not observe the number of buyers present in the market, the total number of potential buyers \( N \) as well as their arrival probability \( \alpha^g \) are common knowledge. The lack of knowledge about competing listings is more problematic since this information directly influences entry probabilities. It does seem reasonable that sellers would have a sound understanding of their competition; therefore I follow Hammond (2010a) in assuming that sellers correctly predict buyers’ entry probabilities, without explicitly modeling how they arrive at these beliefs.

This allows me to specify sellers’ expected utility for each of the three mechanisms. I use the expected utility instead of expected revenue as this is a more flexible formulation allowing for sellers with different risk attitudes. In particular, I consider risk-neutral sellers and those with CARA utility, but could easily accommodate additional specifications. I denote seller \( l \)'s utility function by \( w_l(x) \) and her expected utility from choosing mechanism \( m \) by \( EW_{lm} \). If a sale occurs the seller receives an expected payment; otherwise she keeps the item and gets utility out of her outside
option. For FP listings the expected utility is:

\[
EW_{FP}(p_l) = P_{FP}(p_l) w_l(p_l) + (1 - P_{FP}(p_l)) w_l(v_l^0) 
\tag{2.7}
\]

where

\[
P_{FP}(p_l) = \sum_{\kappa_N} \sum_{\kappa_{FP_l}} \eta_N(\kappa_N) \eta_{FP_l}(\kappa_{FP_l})
\]

\[
\cdot [1 - F_{FP_l}(p_l)^{\kappa_{FP_l}} - F_N(\kappa_N)]
\]

\[
\eta_t(\kappa_{t_l}) = \left( \frac{N_t}{\kappa_t} \right) (\alpha^{\theta} q_{t_l})^{\kappa_{t_l}} (1 - \alpha q_{t_l})^{N_t - \kappa_{t_l}}
\]

\(P_{FP}(p_l)\) is the probability that the item is sold. This happens when at least one buyer enters the listing whose valuation is greater or equal to the posted price \(p_l\).

\(\eta_t(\kappa_{t_l})\) is the probability that exactly \(\kappa_{t_l}\) buyers of type \(\tau\) enter listing \(l\).

The expected utility in auctions is slightly more complicated as now the payment in the case of a sale is a random variable itself. Particularly, the expected utility depends on the probability distribution of the second highest bid, \(H_l(x)\) and its derivative \(h_l(x)\):

\[
EW_{IA}(r_l) = \sum_{\kappa_N} \sum_{\kappa_{FP_l}} \eta_N(\kappa_N) \eta_{FP_l}(\kappa_{FP_l}) \left\{ \int_{\kappa_{t_l}}^{\infty} w_l(x) h_l(x|\kappa_N, \kappa_{FP_l}) dx 
\right. 
\]

\[+ \left[ (1 - F_{FP_l}(r_l))^{\kappa_{FP_l}} F_{FP_l}(r_l)^{\kappa_{FP_l}-1} F_N(\kappa_N) \right] \]

\[+ (1 - F_N(\kappa_N)) \kappa_N F_{NI}(r_l) \kappa_N \left[ F_{FP_l}(r_l)^{\kappa_{FP_l}} \right] w_l(r_l) \]

\[+ F_{NI}(r_l) \kappa_N F_{FP_l}(r_l)^{\kappa_{FP_l}} v_l^0 \left\} \right. 
\tag{2.8}
\]
The integral on the first line of equation (2.8) captures the possibility that at least two bidders have valuations above the reserve price. In this case the expected utility can be found by integrating over the distribution of the second highest valuation. The next two lines specify the possibility of selling for the reserve price. This happens when exactly one entrant has a valuation above the reserve price. The final line states that the seller receives the utility from her outside option if no buyer is willing to pay the reserve price for her item. To calculate the expected utility I still need to find the probability distribution of the second highest valuation. This is given by:

\[ H_l(x|\kappa_{NI}, \kappa_{FPl}) = F_{FPl}(x)^{\kappa_{FPl}}F_{NI}(x)^{\kappa_{NI}-1}(1 - F_{NI}(x))^{\kappa_{NI}} \\
+ F_{FPl}(x)^{\kappa_{FPl}-1}(1 - F_{FPl}(x)) F_{NI}(x)^{\kappa_{NI}} \kappa_{FPl} \\
+ F_{FPl}(x)^{\kappa_{FPl}} F_{NI}(x)^{\kappa_{NI}} \]

That is, the probability that the second highest bid is below some value \( x \) consists of three parts: the probability that exactly one FP lover but no neutral has a value above \( x \), the probability that exactly one neutral but no FP lover has a value above \( x \), and the probability that all valuations are below \( x \).

In BIN auctions I encounter another complication as there are now two ways of selling the item. Let, with a slight abuse of notation, \( \rho_{\tau l}(\kappa_{\tau l}) \) be the probability that there are exactly \( \kappa_{\tau l} \) entrants of type \( \tau \) who want to purchase item \( l \).\(^{16}\) That is, \( \rho_{\tau l}(\kappa_{\tau l}) \) is given by the following two expressions:

\(^{16}\) Recall that in Section 4.1 \( \rho_{\tau l} \) stood for the probability distribution over the number of opposing bidders (from buyer \( i \)'s perspective) who want to buy item \( l \).
\[
\rho_{NI}(\kappa_{NI}) = \left(\frac{N_N}{\kappa_{NI}}\right)^\kappa_{NI} (\alpha^g q_{NI}(1 - F_{NI}(r_l)))^{\kappa_{NI}} (1 - \alpha^g q_{NI}(1 - F_{NI}(r_l)))^{N_N - \kappa_{NI}}
\]

\[
\rho_{FPl}(\kappa_{FPl}) = \left(\frac{N_{FP}}{\kappa_{FPl}}\right)^{\kappa_{FPl}} (\alpha^g q_{FPl}(1 - F_{FPl}(\min(r_l, p_l - c))))^{\kappa_{FPl}} (1 - \alpha^g q_{FPl}(1 - F_{FPl}(\min(r_l, p_l - c))))^{N_{FP} - \kappa_{FPl}} \tag{2.9}
\]

Using this I can write the seller’s expected utility as follows:
\[ EW_{BIN}(p_l, r_l) = \sum_{\kappa_{NI}=0}^{N_{NI}} \sum_{\kappa_{FP}=1}^{N_{FP}} \rho_{NI}(\kappa_{NI}) \rho_{FP}(\kappa_{FP}) \]

\[ \begin{cases} \frac{\kappa_{NI}}{\kappa_{NI} + \kappa_{FP}} & F_{NI}(\bar{v}_{NI}) - F_{NI}(r_l) \\ \frac{1 - F_{NI}(r_l)}{1 - F_{NI}(\bar{v}_{NI})} & \end{cases} \]

\[ \left[ \int_{r_l}^{\infty} \omega(x) \left( \kappa_{NI}, \kappa_{FP}, A_N \right) dx \right] + \mathbb{1}(\kappa_{NI} = 1) F_{FP}(r_l | v_{FP} \geq \min(r_l, p_l - c))^{\kappa_{FP}} \omega_l(r_l) \]

\[ + \frac{\kappa_{NI}}{\kappa_{NI} + \kappa_{FP}} \frac{1 - F_{NI}(\bar{v}_{NI})}{1 - F_{NI}(r_l)} \omega_l(p_l) \]

\[ + \frac{\kappa_{FP}}{\kappa_{NI} + \kappa_{FP}} \frac{1 - F_{FP}(\bar{v}_{FP})}{1 - F_{NI}(\min(r_l, p_l - c))} \omega_l(p_l) \]

\[ + \frac{\kappa_{FP}}{\kappa_{NI} + \kappa_{FP}} \frac{F_{FP}(\bar{v}_{FP}) - F_{NI}(\min(r_l, p_l - c))}{1 - F_{NI}(\min(r_l, p_l - c))} \]

\[ \left( \int_{r_l}^{\infty} \omega(x) \left( \kappa_{NI}, \kappa_{FP}, A_{FP} \right) dx + \mathbb{1}(\kappa_{NI} = 0) \right) \]

\[ F_{FP}(r_l | v_{FP} \geq \min(r_l, p_l - c))^{\kappa_{FP}-1} \omega_l(r_l) \]

\[ + \rho_{NI}(\kappa_{NI} = 0) \rho_{FP}(\kappa_{FP} = 0) \omega_l(r_l^{0}) \]

If at least one entrant wants to buy the item after learning his valuation the following happens: With probability \( \frac{\kappa_{NI}}{\kappa_{NI} + \kappa_{FP}} \) bidder 1 is neutral. He starts the auction if his valuation is below the relevant cutoff; the probability for this is \( \frac{F_{NI}(\bar{v}_{NI}) - F_{NI}(r_l)}{1 - F_{NI}(r_l)} \) since he would not have wanted to buy if his value was below \( r_l \). The seller’s expected
utility from the auction in this case is given in the second line of the equation. I already know at this point that at least one bidder (bidder 1) has a valuation above the reserve price. If there is no other such bidder then the item is sold for \( r_l \). This happens only if \( \kappa_{Nl} = 1 \) since neutral entrants are only willing to buy the item if their value is at least as great as the reserve price. FP lovers, on the other hand, might be willing to buy the item even though their valuation is below \( r_l \). This can happen if their utility from a purchase at a posted price is greater than the difference between BIN price and reserve. The expression \( F_{FP}(r_l | v_{FP} \geq \min(r_l, p_l - c))^{K_{FP}} \) denotes the probability that no FP lover’s valuation for auction purchases is above \( r_l \) conditional on him being willing to purchase the item. With the opposite probability there are at least two buyers who are willing to bid more than \( r_l \) in the auction. In this case I find the expected revenue by integrating over the pdf of the second highest bid conditioned on \( \kappa_{Nl}, \kappa_{FP} \) and on the fact that a neutral bidder chose to start the auction.

The expressions in the case that bidder 1 is an FP lover are very similar to the ones described so that a detailed discussion is not necessary. Therefore I come to the last line of the equation. It indicates that if no entrant is willing to buy the item at either BIN price or reserve price \( (\kappa_{Nl} = \kappa_{FP} = 0) \) the seller retains the goods and receives the utility from her outside option.

Since seller \( l \) knows all the parameters in (2.7)-(2.10) she can maximize these expressions with respect to the price \( p_l \) and/or the reserve price \( r_l \) in order to work out her optimal pricing strategy. This information is also crucial for the choice of the sales mechanism because of course a mechanism is more attractive the more revenue a seller can expect to earn. However, remember that sellers also incur costs when setting up a listing. I denote seller \( l \)'s cost associated with mechanism \( m \) by \( \omega_{lm} \).
Thus, the seller chooses the mechanism which gives her the highest net utility:

$$\pi_{lm} = \max_{(p_t, r_t)} EW_{lm}(p_t, r_t) - \omega_{lm}$$

### 2.5 Discussion of Assumptions

Having introduced the setup I will now devote a few paragraphs to discussing the major assumptions of the model.

**IPV with unit demand** I use data from a secondary market for baseball tickets. These items are bought for private use rather than investment purposes.\(^{17}\) It does not seem likely that one’s utility from visiting a game depends on other buyer’s willingness to pay. Therefore the IPV assumption seems reasonable.

Unit demand might look strange at first given that most people visit events in groups. However, many listings in my dataset are for multiple tickets - in fact, I only use data for pairs of tickets. If instead of buying a pair of tickets one bought two single tickets then seats would potentially be far apart which would defy the purpose of going in groups. Therefore the unit demand assumption also is not restrictive.

**Short-lived buyers** In my model buyers leave the market after one period, whether they successfully purchased an item or not. This is clearly a simplification since in reality buyers who don’t buy today have the possibility of buying tomorrow. However, based on my data this does not seem to create a large problem. In my final dataset 85.13% of buyers submit bids only in a single period, 95.66% in no more than two periods. Even among losing bidders less than 25% return

\(^{17}\) Some re-sellers are active in this market. As explained in the previous section I try to eliminate them from my data.
for a second period, and less than 8% return for two periods or more. Of course a bidder might participate in the market without submitting bids; still I think that these numbers sufficiently justify this assumption. At the same time this limited deviation from reality greatly simplifies my problem since I do not have to consider forward-looking behavior. That is, since buyers don’t care about future periods there is no bid-shading and no updating of expectations I need to keep track of.

**Entry in a single listing** I do not allow buyers to enter several listings in a period. Probably a more appropriate way of modeling within-period behavior would be to set up a search model in which buyers consider the benefits of several listings before they finally bid on their most preferred alternative. However, 83.34% of observed bidders bid only in a single listing in the respective period, 92.77% in no more than two listings. This makes me believe that buyers do not tend to shop around very much. Note that my modeling choice does not mean buyers do not consider multiple listings. In fact, listing choice is an important part of my model. Recall that buyers’ make equilibrium entry decisions based on the characteristics of each listing. I merely do not allow buyers to repeatedly enter and leave listings.

**Simulatenous entry** In reality, buyers arrive in the market and bid at different times. This might influence their behavior because their options will change over time. For instance, two buyers (A and B) arriving at the same time might choose to enter the same listing. If, however, buyer B arrives just slightly after A his listing choice might be altered if A already submitted a high bid for B’s previously preferred listing. In my model I do not consider the sequential nature of the entry game. This again is a simplification of the problem. Otherwise I
would have to keep track of a much larger state space and expectations over it. In the above example, A’s behavior will depend on his expectation of B’s behavior, the possibility of deterring B’s entry by submitting a high bid or a bid in a less attractive listing, as well as the possibility that another buyer arrives after A but before B, possibly submitting a bid that makes A’s listing of choice more desirable to B by raising the price of another item. The data provides some defense for the assumption of simultaneous entry as more than 25% of bids are submitted within the last six minutes before listings close. Figure B.4 shows the timing of auction bids in my dataset during the last five days of auctions. It illustrates how the frequency of bids shoots up as the auction end comes near. Although bidding sometimes happens early on as well, there is a large concentration of bids during the last hour of auctions.

**Unknown valuation** In my models buyers know the distribution of valuations but not the realization of their own valuation before they enter a listing. To some degree this seems defensible since only after making the listing choice they see the seller’s exact description - before, they only see a headline. More realistic would be, however, that buyers have an imperfect signal of their valuation before entry. The problem with modeling this is that it leads to extremely complicated decision making. Each buyer would have a threshold signal for entering a certain listing, but each threshold depends on other listings and on expectations over other buyer’s thresholds. Solving this kind of game would be computationally infeasible. At the same time the gain would be very limited. In reality buyers are more likely to enter listings for which they have high valuations; in my model, on the other hand, buyers with different valuations have the same probability of entering a listing. This might lead to an overestimation of valuations. However, when calculating expected revenues the
same simplification has the contrary effect on results: For a given distribution of valuations, my method leads to a revenue which is below the true one if in reality high-value types are more likely to enter. Intuitively, the two effects cancel out, so that the calculated revenues are accurate.

Existence of FP lovers I allow for the existence of two different types of buyers: neutrals whose utility does not depend on the mode of purchase and FP lovers who prefer buying at posted prices. As mentioned in the introduction, there are several reasons why rational buyers might prefer FP listings. For instance, impatient buyers might hesitate to bid in auctions since eBay auctions usually run for several days so that the buyer has to wait longer for the item. Also, risk aversion might be a reason for preferring FP listings: In FP listings a buyer can secure himself a certain surplus. In auctions the bidding success depends on other bidders’ behavior which makes it less predictable. In any case it should be noted that I do not assume the existence of FP lovers. Instead I allow for it and estimate the share of FP lovers.

Nonexistence of auction lovers It might seem strange that I consider the existence of FP lovers but do not allow for a matching type “Auction lover”. As mentioned above there are several arguments why buyers might prefer posted prices. However, in an IPV framework it is hard to find reasons for favoring auctions. Some buyers might just enjoy the competition aspect and see auctions as a pastime. Such behavior would seem more likely in markets without time restrictions, which makes it much easier to bid repeatedly. Trying to implement auction lovers into the game would also require the econometrician to overcome high hurdles. First, it is not clear whether preferences for auction purchases are identified from the data. In the current model the FP preferences
are identified from the difference in auction and FP revenues. But there is no additional variation that helps to uncover auction preferences. Second, even if one can devise an ingenious method to overcome this issue, doing so might be computationally too costly. As I don’t observe buyers’ types I have to integrate them out; thus, each added type increases the computation time significantly.

**Distribution of valuations** In my model the valuations in listing \( l \) are distributed according to \( N(\mu_{ilm}, \sigma) \). While any functional form is somewhat arbitrary I think that the normal distribution is not a particularly offensive assumption. It is known that many stochastic processes follow a normal distribution at least approximately. Furthermore, the assumption of normality is common in the literature, for instance for error terms. Another assumption I make about the distribution of valuations is that the expected valuation \( \mu_{ilm} \) changes across listings but the standard deviation \( \sigma \) does not. I do this in order to simplify the estimation. In principle the model can easily be generalized to allow for the standard deviation to vary across listings. Merely inserting the new probability distribution into the expressions of the model is all that is necessary when adjusting the model. The reason why I use a constant standard deviation is that I believe that its movement is a secondary effect compared to the change of the expected valuation. Since I already estimate a relatively large number of parameters I sacrifice some flexibility of the model for a reduced computational burden. Another concern might be that this formulation allows for negative valuations. For baseball tickets certainly free disposal is a good description of reality, so taken literally this implication of my distributional assumption seems problematic. However, the distribution left of the reserve price does not matter as of course negative payments are excluded. Thus, the normal distribution gives me the same result as if it was truncated at zero. Having said all this, it is
worth noting that my model and estimation technique can easily accommodate other distributions.

2.6 Estimation

2.6.1 Demand Side

On the demand side I take listing mechanisms and prices as given, so that there are the following variables to estimate: the number of potential entrants \((N)\), the arrival probability \((\alpha)\), the distribution of valuations as a function of covariates \((\beta\) and \(\sigma)\) and the share of FP lovers \((\lambda)\) as well as the intensity of their preferences \((\epsilon)\). I employ a maximum likelihood approach to estimate most of these. However, I devise a different strategy to uncover \(N\), in an attempt to keep both data requirements and computational burden manageable.

First, I divide my data into periods of one day length\(^{18}\) and find the number of bids submitted in each period\(^{19}\). Since according to my model each market participant submits at most one bid, the maximum number of bids submitted in one period is a lower bound for \(N\). In my data this lower bound turns out to be 108. While there is no way of deriving an upper bound I note that in almost 93% of periods no more than 10 bids each are submitted. This suggests that \(N\) is not too far above the lower bound specified before. To find a more precise value I estimate my model assuming

\(^{18}\) I assume that auctions are available only on the last listing day. This is consistent with the observation from the previous section that by far the most bids are submitted in the last minutes before the auction closes. In contrast, FP listings are available on every day from listing start to listing end. BIN auctions are available from the listing start to the day of a BIN sale; or, if the auction option is used, from the start day to the submission of the first bid and again on the last day of the listing.

\(^{19}\) While any choice of period length is somewhat arbitrary, there are two reasons why I believe that my choice of very short (day-long) periods is acceptable: First, given the abundance of outside options like online ticket brokers or scalpers it seems unlikely that a prolonged search through eBay offers is an efficient use of potential buyer’s time. Second, as discussed in section 3, I observe very few bidders who submit bids on different days, suggesting that most users stay in the eBay market only briefly.
different values of $N$ between 100 and 400 and use the estimates which provide the 
best fit. This happens be provided by the model with $N = 200$.

However, it turns out that the exact value of $N$ is almost irrelevant. The purpose 
of the demand side estimation is to gain information about expected revenues and 
sale probabilities which are necessary for the supply side estimation. As table B.5 
shows these values are virtually independent from the choice of $N$. The reason for 
this is that an increase of $N$ is almost perfectly offset by a lower estimate of the 
arrival probability $\alpha^9$, thus leaving the expected number of arriving buyers nearly 
unchanged.\footnote{This is similar to Seim (2006). In her estimation of profits she includes a variable to capture 
the unobserved heterogeneity among different markets. When she assumes a large set of poten-
tial entrants the estimated mean of this market level effect is small and vice versa. Thus, the 
expected number of entrants remains constant, and other estimates are virtually independent from 
the assumed set of potential entrants.}

Having established the number of potential entrants I can now turn to the other 
parameters. Recall from the previous section that the distribution of valuations is 
normal with mean $\mu_{ilm}$ and variance $\sigma^2$. I allow the mean to depend on observable 
ticket characteristics, the buyer’s type $\tau_i$ and the purchase method which with some 
abuse of notation I denote $m_{il}$. I assume an additive separable form for $\mu_{ilm}$:

$$
\mu_{ilm} = X_l \beta + \mathbb{I}(\tau_i = FP) \mathbb{I}(m_{il} = P)c
$$

$X_l$ is a row vector of a constant and listing characteristics: game quality, row quality, 
section quality, a dummy for low seller feedback score, and advertising activities by 
the seller; $\beta$ is a column vector of coefficients which are to be estimated. The first 
indicator is one if the seller is an FP lover and zero otherwise; the second one is one 
if a posted price purchase is made and zero otherwise.

It seems likely that more bidders arrive for more popular games. In order to
account for this I allow \( \alpha^g \) to depend on game quality. More specifically, I estimate two parameters, \( \alpha_0 \) and \( \alpha_1 \), and assume that \( \alpha^g \) follows the functional form below:

\[
\alpha^g = \frac{\exp(\alpha_0 + \text{gamequality}_g \alpha_1)}{1 + \exp(\alpha_0 + \text{gamequality}_g \alpha_1)}
\]

This specific function has the advantage of restricting the resulting arrival probability to be between zero and one while requiring the estimation of only two parameters.

I use a maximum likelihood approach to uncover the parameters \( \beta, \lambda, c, \alpha_0 \) and \( \alpha_1 \). Given \( N \) the likelihood function depends on information of sale prices, number of bidders, and BIN choices. In FP listings, I only observe whether the item has been sold or not. The probability of the latter is:

\[
P_{l,FP}^{NS} = \sum_{\kappa_{rl}=0}^{N} \sum_{\kappa_{FP}=0}^{N_{FP}} \prod_{\tau \in \{N,FP\}} \eta_{rl}(\kappa_{rl}) [F_{rlP}(p_l)]^{\kappa_{rl}}
\]

(2.11)

As before, \( \eta_{rl}(\kappa_{rl}) \) which is defined in equation (2.7) is the probability to have \( \kappa_{rl} \) entrants of type \( \tau \). \( [F_{rlP}(p_{rl})]^{\kappa_{rl}} \) is the probability that all entrants of type \( \tau \) have a valuation below the price for good \( l \). I multiply over types and sum over the number of potential entrants, so that the right-hand side of (2.11) gives me the probability that all buyers have a value below the posted price. The probability of a fixed price item being sold is now easy to find:

\[
P_{l,FP}^{l,FP} = 1 - P_{l,NS}^{l,FP}
\]

(2.12)

For auction listings, the probability that the item is not sold looks just like for FP listings, except that the fixed price \( p_l \) is replaced with the reserve price \( r_l \):
In the case of the item being sold the likelihood looks different, because in this case
the revenue of the auction is informative. Note that in auctions both types of bidders
have the same distribution of valuations; hence, I drop the type subscript to simplify
notation. Analogously to equation (2.7) I define \( \eta_l(\kappa_l) \) as the probability to have
exactly \( \kappa_l \) entrants:

\[
\eta_l(\kappa_l) = \sum_{\kappa_{FP}=0}^{\kappa_l} \left( \begin{array}{c}
\kappa_{FP} \\
\kappa_l
\end{array} \right) \left( \alpha q_{FP} \right)^{\kappa_{FP}} \left( 1 - \alpha q_{FP} \right)^{N_{FP} - \kappa_{FP}} \left( \begin{array}{c}
N_N \\
\kappa_{FP}
\end{array} \right) \left( \alpha q_{NI} \right)^{\kappa_l - \kappa_{FP}} \left( 1 - \alpha q_{NI} \right)^{N_N - (\kappa_l - \kappa_{FP})}
\]

This expression uses the fact that the \( \kappa_l \) entrants can consist of different shares of the
two bidder types. That is, there can be many FP lovers which then in turn means
few neutrals, or vice versa.

The probability of selling at the reserve price can now be written as:

\[
P_{S}^{l,A}(r_l) = \sum_{\kappa_l=1}^{N} \kappa_l \eta_l(\kappa_l) [F_l(r_l)]^{\kappa_l-1} (1 - F_l(r_l))
\]

As before, \( \eta_l(\kappa_l) \) is the probability that exactly \( \kappa_l \) buyers enter listing \( l \). \([F_l(r_l)]^{\kappa_l-1}\)
is the probability that \( \kappa_l - 1 \) entrants have valuations below the reserve price and
therefore decide not to bid. \((1 - F_l(r_l))\) is the probability that one entrant has a
valuation above the reserve price and submits a bid reflecting this.

If the item was sold for a price above the reserve price we have even more infor-
mation. I assume that all bidders use proxy bidding. I also ignore the minimum bid
increment, which tends to be small for the listings in my dataset. Together, these two assumptions imply that the second highest bid is equal to the second highest valuation, a fact that can be used to uncover the distribution of valuations. In order to be able to identify $\alpha^g$ I also take the number of observed bidders into account. I denote by $W^l_n(\kappa_l)$ the probability of observing $n$ bids given $\kappa_l$ entrants. $W^l_n(\kappa_l)$ is somewhat tricky to calculate because each entrant’s probability of bidding depends on previous bids. Since in this context ordering matters, the number of cases that need to be considered quickly becomes overwhelming. In order to tackle this problem I therefore resort to a simulation method.

Note that the probability distribution over the number of observed bidders depends on several factors: the number of entrants, the distribution of valuations, and the reserve price. I therefore simulate auctions on a grid over those parameters. For every simulated auction I make sure to note the order of arrival of bidders, so that I can count the number of bids submitted. After sufficiently many repetitions I thus create a probability distribution over the number of bidders. I choose to simulate 1,000,000 auctions per grid point; this ensures that I get highly accurate results.

In order to calculate the probability of selling for a price above the reserve, let $b_{l_2}$ denote the second highest bid in the auction. Remember that the second highest bid is equal to the second highest valuation in this case. Then the probability for selling at $b_{l_2}$ can be written as

$$P^l_A(b_{l_2}) = \sum_{\kappa_l=2}^{N} \eta_l(\kappa_l) \cdot W^l_n(\kappa_l) \cdot n(n - 1) \left[ \frac{F_l(b_{l_2}) - F_l(r_l)}{1 - F_l(r_l)} \right]^{n-2} \frac{1 - F_l(b_{l_2})}{1 - F_l(r_l)} \frac{f_l(b_{l_2})}{1 - F_l(r_l)}$$

(2.15)

As noted above, $\eta_l(\kappa_l)$ is the probability of having $\kappa_l$ entrants, and $W^l_n(\kappa_l)$ is the probability that exactly $n$ bids are submitted given $\kappa_l$. Since I observe the second
highest valuation, \( b_{l,2} \), I know that exactly one bidder has a valuation weakly above \( b_{l,2} \); the probability of this is captured in the term \( \frac{1 - F_l(b_{l,2})}{1 - F_l(r_l)} \). Note that I already took into account the fact that this person submitted a bit which implies that his valuation is above the reserve price. I condition on this fact to calculate the necessary probability. I also know that one bidder has a valuation exactly equal to \( b_{l,2} \); the probability of this is \( \frac{1}{1 - F_l(r_l)} \). And finally, all the other bidders have valuations below \( b_{l,2} \) but above \( r_l \) since otherwise they would not have submitted bids in the first place. The probability for this is \( \left( \frac{F_l(b_{l,2}) - F_l(r_l)}{1 - F_l(r_l)} \right)^{n-2} \).

In BIN auctions there are three possibilities how the item can sell. It can be sold for the BIN price, for the reserve price, or for any price above the reserve price in an auction. A BIN sale occurs if the first entrant has a value above the relevant cutoff. The probability of a BIN sale can therefore expressed as follows:

\[
P_{l,BIN} = \sum_{\kappa_{\tau l}} \sum_{\kappa_{FPl}} \rho_{NI}(\kappa_{NI})\rho_{FPPl}(\kappa_{FPPl}) \left[ \frac{\kappa_{NI}}{\kappa_{NI} + \kappa_{FPPl}} \frac{1 - F_{NI}(\tilde{v}_{NI})}{1 - F_{NI}(r_l)} + \frac{\kappa_{FPPl}}{\kappa_{NI} + \kappa_{FPPl}} \frac{1 - F_{FPPl}(\tilde{v}_{FPPl})}{1 - F_{NI}(\min(r_l, p_l - c))} \right]
\]

\( \rho_{\tau l}(\kappa_{\tau l}) \) is the probability of observing exactly \( \kappa_{\tau l} \) bidders who are willing to buy the item and is defined in (2.9). \( \frac{\kappa_{NI}}{\kappa_{NI} + \kappa_{FPPl}} \) is the probability that the first entrant is neutral given the \( \kappa_{\tau l} \), and \( \frac{1 - F_{NI}(\tilde{v}_{NI})}{1 - F_{NI}(r_l)} \) the probability that he prefers a BIN purchase to starting the auction. The second line of (2.16) gives the corresponding expressions for FP lovers.

If instead the auction is started, a reserve price sale occurs only if no bidder
besides the first entrant has a value above the reserve price:

\[ P_{A,\text{BIN}}^l(r_l) = \sum_{\kappa_N=0}^{N_N} \sum_{\kappa_{FP}=1}^{N_{FP}} \rho_{NI}(\kappa_{NI}) \rho_{FP}(\kappa_{FP}) \left[ \frac{\kappa_{NI}}{\kappa_{NI} + \kappa_{FP}} \right] \frac{F_{NI}(\bar{v}_{NI}) - F_{NI}(r_l)}{1 - F_{NI}(r_l)} \right] \left( \kappa_{NI} = 1 \right) F_{FP}(r_l) \left( v_{FP} \geq \min(r_l, p_l - c) \right)^{\kappa_{FP}} \\
+ \frac{\kappa_{FP}}{\kappa_{NI} + \kappa_{FP}} \frac{F_{FP}(\bar{v}_{FP}) - F_{NI}(\min(r_l, p_l - c))}{1 - F_{NI}(\min(r_l, p_l - c))} \right] \left( \kappa_{NI} = 0 \right) F_{FP}(r_l) \left( v_{FP} \geq \min(r_l, p_l - c) \right)^{\kappa_{FP} - 1} \right] \]

The first bidder starts the auction if his valuation is below the cutoff value for type \( \tau, \bar{v}_{\tau l} \). Following my assumption about bidding behavior he submits a proxy bid. Thus, the high bid at this point is equal to the reserve price. If any other bidder has a valuation above the reserve price he submits a bid himself. In this case, the item will necessarily be sold for a price above the reserve. This means that reserve price sales can only occur if only one bidder, the first bidder, has a valuation above \( r_l \).

The probability to achieve a revenue of \( b_{l2} > r_l \) can be calculated as follows:

\[ P_{A,\text{BIN}}^l(b_{l2}) = \sum_{\kappa_N=0}^{N_N} \sum_{\kappa_{FP}=1}^{N_{FP}} \rho_{NI}(\kappa_{NI}) \rho_{FP}(\kappa_{FP}) \left[ \frac{\kappa_{NI}}{\kappa_{NI} + \kappa_{FP}} \right] \frac{F_{NI}(\bar{v}_{NI}) - F_{NI}(r_l)}{1 - F_{NI}(r_l)} \left( \kappa_{NI} = 1 \right) F_{FP}(r_l) \left( v_{FP} \geq \min(r_l, p_l - c) \right)^{\kappa_{FP} - 1} \right] h_l(b_{l2} | \kappa_{NI}, \kappa_{FP}, A_N) dx + \frac{\kappa_{FP}}{\kappa_{NI} + \kappa_{FP}} \frac{F_{FP}(\bar{v}_{FP}) - F_{NI}(\min(r_l, p_l - c))}{1 - F_{NI}(\min(r_l, p_l - c))} \left( \kappa_{NI} = 0 \right) F_{FP}(r_l) \left( v_{FP} \geq \min(r_l, p_l - c) \right)^{\kappa_{FP} - 1} \right] \]
Recall from above that \( h_l(b_l, \kappa_{NL}, \kappa_{FP}, \tau) \) is the distribution of the second highest valuation given the number of entrants of both types and the fact that a bidder of type \( \tau \) started the auction.

Finally, the probability that an item in a BIN auction is not sold is equal to the probability that no entrant wants to buy the item for the specified prices:

\[
P_{NS}^{l,BIN} = \rho_{NL}(0) \rho_{FP}(0)
\]  

(2.19)

To calculate the likelihood out of (2.11)- (2.19) let \( D_{FP}^l \) be the indicator function for fixed price listings, \( D_{A}^l \) an indicator for auctions, \( D_{pS}^l \) an indicator for a fixed price or BIN sale and \( D_{aS}^l \) an indicator for an auction sale. Then the likelihood function is

\[
L = \prod_{t=1}^{T} \prod_{g=1}^{G} \prod_{l=1}^{l^g} \left\{ \left[ D_{FP}^l \left( P_{FP}^{l} \right)^{1-D_{pS}^l} \right] \left[ D_{A}^l \left( P_{A}^{l} \right)^{1-D_{aS}^l} \right] \left[ D_{pS}^l \left( P_{pS}^{l} \right)^{1-D_{pS}^l-D_{aS}^l} \right] \right\}
\]

(2.20)

where \( \tilde{p}_l \) is the revenue of listing \( l \). That is, I calculate the likelihood as follows: For each listings, observe whether and how it was sold. Then apply the appropriate expression from (2.11)- (2.19) and multiply across all listings.

Note that this likelihood function is an approximation since it does not take the interdependence of listings into account. In reality the number of entrants into one period’s listings follows a multivariate hypergeometric distribution (drawing without replacement); in (2.11) - (2.19) I use a binomial distribution (drawing with replacement). In other words, according to my model bidders who enter one listing cannot enter another listing as well. Contrary to that, when calculating the likeli-
hood I pretend that the entry decision into each listing is independent from other entry decisions. I do this because this way of calculating the likelihood is much less computationally intensive than using the exact function with the hypergeometric distribution. While not completely accurate, the binomial distribution is a reasonable approximation for the hypergeometric distribution as long as the arrival probability $\alpha$ is small enough. Given that, as discussed before, I use $N = 200$ and I observe many periods with few bids it seems safe to assume this condition satisfied. Estimation results with different $N$ support this view; if the binomial approximation would pose a major problem then estimations with larger $N$ should provide very different results. However, the parameter estimates barely change when I vary $N$.

**Identification**

In this subsection I provide some intuition for identification. While not a formal proof this will show the reasoning behind my estimation technique. First, given $\alpha^g$ the distribution of valuations would be identified by the distribution of bids as shown by Athey and Haile (2002). In order to see whether identification with unknown $\alpha^g$ is possible, consider the following: A large $\alpha^g$ means more entrants on average and therefore higher expected revenue. The contrapositive is also true, i.e. a small value of $\alpha^g$ is associated with lower revenue. I will now argue that large $\alpha^g$ and large $\beta$ can be distinguished.

It is immediately clear that only the coefficient on the constant could have the same effect as $\alpha^g$, since the other coefficients never have an impact on all listings while $\alpha^g$ does. However, an increase in $\alpha^g$ always means an increase in the expected number of bids; an increase in $\beta$ leaves the expected number of bids virtually untouched unless the reserve price is high. This is because once the reserve price has been exceeded the number of bids depends on the timing of bidders’ bids and the order of their
valuations; these parameters are not affected by a constant shift of valuations. Thus, a change in $\alpha^g$ cannot be mistaken for a change in $\beta$.

By a similar argument I will now show that changes in $\alpha^g$ and $\sigma$ can be clearly distinguished. A larger $\alpha^g$ always means that on average more bids are submitted; thus, the sale probability increases unambiguously. However, intuitively an increase in $\sigma$ only leads to an increased sale probability if $r_l > \mu_l$ while the sale probability and expected number of bids decreases if $r_l < \mu_l$. This is because in the former case submission of a bid requires the valuation to be (potentially far) above $\mu_l$, while in the latter case a bid is submitted unless the valuation is sufficiently far below $\mu_l$. The larger $\sigma$, the greater is the probability of both these cases since on average valuations are going to be further from the mean.

Finally, imagine that $\sigma$ and the coefficient on the constant in $\mu_l$ both increase. This is similar to an increase in $\alpha^g$ in that all sales probabilities increase. However, again the argument from above is valid: The change in $\alpha^g$ affects listings differently depending on their entry probability. The change in $\mu_l$ and $\sigma$ depends on the reserve price; thus the two lead to different bidding behavior in some listings.

2.6.2 Supply Side

On the supply side I need to uncover the outside options as well as the distribution of mechanisms costs and sellers’ risk attitudes. First, I assume there are several types of sellers with respect to their risk attitudes. Particularly, I consider risk-neutrality ($w(x) = x$), and constant absolute risk aversion ($w(x) = 1 - \exp(-\xi x)$) with $\xi = 0.01$ and with $\xi = 0.1$. These parameter choices represent a low and a high degree of risk aversion, respectively.\footnote{For instance, for a lottery that awards $10 and $50 with probability of 0.5 each, the certainty equivalent is 28.01 if $\xi = 0.01$ and 16.75 if $\xi = 0.1$.} Given the risk attitudes I can now back out the opportunity costs of selling. Recall from the previous section that the seller finds the optimal
price from the first-order conditions of the expected revenue maximization (equations (2.7), (2.8) and (2.10)). I invert this process: I observe prices and reserve prices and plug them into the first-order conditions. Now I can solve for the precise values of $v_l^0$. For FP listings and auctions this is straightforward. For BIN auctions I actually have two first-order conditions which in general give me different $v_l^0$. I uncover three sets of outside options: one out of each first-order condition and one using both first-order conditions and allowing for an additional variable which captures a seller’s preference over selling at a posted price. The values uncovered from the reserve price seem slightly more sensible than the ones from the other two methods. Therefore I decide to use opportunity costs of sale backed out of the first-order condition with respect to $r_l$.

Having pinned down $v_l^0$ I can calculate the expected revenue for each item, mechanism and risk attitude. This puts me in a position to turn my attention to mechanism costs $\omega_{lm}$ and types of risk attitudes. These are in general estimable from the observed mechanism choice. However, the magnitude of $\omega_{lm}$ is not identified. This is because I do not observe sellers’ decision whether or not to list on eBay. Instead, I do observe the choice of mechanisms for those sellers who do list on eBay. This identifies the difference in costs between mechanisms. Therefore I define $\gamma_{lA} = \omega_{lA} - \omega_{lFP}$, $\gamma_{lBIN} = \omega_{lBIN} - \omega_{lFP}$ and $\gamma_{lFP} = 0$ and estimate the distribution of the difference of mechanism costs. I assume that $\gamma_{lm} (m = A, BIN)$ is distributed normally with mean $\mu_m^\gamma$ and standard deviation $\sigma_m^\gamma$. This allows me to estimate the distribution of mechanism costs in a multivariate probit estimation. In the same process I also estimate the distribution of risk attitude types. Since I can calculate expected revenues for each utility function I can find which parameterization best explains the observed mechanism choice. When sellers choose mechanisms they of course know their own utility function and can therefore pick the correct expected utility. As the
econometrician, on the other hand, I do not have this luxury. Instead, I estimate the shares of sellers of each risk type. Then I weight the three different expected utilities by the probability that a seller is of the respective type. That is, I integrate out sellers’ unobserved risk preferences and determine the choice probabilities based on this weighted utility.

Seller $l$ chooses mechanism $m_l$ if it gives her a higher utility than selling at either of the other two mechanisms, $m'_l$ and $m''_l$. The probability of this is:

$$P_l(m_l) = P \left[ (EW_{lm}(p_l, r_l) - w_l(\gamma_{lm}) > EW_{lm'}(p'_l, r'_l) - w_l(\gamma_{lm'}) ) \right]$$

$$\wedge (EW_{lm}(p_l, r_l) - w_l(\gamma_{lm}) > EW_{lm''}(p''_l, r''_l) - w_l(\gamma_{lm''})) \right]$$

The two probabilities, $P \left( EW_{lm}(p_l, r_l) - w_l(\gamma_{lm}) > EW_{lm'}(p'_l, r'_l) - w_l(\gamma_{lm'}) \right)$ and $P \left( EW_{lm}(p_l, r_l) - w_l(\gamma_{lm}) > EW_{lm''}(p''_l, r''_l) - w_l(\gamma_{lm''}) \right)$, are clearly not independent since $\gamma_{lm}$ influences both events. Thus, the estimation does not follow a standard probit procedure; instead I use the multivariate probit.

2.7 Results

2.7.1 Demand Side

It is likely that the conditions on both the demand side and the supply side change over time. Therefore, I perform the demand side estimation on three different time intervals: less than 10 days before the game, 11-20 days before the game and 21-40 days before the game. I provide the parameter estimates for each interval in table B.4. All parameters have the expected sign. Valuations increase in the quality indices and advertising. The willingness to pay is lower when the seller has a low reputation score. The expected valuation for an average pair of tickets is 71.16 dollars less than...
10 days before the game, 58.29 dollars 11-20 days before the game, and 55.97 dollars 21-40 days before the game.\textsuperscript{22}

A fair number of buyers has a significant preference for buying at posted prices. The share of FP lovers, $\lambda$, ranges from 0.26 to more than 0.32. The intensity of the FP preference, $c$, comes out at values above 20 dollars.

The arrival probability increases drastically over time. In early listings the arrival probability for a game of average interest is estimated to be 0.0178, while close to the game it is 0.0732. This means that the expected number of bidders in the market place increases from 3.6 to 14.6.

In order to test the accuracy of my model I calculate expected revenues and sale probabilities based on the estimates from the demand section. Table B.6 reports these values and compares with their actual counterparts. Overall I get a good fit. Recall that I estimate the model by maximum likelihood, not by a method of moments; thus, the moments do not necessarily have to match.

\subsection*{2.7.2 Supply Side}

I divide sellers into two types, small and large; large sellers are sellers who list more than 200 pairs of baseball tickets during the year. Note that this includes listings for other teams’ home games. My rationale is that large sellers might be more experienced in price setting and therefore have different mechanism costs and risk preferences. In fact it seems likely that these large sellers are professionals and small firms who specialize on eBay sales. About 7.5\% of sellers are classified as large. These sellers account for more than 40\% of listings. In table B.7 I report the mechanism choice by seller type. Large sellers are much more likely to choose FP listings or

\textsuperscript{22} To obtain these numbers I calculate the expected valuation of a ticket assuming game quality = row quality = section quality = 0.5, and further assuming that no advertising was chosen and that the dummy for low seller score was 0. That is, I calculate $\beta_1 + \frac{1}{2}(\beta_2 + \beta_3 + \beta_4)$. 

55
BIN auctions, while almost two thirds of listings by small sellers are auctions. This is consistent with the aforementioned thoughts about experience, since it might be easier to set reserve prices, which do not completely determine revenue, than fixed prices.

I estimate the supply side separately for each type. Figure B.5 shows the estimated opportunity costs of selling for both types of sellers. Two phenomena are immediately obvious: First, large sellers have slightly higher opportunity costs on average. Second, there is a relatively large number of negative values. Two arguments can explain why I find more valuable outside options for large sellers. Small sellers are less experienced and therefore might underprice; and large sellers might face smaller costs of relisting as they often sell tickets semi-professionally or professionally. Small sellers on the other hand might be tempted to avoid the hustle of having to list the tickets again.

For baseball tickets, free disposal is certainly a good description of reality. Therefore it seems odd to find a large number of sellers with negative opportunity costs. There are several reasons why a seller’s outside option might come out negative. First, the face value might serve as a focal point. Some states have laws against the sale of tickets for more than the face value. While this is not the case in Ohio, such a law does exist in neighboring Kentucky. Even if no law exists, some sellers might have moral qualms against selling the ticket for a profit. Indeed, I find that start prices have a mass point at the level of the respective face value. Second, tickets are generally checked at the stadium and possibly section entrance but not at the individual seat. Thus, as long as the stadium is not sold out ticket holders can move to better places. Realizing this sellers might charge a low price even for good seats; otherwise buyers can simply buy a cheap ticket and move to a better place. My model does not control for this, so that it would overestimate buyers’ willingness to
pay. Finally, sellers make mistakes. The fact that negative $v^0$ are more prevalent with small sellers might indicate that this can at least partially explain the results.

Figures B.6 and B.7 help with further analysis of the outside options. For large sellers there is a clear distinction: They select FP listings or BIN auctions if they have a valuable outside option and an auction if they have a poor one. As mentioned above this is reasonable. Sellers with less valuable outside options will feel a higher urgency of selling their tickets. Therefore they tend to choose auctions, which provide the highest sale probability among the available mechanisms. For small sellers, on the other hand, the three distributions of opportunity costs look almost perfectly alike. Again I attribute this difference to small sellers’ lack of experience.

Finally, table B.9 shows how the mean outside options decrease as the game approaches. This effect is not strong; however, it fits the idea that fewer possibilities for relisting lead to lower opportunity costs of sale. Recall from above that large sellers tend to choose auctions if the value of their outside option is low and FP listings or BIN auctions otherwise. Thus, the decreasing opportunity costs are one explanation why FP listings are less favored close to the game. An alternative explanation for decreasing opportunity costs is that particularly valuable tickets are offered early. However, my data does not support this argument. In fact, table B.10 shows that the mean quality of tickets stays almost perfectly constant over time.

The results from the probit estimation are provided in tables B.8 and B.11. Large sellers are virtually indifferent between mechanisms; they choose almost exclusively based on their revenue expectations and risk preferences. Small sellers also don’t show significant preferences over mechanisms. However, they do seem to somewhat prefer auctions over FP listings and FP listings over BIN auctions. I also note that the variance of sellers’ mechanism costs is very small. This is comforting as it implies that sellers’ utility can explain most mechanism choices. Thus I conclude
that sellers’ risk attitudes as well as their outside options are important determinants of mechanism choice.

Large sellers on average are also less risk averse than their smaller counterparts. Almost two thirds of large sellers are risk neutral; for small sellers this share is close to one third and the largest group is that of strongly risk averse agents which comprises of almost 40% of small sellers. It is intuitive that large sellers show less signs of risk aversion. They list on average more than 1200 sets of tickets over the course of the baseball season. Thus, the risk associated with an individual listing almost completely cancels out.

2.8 Counterfactual: Welfare Effect of BIN Auctions

In this section I discuss how the existence of BIN auctions affects consumer and producer surplus. I use the estimates describing buyer and seller behavior from the previous section and calculate the expected utility for buyers, the utility from net revenue for sellers, and the revenue from fees for eBay.

Then I consider the market without BIN auctions. I can calculate the expected seller utility for each mechanism and alter mechanism choice of sellers who originally chose BIN auctions. I simulate sellers’ new mechanism choice; that is, given their expected utilities from each mechanism and the distribution of mechanism costs I determine the probability that a given seller chooses mechanism $m$. Then I simulate the new mechanism 500 times. In each simulation of the altered market, I again calculate the expected utility for buyers and sellers as well as eBay’s expected fee income.

Recall from table B.1 that in the actual market about 50% of listings are auctions, about 12% are FP listings, and close to 38% are BIN auctions. Under the counterfactual market structure obviously the share of BIN auctions goes to zero.
These listings are split among auction and FP listings roughly in a ratio of 1:2. This results in new mechanism shares of approximately 61.3% for auctions and 38.7% for FP listings. Thus, the new market makes it easy for FP lovers to find their desired sale method while providing the efficiency of auctions in most listings.

I find that buyers benefit from BIN auctions: Their surplus goes up by 0.55% for FP lovers and by 5.78% for neutrals. Sellers on the other hand are better off in a market which offers only FP listings and auctions. The BIN auction reduces their utilities by 11.91% for small sellers and 15.84% for large sellers. eBay’s fees largely depend on sellers’ revenues. Therefore it is not surprising that eBay also would benefit from abandoning the BIN auction. Its fee revenue would go up by 10.63%. Note however that this analysis does not consider the effect of competition with other sales platforms. It is possible that buyers, understanding how BIN auctions increase their welfare, would switch to other sales platforms if eBay did abandon BIN auctions. Thus, the competitive pressure might force eBay to allow for BIN auctions.

In the counterfactual market structure, sellers can split the market. Some sellers offer FP listings, catering to buyers who prefer posted prices. Others offer auctions; auctions are attractive for selling to neutral buyers because they are more efficient than FP listings. In equilibrium, sellers in both mechanisms earn the same amount. Thus, neither type of seller has an incentive to deviate; instead both can use features of their mechanism to earn a relatively high revenue: Sellers offering FP listings benefit from FP lovers’ higher willingness to pay. Sellers offering auctions have the chance of selling for a high price if multiple high-value bidders enter.

In contrast, in the original market structure with BIN auctions, this market splitting does not constitute equilibrium behavior. Auction sellers now have an incentive to deviate. They can use the BIN price to attract FP lovers in addition to
neutral bidders. Similarly, FP sellers might wish to offer an auction option; again, this makes it more likely that buyers of both types enter and therefore increases revenue expectations. That is, the existence of BIN auctions increases competition between sellers as BIN auctions attract both types of buyers. Thus, sellers find themselves in a Prisoner’s Dilemma situation. Offering BIN auctions is individually rational. However, in equilibrium it hurts sellers since it takes away the possibility of differentiation by mechanism choice.

This result is consistent with several papers in the marketing literature. They show that bundling, which is revenue maximizing at an individual level, reduces revenues in competitive markets. The underlying reason for this is that bundling makes the items offered by different sellers more similar by averaging out inherent product specific differences.

2.9 Conclusion

I examine competition in markets which feature multiple sales mechanisms. On the demand side I model buyers’ listing choice as equilibrium decisions. That is, each buyer takes expected entry decisions of other buyers into account. On the supply side I analyze sellers’ mechanism choice. I find that sellers with valuable outside options are more likely to choose FP listings and BIN auctions; those with poor outside options prefer auctions. I also estimate risk attitudes of sellers and find that small sellers show significant levels of risk aversion while most large sellers are risk neutral. Taken together risk preferences and outside options explain sellers’ mechanism choice well.

Based on my results I examine the welfare effects of BIN auction. I find that buyers benefit from the existence of BIN auctions while sellers and eBay itself would prefer a world without the hybrid mechanism. This conforms to the intuition dis-
cussed in detail in the previous section. Sellers can use mechanism choice as a means of product differentiation. This breaks down when BIN auctions are available, because as a hybrid mechanism BIN auctions attract buyers of both types. Thus, their existence strengthens competition.
3

Incidence of Taxes on Retail Soft Drinks:
Theory & Evidence from Scanner Data

3.1 Introduction

With obesity and diabetes numbers on the rise, soft drinks have recently become more and more the focus of health politics. The US senate, the District of Columbia, and twelve states have drafted, and in some cases passed, a variety of sugar tax proposals meant to decrease Americans’ consumption of sugary soda. However, it is not clear how effective such measures can be. For instance, if the tax is not high enough then consumers might not react strongly to it. In addition calories saved from soft drinks might be replaced by other unhealthy dietary choices. In this paper we are looking at a third problem: It is not clear yet how much of a soda tax would be passed through to consumers and how much would be borne by producers and
This question is relevant because a low pass-through would mean that consumer choices and therefore consumer behavior don’t change very much. Thus, they would require different ways of influencing the national health.

We find that generally speaking pass-through levels highly depend on market specifics and that in certain situations the whole tax is passed through while in other situations virtually no tax is passed through. In still other situations a small portion of the tax is passed on to consumers. The goal of this paper is to identify the factors that determine the level of pass-through. This would allow us to make more accurate predictions on how sales taxes influence consumer behavior.

The rest of the paper will proceed as follows. The next section provides a detailed description of the datasets used along with relevant summary statistics and institutional details. In section 3, we present our empirical findings along with theoretical models and their predictions. In section 4 we conclude.

3.2 Data

In this paper, we use make use of three sets of data. The primary data set is a weekly scanner data provided by Information Resources Inc. (IRI) from 2001 to 2007. The two auxiliary data sets come from ImpacTeen, a policy research partner of Healthier
Youth Group, and the census QuickFacts.

3.2.1 IRI Data

The scanner data provides a panel of weekly retail sales information on all carbonated beverages for each grocery store in the sample. The IRI sample contains over 2,800 stores the across continental United States. For each and every item sold in each week and each store, we observe information on its total revenue collected, total units sold, and any promotional activities. We use measurements on the revenue and units sold to construct a proxy for the unit price.

There are close to 15,000 unique soda items offered across different locations and different time periods. Products differ in their brand, their taste, and the container’s size and shape. IRI provides product identifier information that allow us to know which brand each item is, what flavor each item have, and what kind of container each item is bottled in. Thus, we can narrow products specification for easier and more accurate comparison of prices. For example, in one specification, we choose to concentrate on 2 liter bottled Classic Coke.

For each store, we observe when it starts being included in the data and when it stops being included. Furthermore, for each store we observe the state in which it is located. We use this location information to control for time variation in price changes. That is, for a state that experiences an introduction or removal of a soda
tax, we control for the natural changes in prices by using the pricing information in
a state that has similar demographical characteristics but did not experience such
changes.

3.2.2 ImpacTeen Data

Soda tax laws vary, occasionally with significant changes, over time and over states.
This information is generally obtainable by going through past state tax regulations
as most states keep a record of this information. However, most states do not have
easily accessible tax information. The ImpacTeen program keeps a record of all taxes
related to soft drinks and salty snacks. Here we have available tax rates across all
US states from 2001 to 2007, which covers all years of the store panel data we have
from IRI.

This data set shows, for each of the seven years, what the general sales tax of
each state is; whether that state has any tax on food products; if the state has a
general food tax, what is its tax rate; whether that state taxes soft drinks; and if
soda is being taxed, then what its rate is. Out of the 50 states and the district of
Colombia, 37 states have experienced a soda tax at least in one of the years. Out
of these 37 states, 22 have a "disadvantaged" soda tax. That is, in these 22 states,
soda is taxed at a higher rate than general food items. For instance, in Ohio, soda
is not listed in the definition of food; hence it is taxed as a non-food item.
Out of all the states that have ever had a soda tax between 2001 and 2007, 15 experienced a change in soda tax rates. Most of these tax changes are between 0.5% and 1%. However, there are seven states that have had a change in soda tax of at least 2%. Table 3.1 lists these states and their tax change information.

Table 3.1: Significant Soda Tax by State

<table>
<thead>
<tr>
<th>State</th>
<th>Tax Rate Before (%)</th>
<th>Tax Rate After (%)</th>
<th>Year Instituted</th>
</tr>
</thead>
<tbody>
<tr>
<td>DC</td>
<td>5.75</td>
<td>0</td>
<td>2002</td>
</tr>
<tr>
<td>North Carolina</td>
<td>4.00</td>
<td>0</td>
<td>2002</td>
</tr>
<tr>
<td>North Carolina</td>
<td>0</td>
<td>4.5</td>
<td>2004</td>
</tr>
<tr>
<td>New Mexico</td>
<td>5.00</td>
<td>0</td>
<td>2005</td>
</tr>
<tr>
<td>Ohio</td>
<td>0</td>
<td>5.00</td>
<td>2003</td>
</tr>
<tr>
<td>South Carolina</td>
<td>5.00</td>
<td>3.00</td>
<td>2007</td>
</tr>
<tr>
<td>Utah</td>
<td>4.75</td>
<td>2.75</td>
<td>2007</td>
</tr>
<tr>
<td>Wyoming</td>
<td>4.00</td>
<td>0</td>
<td>2007</td>
</tr>
</tbody>
</table>

In this paper, we make use of three of these state tax changes: changes in the DC soda tax from 2001 to 2002, changes in the North Carolina soda tax from 2003 to 2004, and changes in the Ohio soda tax from 2002 to 2003.

3.2.3 Census Data

The last set of data we use is the Census QuickFact data. We use this data to ensure that any two states that are being compared against each other have similar demographical characteristics. Since we use states that do no experience soda tax changes as a control for natural price changes over the years, it is important that these ”control” states are not too different from the ”experiment” states.
3.3 Empirical Analysis

We focus on the determinants of the pass-through level of soda taxes. Currently, we conduct two sets of analyses. In the first set, we study how the size of the stores influences the level of pass through, where the size of a store is represented by its capacity. We set up a basic model of firm behavior with differing capacity constraints and compare the results predicted by this simple theory model to the empirical pass-through seen in the data. In the second set of analysis, we examine how the location of a supermarket influences its pass-through level. We again set up a theoretical model of firm behavior with consumers of differing travel cost and compare the results predicted by this model to empirical results seen in the data. In all empirical analyses, we employ the differences-in-differences method to control for any possible time trends. Each of these analyses are described in detail in the follow sections.

3.3.1 Large vs. Small Stores

We set up a simple model with of monopolistic firms facing a capacity constraint. The capacity constraint is used to represent firms of different sizes. For large, big-box supermarkets the constraint does not bind; while the smaller, more local, stores are assumed to be capacity constrained. Each is assumed to be a monopolist in its
market. This capacity can be thought of as the available inventory space of the store.

Here, we use the most fundamental demand function and derive pass-through level by profit maximization. While this model is far too simplistic for the complex reality of the US supermarket industry, it does shed some light on the pass-through and its determinants.

Assume we have a monopolist with constant marginal cost $c$ and capacity $k$. Furthermore, the monopolist faces demand: $q = \frac{a-p}{b}$. Or, $p = a - b \cdot q$. The goal of the monopolist, as always, is to maximize its profit. Its objective function is:

$$\max_q \pi = (a - bq - c) q$$

Recall that in this setting, maximizing with respect to quantity is equivalent to maximizing with respect to price. Following standard procedures, we obtain the first order condition, $a - 2bq - c = 0$. Solving the first order condition for quantity, we obtain the standard result:

$$q = \frac{a - c}{2b}$$

Hence, the optimal quantities and prices, depending on capacity constraint, can be
written as:

\[ q^* = \begin{cases} 
  k & \text{if } k < \frac{a-c}{2b} \\
  \frac{a-c}{2b} & \text{otherwise}
\end{cases} \quad \text{and} \quad p^* = \begin{cases} 
  a - bk & \text{if } k < \frac{a-c}{2b} \\
  \frac{a+c}{2} & \text{otherwise}
\end{cases} \]

Now assume an ad valorem tax, \( t \), is introduced. The demand becomes \( q = \frac{a - p(1+t)}{b} \). Or, \( p = \frac{a-bq}{(1+t)} \). The new optimal quantities and prices are:

\[ q^*_{\text{tax}} = \begin{cases} 
  k & \text{if } k < \frac{a-(1+t)c}{2b} \\
  \frac{a-(1+t)c}{2b} & \text{otherwise}
\end{cases} \quad \text{and} \quad p^*_{\text{tax}} = \begin{cases} 
  \frac{a-bk}{1+t} & \text{if } k < \frac{a-(1+t)c}{2b} \\
  \frac{a+(1+t)c}{2(1+t)} & \text{otherwise}
\end{cases} \]

To determine the pass through level, we simply compare the optimal prices before and after tax for each of the two types of monopolists. Assume the firm is capacity constrained, that is, \( k < \frac{a-(1+t)c}{2b} \). Then comparing the prices paid by consumers under \( p^*_{\text{tax}} \) with \( p^* \) we see:

\[
(1+t)p^*_{\text{tax}} - p^* = (1+t)\frac{a-bk}{1+t} - (a-bk) = 0
\]

Therefore, under this setting, the capacity constrained supermarket will have a pass-through level of 0%. It will absorb all of incidence of the tax and pass no tax burden onto the consumers. On the other hand, assume the firm is not capacity constrained.
constrained, \( k \geq \frac{a-c}{2b} \). And again comparing the prices paid by consumers under \( p^*_\text{tax} \) with \( p^* \):

\[
(1 + t)p^*_\text{tax} - p^* = (1 + t) \frac{a + (1 + t)c}{2(1 + t)} - \frac{a + c}{2}
\]

\[
= \frac{a + (1 + t)c}{2} - \frac{a + c}{2} = \frac{tc}{2}
\]

\[
> 0
\]

We see the non-capacity constrained firm will not absorb all of the burden of the tax. A portion, \( \frac{c}{2} \), will be passed onto the consumers. While we don’t know the marginal cost, \( c \), it is clear that the price difference is strictly positive.

Finally, consider a medium-sized firm that is capacity constrained without tax but not with tax (i.e. \( \frac{a-(1+t)c}{2b} \leq k < \frac{a-c}{2b} \)). In this case we get:

\[
(1 + t)p^*_\text{tax} - p^* = (1 + t) \frac{a + (1 + t)c}{2(1 + t)} - (a - bk)
\]

\[
= \frac{(1 + t)c - a}{2} + bk
\]

The last expression is greater than or equal to zero since \( k \geq \frac{a-(1+t)c}{2b} \); it is also less than \( \frac{c}{2} \) since \( k < \frac{a-c}{2b} \). Thus, the pass-through for medium-sized stores is between the one for large stores and the one for small stores.
These results are fairly intuitive. A store facing a binding capacity constraint cannot supply the optimal unconstrained quantity. In order to maximize profit it charges a price that allows it to get as close to the unconstrained optimum as possible, i.e. use its whole capacity. Since the capacity does not change when the tax is introduced the stores the store has to bear the whole burden of the tax in order to keep selling its whole capacity.

For large stores in this set up the capacity constraints do not bind. Therefore, all else equal, their profit maximizing quantities sold are larger than those of small stores. After a tax is introduced, the tax acts as an additional marginal cost. The large monopolist reacts to the increased marginal cost by increasing its price and hence passes some of the tax burden onto the consumers.

From this simple model, one point can be clearly shown: The pass-through level does not always and only depend on demand elasticities. We observe that under this fundamental setup, the capacity constrained firm passes zeros percent of the tax onto consumers and the non-capacity constrained firm passes a share $\frac{c}{2}$ of the tax burden on to consumers. The pass through level does not depend on demand parameters, $a$ and $b$, in either case. Hence, it is not always clear that firms’ pass-through decision depends purely on the demand elasticities.

We also find support for the predictions of the model in the data. We use the
North Carolina and South Carolina data from 2003 to 2004. The two states have comparable demographical characteristics. In 2004, North Carolina changed its taxing scheme on soft drinks. In the two years before, soft drinks were not taxed. However, in 2004 the state instituted a 4.5% sales tax on all soda. In comparison, no tax changes were experienced by South Carolina, having a consistent 5% sales tax on all soda.

Since there are no pre-defined size of stores and no information of the square-footage of each supermarket are given, we have to construct measurements for the size of the store. A large store is defined here as a store that sells more than 300,000 liters of soft drinks per year. In this definition, the small stores account for the 25% of the sample. We are also conducting robustness checks on this definition as it is always somewhat arbitrary.

For straight-forward comparison of prices, we use only 2-liter bottles of Coke. Similar results seem to hold for other products. We employ the differences-in-differences technique in obtaining the pass-through estimate. As North Carolina is comparable to South Carolina, this allows us to tease out any time trends in the data. The regression results are presented below. Table 3.2 shows the price change as a reaction to the tax increase (coefficient on time and state interaction) of small stores and table 3.3 shows the pass-through of large stores.
Table 3.2: Small Store Diff-n-Diff Regression Results:

<table>
<thead>
<tr>
<th></th>
<th>coefficient</th>
<th>standard error</th>
<th>t-statistic</th>
<th>P-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>constant term</td>
<td>$1.24</td>
<td>0.0113</td>
<td>110.42</td>
<td>0.000</td>
</tr>
<tr>
<td>state dummy</td>
<td>$0.07</td>
<td>0.0154</td>
<td>4.62</td>
<td>0.000</td>
</tr>
<tr>
<td>time dummy</td>
<td>$0.07</td>
<td>0.0159</td>
<td>4.56</td>
<td>0.000</td>
</tr>
<tr>
<td>state-time interaction</td>
<td>-$0.07</td>
<td>0.0346</td>
<td>-2.00</td>
<td>0.047</td>
</tr>
</tbody>
</table>

Table 3.3: Large Store Diff-n-Diff Regression Results:

<table>
<thead>
<tr>
<th></th>
<th>coefficient</th>
<th>standard error</th>
<th>t-statistic</th>
<th>P-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>constant term</td>
<td>$1.17</td>
<td>0.0040</td>
<td>289.12</td>
<td>0.000</td>
</tr>
<tr>
<td>state dummy</td>
<td>$0.01</td>
<td>0.0051</td>
<td>2.03</td>
<td>0.042</td>
</tr>
<tr>
<td>time dummy</td>
<td>$0.73</td>
<td>0.0057</td>
<td>12.98</td>
<td>0.000</td>
</tr>
<tr>
<td>state-time interaction</td>
<td>-$0.01</td>
<td>0.0072</td>
<td>-1.64</td>
<td>0.100</td>
</tr>
</tbody>
</table>

From table 3.2, we see that when a 4.5% sales tax is introduced in North Carolina, the price of soda in small stores decrease by seven cents (a pass-through of -1.33%). This estimate is statistically significant at a 95% confidence level. Note, the average price of this product is $1.24. According to our theory, in order to continue selling its original capacity, small stores would have to reduce its price such that the product costs consumers exactly the same as before the tax. In this case, the average price charge to consumers, before tax, would have to be around $1.18. This means a predicted price decrease of 6 cents. This is, surprisingly, very close to the observed price decrease (1 cent lower) in the data.

From table 3.3, we see that when a 4.5% sales tax is introduced in North Carolina, the price of soda in large stores decreases by one cent (a pass-through of 87.84%). This estimate, however, is not statistically significant at a 95% confidence level.
level. According to our theoretical model, large store will let consumer bear some burden of the tax. However, since we don’t observe their marginal cost, we cannot determine the level of predicted pass-through exactly. From our empirical result, it seems that in large stores, most of the burden of the tax will fall on consumers.

We conclude from this piece that capacity-constrained stores will bear all of the burden of the tax while non-capacity constrained stores will pass through a strictly positive portion of the tax to consumers. This prediction is supported by the data. Moreover, we also show using this simple setup that demand elasticities are not the sole determinant of pass through levels. In the following subsection, we study how the geographical location influences store’s tax pass through level.

3.3.2 Rural vs. Urban Locations

A second possible determinant of tax pass-through levels could be the geographical location of a store. It is conceivable that due to the higher concentration of consumers in more urban locations, supermarkets too are built within closer vicinity of each other. As supermarkets become more concentrated competition then becomes fiercer. In more rural areas, consumers live in more spread out communities. This increases travel cost between stores and lessens competition. Assuming this intuition is correct, we develop a theoretical model with consumer travel cost. As previously, we then
compare the predictions of this model to results found in our empirical analysis.

We now develop a model that allows us to capture differences in density of stores and consumers. Consider a population of consumers with unit demand. The consumers live in a linear Hotelling-type city. There are two retailers and two manufacturers (Coke and Pepsi). Both retailers sell both goods. They compete in a Bertrand-type game, i.e. they compete in prices. Retailer $r$ pays price $p_{br}^m$ for one unit of item $b$. This price is determined by Nash Bargaining between the store and the manufacturer.

Consumers face the decision which of the goods to buy (if any) and at which retailer. They make this decision not only based on prices but also on travel costs: A consumer might buy at a more expensive store if that one is closer. Consumer $i$ chooses his purchase such that he maximizes his utility function:

$$U_{ibr} = \alpha_b - \beta p_{br} + \epsilon_{ibr} - \gamma |l_i - l_r|$$

$\alpha_b$ is a brand fixed effect; $\beta$ is consumers’ marginal utility of income and $p_{br}$ is the price of brand $b$ in store $r$. $\gamma$ is the travel cost, and $l_i$ and $l_r$ respectively are the locations of consumer $i$ and retailer $r$. Finally, $\epsilon_{ibr}$ is an idiosyncratic shock which is distributed normal with mean zero and standard deviation $\sigma$.

Given locations and manufacturer prices, retailer $r$ maximizes his profit with
respect to retail prices $p_{br}$. The profit is given by:

$$\pi_r = \sum_b (p_{br} - c_{br} - p_{br}^m) s_{br} M$$

c_{br} is the marginal cost to retailer $r$ associated with selling an item of brand $b$; we assume constant marginal costs so that $c_{br}$ does not depend on sale quantities. Thus, $(p_{br} - c_{br} - p_{br}^m)$ is the surplus $r$ earns per unit of product $b$. $M$ is the size of the market and $s_{br}$ is the market share of a given retailer-brand combination, so that $s_{br} M$ captures retailer $r$’s total sales of brand $b$.

Producer $b$’s profit is:

$$\pi_b = \sum_r (p_{br}^m - c_b^m) s_{br} M$$

Again, $s_{br} M$ are the total sales of brand $b$ at store $r$. $c_b^m$ is producer $b$’s marginal cost of production; again we assume constant marginal cost, so that $(p_{br}^m - c_b^m)$ is the producer’s surplus per piece.

The producer’s price, $p_{br}^m$, is determined by Nash bargaining between store $r$ and manufacturer $b$. Here we are assuming that each bargaining process is independent from the other ones; i.e. retailers and manufacturers accurately predict their profits if bargaining succeeds as well as if it fails.

This model is extremely hard to solve analytically since there are so many layers
of optimization involved. Therefore we solve the game numerically in order to compare the theoretical predictions with the empirical results discussed below. For our simulations we use a setting with two retailers and the following parameters:

<table>
<thead>
<tr>
<th></th>
<th>Coke</th>
<th>Pepsi</th>
</tr>
</thead>
<tbody>
<tr>
<td>Retailer’s marginal cost</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$c_{b1}$</td>
<td>0.2</td>
<td>0.2</td>
</tr>
<tr>
<td>$c_{b2}$</td>
<td>0.1</td>
<td>0.1</td>
</tr>
<tr>
<td>Manufacturer’s marginal cost</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$c_{m}$</td>
<td>0.3</td>
<td>0.1</td>
</tr>
<tr>
<td>Demand parameters</td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\alpha_b$</td>
<td>2.0</td>
<td>1.7</td>
</tr>
<tr>
<td>$\beta$</td>
<td>0.9</td>
<td></td>
</tr>
<tr>
<td>$\sigma$</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>$\gamma$</td>
<td>0.5</td>
<td></td>
</tr>
<tr>
<td>$M$</td>
<td>1000</td>
<td></td>
</tr>
</tbody>
</table>

Since we want to compare rural and urban settings, we calculate results for city lengths of 1 and 2, respectively. In the former case we assume that the stores are located at $l_1 = 0.25$ and $l_2 = 0.75$, in the latter case we assume $l_1 = 0.5$ and $l_2 = 1.5$. Consumers are in both cases distributed uniformly.

We report our simulation results in table 3.5. The table shows that pass-through levels are higher in rural settings than in urban ones. This is a result that gets confirmed in the data as is shown below.

To compare any tax pass through differences between an urban and a rural loca-
Table 3.5: Simulation Results for Different Cases

<table>
<thead>
<tr>
<th></th>
<th>No Tax</th>
<th>5% Tax</th>
<th>Pass-Through</th>
</tr>
</thead>
<tbody>
<tr>
<td>Urban</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Retail 1 - Coke</td>
<td>$2.59</td>
<td>$2.56</td>
<td>75.68%</td>
</tr>
<tr>
<td>Retail 1 - Pepsi</td>
<td>$2.92</td>
<td>$2.87</td>
<td>64.04%</td>
</tr>
<tr>
<td>Retail 2 - Coke</td>
<td>$2.86</td>
<td>$2.80</td>
<td>55.94%</td>
</tr>
<tr>
<td>Retail 2 - Pepsi</td>
<td>$3.13</td>
<td>$3.08</td>
<td>66.45%</td>
</tr>
<tr>
<td>Rural</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Retail 1 - Coke</td>
<td>$2.33</td>
<td>$2.34</td>
<td>104.51%</td>
</tr>
<tr>
<td>Retail 1 - Pepsi</td>
<td>$2.92</td>
<td>$2.91</td>
<td>92.81%</td>
</tr>
<tr>
<td>Retail 2 - Coke</td>
<td>$2.86</td>
<td>$2.83</td>
<td>77.97%</td>
</tr>
<tr>
<td>Retail 2 - Pepsi</td>
<td>$3.24</td>
<td>$3.22</td>
<td>87.04%</td>
</tr>
</tbody>
</table>

tion, we need not only two such places but also 1) each location experiences significant tax changes and 2) each location has a demographically comparable place that has no tax changes. The first requirement is obvious. The unit prices of soft drinks are small. Therefore, if we observe only minor tax changes, less than 2%, we would not be likely to observe any significant pass through. The second requirement comes from the fact that we use differences-in-differences method to control for any unobservable time-varying trends.

The set of locations that satisfy the first criterion is listed in table 3.1. Out of those seven possible states, we choose DC as the representative of the urban location and North Carolina as the representative of the rural location. DC experienced a dramatic change in soda tax in 2002, when the sales tax on soda went from 5.75% to 0%. In the same period, however, places on the DC-Maryland border experienced no tax changes. All soda in these locations were being taxed at the usual 5%. The
population in these two places are very comparable and thus making DC is good candidate for analysis. The same holds for North Carolina. As the previous subsection points out, after two years of no taxation on soda North Carolina instituted a 4.5% sales tax in 2004. In comparison, no tax changes were experienced by South Carolina, which has had a consistent 5% sales tax on all soda. The two states share comparable demographical attributes.

The following table 3.6 documents diff-n-diff regression results of each of the locations. Similarly to before, to ease the comparison of prices, we use 2-liter Coke products in these regressions.

<table>
<thead>
<tr>
<th>States</th>
<th>coefficient</th>
<th>standard error</th>
<th>t-statistic</th>
<th>P-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>DC:</td>
<td>constant term</td>
<td>$1.26</td>
<td>0.0107</td>
<td>117.62</td>
</tr>
<tr>
<td></td>
<td>state dummy</td>
<td>$0.01</td>
<td>0.0126</td>
<td>0.73</td>
</tr>
<tr>
<td></td>
<td>time dummy</td>
<td>-$0.01</td>
<td>0.0117</td>
<td>-0.58</td>
</tr>
<tr>
<td></td>
<td>state-time interaction</td>
<td>$0.04</td>
<td>0.0143</td>
<td>2.47</td>
</tr>
<tr>
<td>NC:</td>
<td>constant term</td>
<td>$1.18</td>
<td>0.0038</td>
<td>305.86</td>
</tr>
<tr>
<td></td>
<td>state dummy</td>
<td>$0.00</td>
<td>0.0049</td>
<td>0.53</td>
</tr>
<tr>
<td></td>
<td>time dummy</td>
<td>$0.07</td>
<td>0.0054</td>
<td>13.31</td>
</tr>
<tr>
<td></td>
<td>state-time interaction</td>
<td>-$0.01</td>
<td>0.0069</td>
<td>-1.88</td>
</tr>
</tbody>
</table>

As we can see, in DC area, after the 5.75% soda tax is removed, prices increased by four cents. Since this estimate is statistically significant at a 95% confidence level, it shows that there is some indication that the pass through level is not 100% and stores are absorbing some of the burden of the tax. On the other hand, in North
Carolina, after the introduction of a 4.5% soda tax, no significant changes in prices can be found. This implies that consumers bear most of the burden of the tax by paying the original prices in addition to the tax.

This analysis indicates that there is some evidence to suggest the competition in urban areas drive stores to absorb some of the burdens of the tax and hence have lower pass through rates.

3.4 Conclusion

In this paper we study the pass-through of taxation levied on soft drinks. To do so we empirically analyse price changes when major changes in the sales tax on soda occur. We find that small stores exhibit a smaller pass-through than their larger counterparts. This is consistent with a simple theoretical model in which capacity constrained retailers shift less of the tax burden to consumers than those stores for which the capacity constraint is not binding. We also observe different pass-through levels between stores in Washington, DC and in North Carolina. We think this might be due to the differences of an urban versus a rural setting; results from a theoretical framework support this interpretation, but more work has to be done to exclude alternative explanations. Overall we find that pass-through levels are highly dependent on the specifics of the setting. In future work we will investigate the major
influences in more detail.
Appendix A

Appendix to Chapter 1
Table A.1: Regression of Sale for FP Listings

<table>
<thead>
<tr>
<th>Variable</th>
<th>Coefficient</th>
<th>(Std. Err.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Relative Price</td>
<td>-0.020**</td>
<td>(0.001)</td>
</tr>
<tr>
<td>Fee dummy</td>
<td>0.028**</td>
<td>(0.003)</td>
</tr>
<tr>
<td>Seller with low feedback score</td>
<td>-0.160**</td>
<td>(0.011)</td>
</tr>
<tr>
<td>Dummy for 1 ticket</td>
<td>0.045*</td>
<td>(0.018)</td>
</tr>
<tr>
<td>Dummy for 2 tickets</td>
<td>0.057**</td>
<td>(0.014)</td>
</tr>
<tr>
<td>Dummy for 3 tickets</td>
<td>0.033*</td>
<td>(0.016)</td>
</tr>
<tr>
<td>Dummy for 4 tickets</td>
<td>0.060**</td>
<td>(0.015)</td>
</tr>
<tr>
<td>Dummy for 5 tickets</td>
<td>-0.024</td>
<td>(0.020)</td>
</tr>
<tr>
<td>1 day prior to game</td>
<td>0.313**</td>
<td>(0.012)</td>
</tr>
<tr>
<td>2 days prior to game</td>
<td>0.331**</td>
<td>(0.012)</td>
</tr>
<tr>
<td>3 days prior to game</td>
<td>0.324**</td>
<td>(0.012)</td>
</tr>
<tr>
<td>4-8 days prior to game</td>
<td>0.274**</td>
<td>(0.010)</td>
</tr>
<tr>
<td>9-15 days prior to game</td>
<td>0.207**</td>
<td>(0.009)</td>
</tr>
<tr>
<td>16-20 days prior to game</td>
<td>0.145**</td>
<td>(0.010)</td>
</tr>
<tr>
<td>21-30 days prior to game</td>
<td>0.096**</td>
<td>(0.009)</td>
</tr>
<tr>
<td>31-40 days prior to game</td>
<td>0.060**</td>
<td>(0.010)</td>
</tr>
<tr>
<td>41-60 days prior to game</td>
<td>0.030**</td>
<td>(0.009)</td>
</tr>
<tr>
<td>More than 60 days prior to game</td>
<td>0.007</td>
<td>(0.010)</td>
</tr>
<tr>
<td>Number of competing listings</td>
<td>-0.001**</td>
<td>(0.000)</td>
</tr>
<tr>
<td>Average relative fixed price</td>
<td>0.045**</td>
<td>(0.003)</td>
</tr>
<tr>
<td>Average relative auction reserve price</td>
<td>-0.001</td>
<td>(0.003)</td>
</tr>
<tr>
<td>Average relative reserve price in BIN</td>
<td>0.004</td>
<td>(0.003)</td>
</tr>
<tr>
<td>Constant</td>
<td>-0.023</td>
<td>(0.018)</td>
</tr>
</tbody>
</table>

Number of observations: 76982

Notes: ** indicates significance at 99% level.
* indicates significance at 95% level.
† indicates significance at 90% level.
<table>
<thead>
<tr>
<th>Variable</th>
<th>Coefficient</th>
<th>(Std. Err.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Relative Price</td>
<td>-0.122**</td>
<td>(0.001)</td>
</tr>
<tr>
<td>Fee dummy</td>
<td>0.065**</td>
<td>(0.002)</td>
</tr>
<tr>
<td>Seller with low feedback score</td>
<td>-0.164**</td>
<td>(0.003)</td>
</tr>
<tr>
<td>Dummy for 1 ticket</td>
<td>-0.315**</td>
<td>(0.020)</td>
</tr>
<tr>
<td>Dummy for 2 tickets</td>
<td>-0.149**</td>
<td>(0.013)</td>
</tr>
<tr>
<td>Dummy for 3 tickets</td>
<td>-0.103**</td>
<td>(0.016)</td>
</tr>
<tr>
<td>Dummy for 4 tickets</td>
<td>-0.070**</td>
<td>(0.014)</td>
</tr>
<tr>
<td>Dummy for 5 tickets</td>
<td>-0.068**</td>
<td>(0.022)</td>
</tr>
<tr>
<td>1 day prior to game</td>
<td>-0.276**</td>
<td>(0.024)</td>
</tr>
<tr>
<td>2 days prior to game</td>
<td>0.046**</td>
<td>(0.009)</td>
</tr>
<tr>
<td>3 days prior to game</td>
<td>0.020*</td>
<td>(0.009)</td>
</tr>
<tr>
<td>4-8 days prior to game</td>
<td>0.075**</td>
<td>(0.008)</td>
</tr>
<tr>
<td>9-15 days prior to game</td>
<td>0.108**</td>
<td>(0.007)</td>
</tr>
<tr>
<td>16-20 days prior to game</td>
<td>0.106**</td>
<td>(0.008)</td>
</tr>
<tr>
<td>21-30 days prior to game</td>
<td>0.092**</td>
<td>(0.007)</td>
</tr>
<tr>
<td>31-40 days prior to game</td>
<td>0.069**</td>
<td>(0.008)</td>
</tr>
<tr>
<td>41-60 days prior to game</td>
<td>0.043**</td>
<td>(0.007)</td>
</tr>
<tr>
<td>More than 60 days prior to game</td>
<td>0.005</td>
<td>(0.008)</td>
</tr>
<tr>
<td>Number of competing listings</td>
<td>-0.001**</td>
<td>(0.000)</td>
</tr>
<tr>
<td>Average relative fixed price</td>
<td>0.020**</td>
<td>(0.002)</td>
</tr>
<tr>
<td>Average relative auction reserve price</td>
<td>-0.012**</td>
<td>(0.002)</td>
</tr>
<tr>
<td>Average relative reserve price in BIN</td>
<td>0.024**</td>
<td>(0.002)</td>
</tr>
<tr>
<td>Constant</td>
<td>0.717**</td>
<td>(0.016)</td>
</tr>
</tbody>
</table>

Number of observations: 187908

Notes: ** indicates significance at 99% level.
* indicates significance at 95% level.
† indicates significance at 90% level.
Table A.3: Regression of Sale for BIN Auctions

<table>
<thead>
<tr>
<th>Variable</th>
<th>Coefficient</th>
<th>(Std. Err.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Relative Price</td>
<td>-0.085**</td>
<td>(0.001)</td>
</tr>
<tr>
<td>Fee dummy</td>
<td>0.050**</td>
<td>(0.003)</td>
</tr>
<tr>
<td>Seller with low feedback score</td>
<td>-0.191**</td>
<td>(0.006)</td>
</tr>
<tr>
<td>Dummy for 1 ticket</td>
<td>-0.147**</td>
<td>(0.024)</td>
</tr>
<tr>
<td>Dummy for 2 tickets</td>
<td>0.013</td>
<td>(0.020)</td>
</tr>
<tr>
<td>Dummy for 3 tickets</td>
<td>0.046*</td>
<td>(0.022)</td>
</tr>
<tr>
<td>Dummy for 4 tickets</td>
<td>0.090**</td>
<td>(0.020)</td>
</tr>
<tr>
<td>Dummy for 5 tickets</td>
<td>0.078**</td>
<td>(0.026)</td>
</tr>
<tr>
<td>1 day prior to game</td>
<td>0.115**</td>
<td>(0.013)</td>
</tr>
<tr>
<td>2 days prior to game</td>
<td>0.146**</td>
<td>(0.013)</td>
</tr>
<tr>
<td>3 days prior to game</td>
<td>0.155**</td>
<td>(0.013)</td>
</tr>
<tr>
<td>4-8 days prior to game</td>
<td>0.161**</td>
<td>(0.012)</td>
</tr>
<tr>
<td>9-15 days prior to game</td>
<td>0.154**</td>
<td>(0.012)</td>
</tr>
<tr>
<td>16-20 days prior to game</td>
<td>0.141**</td>
<td>(0.012)</td>
</tr>
<tr>
<td>21-30 days prior to game</td>
<td>0.098**</td>
<td>(0.012)</td>
</tr>
<tr>
<td>31-40 days prior to game</td>
<td>0.088**</td>
<td>(0.013)</td>
</tr>
<tr>
<td>41-60 days prior to game</td>
<td>0.057**</td>
<td>(0.013)</td>
</tr>
<tr>
<td>More than 60 days prior to game</td>
<td>0.019</td>
<td>(0.014)</td>
</tr>
<tr>
<td>Number of competing listings</td>
<td>-0.001**</td>
<td>(0.000)</td>
</tr>
<tr>
<td>Average relative fixed price</td>
<td>0.038**</td>
<td>(0.002)</td>
</tr>
<tr>
<td>Average relative auction reserve price</td>
<td>0.005†</td>
<td>(0.003)</td>
</tr>
<tr>
<td>Average relative reserve price in BIN</td>
<td>0.033**</td>
<td>(0.003)</td>
</tr>
<tr>
<td>Constant</td>
<td>0.297**</td>
<td>(0.024)</td>
</tr>
</tbody>
</table>

Number of observations 131306

Notes: ** indicates significance at 99% level.
* indicates significance at 95% level.
† indicates significance at 90% level.
<table>
<thead>
<tr>
<th>Variable</th>
<th>Coefficient</th>
<th>(Std. Err.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Relative Price</td>
<td>-5.713**</td>
<td>(0.205)</td>
</tr>
<tr>
<td>Fee dummy</td>
<td>10.956**</td>
<td>(0.374)</td>
</tr>
<tr>
<td>Seller with low feedback score</td>
<td>-12.600**</td>
<td>(0.622)</td>
</tr>
<tr>
<td>Dummy for 1 ticket</td>
<td>-156.872**</td>
<td>(3.694)</td>
</tr>
<tr>
<td>Dummy for 2 tickets</td>
<td>-89.040**</td>
<td>(2.475)</td>
</tr>
<tr>
<td>Dummy for 3 tickets</td>
<td>-62.419**</td>
<td>(2.978)</td>
</tr>
<tr>
<td>Dummy for 4 tickets</td>
<td>-20.924**</td>
<td>(2.551)</td>
</tr>
<tr>
<td>Dummy for 5 tickets</td>
<td>-13.596**</td>
<td>(4.122)</td>
</tr>
<tr>
<td>1 day prior to game</td>
<td>-19.255**</td>
<td>(4.479)</td>
</tr>
<tr>
<td>2 days prior to game</td>
<td>13.245**</td>
<td>(1.652)</td>
</tr>
<tr>
<td>3 days prior to game</td>
<td>11.230**</td>
<td>(1.706)</td>
</tr>
<tr>
<td>4-8 days prior to game</td>
<td>17.508**</td>
<td>(1.385)</td>
</tr>
<tr>
<td>9-15 days prior to game</td>
<td>18.956**</td>
<td>(1.368)</td>
</tr>
<tr>
<td>16-20 days prior to game</td>
<td>17.192**</td>
<td>(1.392)</td>
</tr>
<tr>
<td>21-30 days prior to game</td>
<td>15.787**</td>
<td>(1.348)</td>
</tr>
<tr>
<td>31-40 days prior to game</td>
<td>14.639**</td>
<td>(1.408)</td>
</tr>
<tr>
<td>41-60 days prior to game</td>
<td>9.608**</td>
<td>(1.377)</td>
</tr>
<tr>
<td>More than 60 days prior to game</td>
<td>2.871†</td>
<td>(1.498)</td>
</tr>
<tr>
<td>Number of competing listings</td>
<td>-0.057**</td>
<td>(0.008)</td>
</tr>
<tr>
<td>Average relative fixed price</td>
<td>13.612**</td>
<td>(0.313)</td>
</tr>
<tr>
<td>Average relative auction reserve price</td>
<td>0.515</td>
<td>(0.433)</td>
</tr>
<tr>
<td>Average relative reserve price in BIN</td>
<td>11.441**</td>
<td>(0.376)</td>
</tr>
<tr>
<td>Constant</td>
<td>76.246**</td>
<td>(2.856)</td>
</tr>
</tbody>
</table>

Number of observations: 187908

Notes: ** indicates significance at 99% level.
* indicates significance at 95% level.
† indicates significance at 90% level.
Table A.5: Regression of Revenue for BIN Auctions

<table>
<thead>
<tr>
<th>Variable</th>
<th>Coefficient</th>
<th>(Std. Err.)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Relative Price</td>
<td>-3.631**</td>
<td>(0.213)</td>
</tr>
<tr>
<td>Fee dummy</td>
<td>9.006**</td>
<td>(0.522)</td>
</tr>
<tr>
<td>Seller with low feedback score</td>
<td>-17.562**</td>
<td>(1.141)</td>
</tr>
<tr>
<td>Dummy for 1 ticket</td>
<td>-107.330**</td>
<td>(4.862)</td>
</tr>
<tr>
<td>Dummy for 2 tickets</td>
<td>-53.763**</td>
<td>(4.015)</td>
</tr>
<tr>
<td>Dummy for 3 tickets</td>
<td>-37.307**</td>
<td>(4.382)</td>
</tr>
<tr>
<td>Dummy for 4 tickets</td>
<td>-1.018</td>
<td>(4.085)</td>
</tr>
<tr>
<td>Dummy for 5 tickets</td>
<td>-4.320</td>
<td>(5.335)</td>
</tr>
<tr>
<td>1 day prior to game</td>
<td>15.721**</td>
<td>(2.492)</td>
</tr>
<tr>
<td>2 days prior to game</td>
<td>20.353**</td>
<td>(2.499)</td>
</tr>
<tr>
<td>3 days prior to game</td>
<td>23.628**</td>
<td>(2.515)</td>
</tr>
<tr>
<td>4-8 days prior to game</td>
<td>26.371**</td>
<td>(2.349)</td>
</tr>
<tr>
<td>9-15 days prior to game</td>
<td>23.847**</td>
<td>(2.246)</td>
</tr>
<tr>
<td>16-20 days prior to game</td>
<td>23.269**</td>
<td>(2.243)</td>
</tr>
<tr>
<td>21-30 days prior to game</td>
<td>17.263**</td>
<td>(2.383)</td>
</tr>
<tr>
<td>31-40 days prior to game</td>
<td>18.513**</td>
<td>(2.517)</td>
</tr>
<tr>
<td>41-60 days prior to game</td>
<td>12.697**</td>
<td>(2.520)</td>
</tr>
<tr>
<td>More than 60 days prior to game</td>
<td>6.154*</td>
<td>(2.801)</td>
</tr>
<tr>
<td>Number of competing listings</td>
<td>-0.112**</td>
<td>(0.007)</td>
</tr>
<tr>
<td>Average relative fixed price</td>
<td>18.562**</td>
<td>(0.338)</td>
</tr>
<tr>
<td>Average relative auction reserve price</td>
<td>4.773**</td>
<td>(0.555)</td>
</tr>
<tr>
<td>Average relative reserve price in BIN</td>
<td>10.951**</td>
<td>(0.494)</td>
</tr>
<tr>
<td>Constant</td>
<td>28.284**</td>
<td>(4.655)</td>
</tr>
</tbody>
</table>

Number of observations: 131306

Notes: ** indicates significance at 99% level.
* indicates significance at 95% level.
† indicates significance at 90% level.
Appendix B
Appendix to Chapter 2

B.1 Proof of Proposition 1

Proof. The second part of the proposition is trivially true since in the case of $p_l = r_l$ the BIN purchase is a weakly dominant strategy. Hence, I can now concentrate on the first part of the proposition and the more interesting case $p_l > r_l$. I show the proof for the case of a neutral bidder 1. If bidder 1 is an FP lover, the same steps are sufficient to complete the proof. However, the notation is slightly more tedious since in this case a distinction has to be made between the valuation for buying in the auction and buying at the BIN price.

The proof proceeds in the following steps. First, I derive expressions for bidder 1’s profit from a BIN purchase ($\pi_{BIN}(v)$) and his expected profit from starting the auction ($\pi_a(v)$). Then I will note that both of these expressions are continuous in $v$. 88
After that I will show that there always exists a $v$ for which the auction is preferable.

Finally, I’ll show that if the BIN purchase is chosen for one $v$ it is also chosen for all $v' > v$ in the support.

Step 1:

Let $G(x)$ be the probability distribution over the highest competing bid from bidder 1’s perspective, let $g(x)$ be its derivative, and let $\chi$ be its support. Then $\pi_{BIN}(v)$ and $\pi_a(v)$ can be written as:

$$\pi_{BIN}(v) = v - p_{BIN}$$

$$\pi_a(v) = \int_r^v (v - x)g(x)dx$$

$$= \int_r^v vg(x)dx - \int_r^v xg(x)dx$$

$$= v(G(v) - G(r)) - \int_r^v xg(x)dx$$

Step 2:

Clearly, $\pi_{BIN}(v)$ and $\pi_a(v)$ are continuous because they are sums of continuous functions.

Step 3:

Clearly, $\pi_a(v) > \pi_{BIN}(v) \forall r \leq v < p_{BIN}$ since the profit from BIN purchase is
negative for these valuations.

Step 4:

I will now show that if $\pi_{BIN}(v) \geq \pi_a(v)$ then $\frac{1}{v} v' > v$ in $\chi$ such that $\pi_{BIN}(v') \leq \pi_a(v')$. Assume $\pi_{BIN}(v) \geq \pi_a(v)$ for some $v$ with $G(v) < 1$ (with $G(v) = 1$ there is no greater $v$ in the support, so the claim is immediately true). I will show that $\pi_{BIN}(v') > \pi_a(v')$ for all $v' > v$. Let $\delta \equiv v' - v > 0$. I can then write:

$$\pi_{BIN}(v') = v + \delta - p_{BIN} \geq \delta + [G(v) - G(r)]v - \int_v^{v'} xg(x)dx$$

$$= [1 - (G(v) - G(r))]\delta + [G(v) - G(r)]v' - \int_r^{v'} xg(x)dx$$

$$= [1 - (G(v) - G(r))]\delta + [G(v) - G(v')]v'$$

$$+ [G(v') - G(r)]v' - \int_r^{v'} xg(x)dx$$

$$= [1 - (G(v) - G(r))]\delta + [G(v) - G(v')]v'$$

$$+ [G(v) - G(r)]v' - \int_r^{v'} xg(x)dx$$

$$= [1 - (G(v) - G(r))]\delta + [G(v) - G(v')]v'$$

$$+ \int_v^{v'} xg(x)dx + \pi_a(v')$$

Now I only have to show that $A \equiv [1 - (G(v) - G(r))]\delta + [G(v) - G(v')]v' + \int_v^{v'} xg(x)dx > 0$. For this, note that $\int_v^{v'} xg(x)dx \geq v\int_v^{v'} g(x)dx = v[G(v') - G(v)]$.

The inequality holds because on the left-hand side $g(x)$ is multiplied by values ever
increasing from their start point $v$ while on the right-hand side each $g(x)$ is just multiplied by $v$. This allows me to write:

$$A \geq [1 - (G(v) - G(r))] \delta + [G(v) - G(v')] v' + v[G(v') - G(v)]$$

$$= [1 - (G(v) - G(r))] \delta + (v' - v)[G(v) - G(v')]$$

$$= [1 - G(v) + G(r)] \delta + \delta[G(v) - G(v')]$$

$$= \delta[1 + G(r) - G(v')]$$

$$\geq 0$$

The last inequality holds because $\delta > 0$ and because $G(x)$ is a cdf, implying $G(v') - G(r) \leq 1$. Note that the equality can only be reached if $G(v') = 1$; so if $G(v') < 1$ we know that $A > 0$ and we are done. If $G(v') = 1$ then we only know $\pi_{BIN}(v') \geq \pi_a(v')$, so the choice of bidder 1 could change if he is indifferent for both $v$ and $v'$. However, by continuity of $G$ there is a $v''$ between $v$ and $v'$ such that $G(v'') < 1$. Since $G(v'') < 1$, the inequalities hold strictly for comparing choices at $v$ and $v''$ (i.e. $A > 0$), thus proving that $\pi_{BIN}(v'') > \pi_a(v'')$. Now compare choices at $v''$ and $v'$. In this case $A$ might be equal to zero. However, the first inequality in step 4 is strict because we know that $\pi_{BIN}(v'') > \pi_a(v'')$; thus, $\pi_{BIN}(v') > \pi_a(v')$. □
B.2 Data Cleaning

Originally I have data for all 81 home games of the Cincinnati Reds in the 2007 regular season. There are 16,812 listings with a total of 18,875 bids and the number of tickets per listing range from one to six. In order to get a more uniform dataset and because I do not believe that there is much competition between listings with different ticket numbers I keep only listings offering exactly two tickets. The market for pairs of tickets is the thickest, leaving me with 14,309 listings and 15,919 bids.

I drop all listings for the first three games of the season. The beginning of a new season seems to have spurred excitement among baseball fans; thus, these games drew much more interest than others in my sample. In fact, they account for 29.6% of listings and 46.0% of bids in the data, leaving me to believe that the market for these tickets was significantly different from the one for later games. For a similar reason I drop listings for tickets in the “Diamond Seats” section immediately behind the home plate (these are sections 1-6 in figure B.1). These tickets are significantly superior to others, but account for only a small number of sales (less than 0.6% of listings and less than 1.0% of bids). Thus, dropping these listings allows me to concentrate on the effects that drive competition between more common listings without creating a major misrepresentation of the market.

I now drop all listings that end more than 40 days before the game (17.3% of
listings). The early markets are relatively thin compared to those closer to the event; thus I am concerned that the competitive situation is significantly different in this period. Next I drop a few bids (2.8%) for which the bid type in the data signal problems. These are bids that are listed as “Auto Retracted” (47 bids), “Auto Cancelled” (136 bids) or “Motors” (1 bid). I also drop listings that I consider problematic. First, there are 149 listings which sell for less than the listed price. Secondly, I drop 138 listings for which the seat row is missing. This information is essential since in the estimation I use it as one of my covariates. At this point my data still contains rare listing types, namely 27 cases of multi-unit auctions and 74 personal offers, which I also drop in order to focus on the three major mechanisms auction, FP listings and BIN. Now I remove likely resellers of tickets. I do this because resellers face a very different problem from buyers who purchase for personal use. First, in my model I assume that buyers have independent private values; for resellers this assumption is questionable since holding the ticket has no value per se. Second, resellers are likely to be in the market for extended periods of time, while I assume that my buyers are short-lived and only active for one period. In order to eliminate resellers, I drop all bids by buyers who buy more than four pairs of tickets for a single game (0.9% of bids). Furthermore, I do not observe secret reserve prices. Since these might influence bidding and certainly have an impact on sellers’ revenue expectations I drop all
listings with secret reserve prices (1.2% of listings).

Most listings in the data are available for no more than one week. However, there are some cases of extremely long listings, in very few cases reaching more than 200 days. In order to remove this kind of variation I drop listings lasting more than 10 days (4.2%). After this I finally end up with 7,430 bids and 7,382 listings left.
### B.3 Tables and Figures

Table B.1: Summary Statistics for listings by mechanism type.

<table>
<thead>
<tr>
<th></th>
<th>Auctions mean</th>
<th>Auctions std. dev.</th>
<th>FP listings mean</th>
<th>FP listings std. dev.</th>
<th>BIN auctions mean</th>
<th>BIN auctions std. dev.</th>
</tr>
</thead>
<tbody>
<tr>
<td>face value</td>
<td>25.87</td>
<td>12.86</td>
<td>27.72</td>
<td>9.63</td>
<td>31.07</td>
<td>13.70</td>
</tr>
<tr>
<td>game quality</td>
<td>0.410</td>
<td>0.245</td>
<td>0.434</td>
<td>0.248</td>
<td>0.447</td>
<td>0.248</td>
</tr>
<tr>
<td>section quality</td>
<td>0.251</td>
<td>0.177</td>
<td>0.288</td>
<td>0.163</td>
<td>0.319</td>
<td>0.193</td>
</tr>
<tr>
<td>row quality</td>
<td>0.646</td>
<td>0.295</td>
<td>0.675</td>
<td>0.289</td>
<td>0.568</td>
<td>0.315</td>
</tr>
<tr>
<td>start price</td>
<td>22.68</td>
<td>30.11</td>
<td>73.12</td>
<td>57.05</td>
<td>68.74</td>
<td>66.95</td>
</tr>
<tr>
<td>BIN price</td>
<td>N/A</td>
<td>N/A</td>
<td>N/A</td>
<td>96.33</td>
<td>73.36</td>
<td></td>
</tr>
<tr>
<td>low seller score</td>
<td>0.060</td>
<td>0.237</td>
<td>0.017</td>
<td>0.129</td>
<td>0.046</td>
<td>0.210</td>
</tr>
<tr>
<td>“advertising”</td>
<td>0.534</td>
<td>0.772</td>
<td>0.239</td>
<td>0.497</td>
<td>0.526</td>
<td>0.899</td>
</tr>
<tr>
<td>length in days</td>
<td>4.581</td>
<td>2.475</td>
<td>4.717</td>
<td>2.424</td>
<td>3.541</td>
<td>2.529</td>
</tr>
<tr>
<td>number of bids</td>
<td>1.554</td>
<td>1.849</td>
<td>N/A</td>
<td>0.540</td>
<td>0.937</td>
<td></td>
</tr>
<tr>
<td>sale probability</td>
<td>0.589</td>
<td>0.215</td>
<td>0.215</td>
<td>0.361</td>
<td></td>
<td></td>
</tr>
<tr>
<td>revenue in case of sale</td>
<td>40.27</td>
<td>39.98</td>
<td>68.92</td>
<td>39.67</td>
<td>69.24</td>
<td>57.00</td>
</tr>
<tr>
<td>number of listings</td>
<td>3,698</td>
<td>890</td>
<td>2,794</td>
<td>95</td>
<td>3.698</td>
<td>890</td>
</tr>
</tbody>
</table>

Table B.2: Grouping of rows and row quality index.

The rows are counted from the field, so that in each section the row closest to the field is assigned number 1.

<table>
<thead>
<tr>
<th>Group</th>
<th>Rows</th>
<th>Row Quality</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>2</td>
<td>2-3</td>
<td>0.870</td>
</tr>
<tr>
<td>3</td>
<td>4-10</td>
<td>0.655</td>
</tr>
<tr>
<td>4</td>
<td>11-19</td>
<td>0.463</td>
</tr>
<tr>
<td>5</td>
<td>20-26</td>
<td>0.238</td>
</tr>
<tr>
<td>6</td>
<td>27+</td>
<td>0</td>
</tr>
</tbody>
</table>
Table B.3: Grouping of sections and section quality index.

<table>
<thead>
<tr>
<th>Group</th>
<th>Section</th>
<th>Section Quality</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>22-25</td>
<td>1</td>
</tr>
<tr>
<td>2</td>
<td>122-126</td>
<td>0.585</td>
</tr>
<tr>
<td>3</td>
<td>110-113, 133-136</td>
<td>0.420</td>
</tr>
<tr>
<td>4</td>
<td>114, 115, 131, 132</td>
<td>0.471</td>
</tr>
<tr>
<td>5</td>
<td>116-118, 129-130</td>
<td>0.485</td>
</tr>
<tr>
<td>6</td>
<td>119-121, 127-128</td>
<td>0.517</td>
</tr>
<tr>
<td>7</td>
<td>108-109, 137-139</td>
<td>0.303</td>
</tr>
<tr>
<td>8</td>
<td>140-146</td>
<td>0.192</td>
</tr>
<tr>
<td>9</td>
<td>101-107</td>
<td>0.146</td>
</tr>
<tr>
<td>10</td>
<td>401-406</td>
<td>0.019</td>
</tr>
<tr>
<td>11</td>
<td>408-410</td>
<td>0</td>
</tr>
<tr>
<td>12</td>
<td>411-414</td>
<td>0.121</td>
</tr>
<tr>
<td>13</td>
<td>415-419</td>
<td>0.175</td>
</tr>
<tr>
<td>14</td>
<td>220-228, 301-307</td>
<td>0.257</td>
</tr>
<tr>
<td>15</td>
<td>420-431</td>
<td>0.231</td>
</tr>
<tr>
<td>16</td>
<td>432-437</td>
<td>0.104</td>
</tr>
<tr>
<td>17</td>
<td>509+</td>
<td>0.022</td>
</tr>
</tbody>
</table>
Figure B.1: Section plan of the Great American Ballpark.
Source: http://www.ticketsolutions.com/
Figure B.2: Average number of available listings over time
Figure B.3: Development of mechanism choice over time
Figure B.4: Timing of bids during the last five days of the auction.
Table B.4: Estimates of demand side parameters.

Standard deviations in parentheses. All estimates are significant at the 99% level.

<table>
<thead>
<tr>
<th>Days before game</th>
<th>1-10</th>
<th>11-20</th>
<th>21-40</th>
</tr>
</thead>
<tbody>
<tr>
<td>Constant $\beta_1$</td>
<td>-22.4589</td>
<td>-27.0525</td>
<td>-22.4055</td>
</tr>
<tr>
<td></td>
<td>(0.0005)</td>
<td>(0.0028)</td>
<td>(0.0021)</td>
</tr>
<tr>
<td>Game quality $\beta_2$</td>
<td>58.2609</td>
<td>49.5130</td>
<td>43.4314</td>
</tr>
<tr>
<td></td>
<td>(0.0006)</td>
<td>(0.0034)</td>
<td>(0.0021)</td>
</tr>
<tr>
<td>Row quality $\beta_3$</td>
<td>9.7331</td>
<td>10.4477</td>
<td>8.2725</td>
</tr>
<tr>
<td></td>
<td>(0.0007)</td>
<td>(0.0048)</td>
<td>(0.0024)</td>
</tr>
<tr>
<td>Section quality $\beta_4$</td>
<td>119.2380</td>
<td>112.7180</td>
<td>105.0501</td>
</tr>
<tr>
<td></td>
<td>(0.0006)</td>
<td>(0.0114)</td>
<td>(0.0019)</td>
</tr>
<tr>
<td>Low seller score $\beta_5$</td>
<td>-6.0248</td>
<td>-5.5073</td>
<td>-5.3684</td>
</tr>
<tr>
<td></td>
<td>(0.0059)</td>
<td>(0.3230)</td>
<td>(0.2735)</td>
</tr>
<tr>
<td>“advertising” $\beta_6$</td>
<td>2.6001</td>
<td>3.1460</td>
<td>2.8735</td>
</tr>
<tr>
<td></td>
<td>(0.0034)</td>
<td>(0.0175)</td>
<td>(0.0185)</td>
</tr>
<tr>
<td>FP preference $c$</td>
<td>23.8230</td>
<td>24.1303</td>
<td>21.7427</td>
</tr>
<tr>
<td></td>
<td>(0.0126)</td>
<td>(0.0486)</td>
<td>(0.0680)</td>
</tr>
<tr>
<td>Share of FP lovers $\lambda$</td>
<td>0.3229</td>
<td>0.2604</td>
<td>0.2908</td>
</tr>
<tr>
<td></td>
<td>(0.0029)</td>
<td>(0.0136)</td>
<td>(0.0254)</td>
</tr>
<tr>
<td>Arrival prob. (const.) $\alpha_0$</td>
<td>-2.6806</td>
<td>-3.4493</td>
<td>-4.1185</td>
</tr>
<tr>
<td></td>
<td>(0.0016)</td>
<td>(0.0208)</td>
<td>(0.0227)</td>
</tr>
<tr>
<td>Arrival prob. (game qual.) $\alpha_1$</td>
<td>0.2837</td>
<td>0.2486</td>
<td>0.2176</td>
</tr>
<tr>
<td></td>
<td>(0.0089)</td>
<td>(0.0324)</td>
<td>(0.0356)</td>
</tr>
<tr>
<td>Std. dev. of valuations $\sigma$</td>
<td>15.4842</td>
<td>19.2504</td>
<td>23.8347</td>
</tr>
<tr>
<td></td>
<td>(0.0005)</td>
<td>(0.0066)</td>
<td>(0.0022)</td>
</tr>
</tbody>
</table>

Observations 4,584 1,606 1,192

Table B.5: Predicted moments for several values of $N$.

Reported are the average predicted moments for 100 game/day combinations between 21 and 40 days before the game. Predictions based on 100,000 simulations for each listing.

<table>
<thead>
<tr>
<th>$N$</th>
<th>100</th>
<th>200</th>
<th>300</th>
<th>400</th>
</tr>
</thead>
<tbody>
<tr>
<td>Auctions</td>
<td>Exp. Revenue</td>
<td>12.79</td>
<td>12.62</td>
<td>12.69</td>
</tr>
<tr>
<td></td>
<td>Sale Probability</td>
<td>0.4755</td>
<td>0.4732</td>
<td>0.4740</td>
</tr>
<tr>
<td>FP listings</td>
<td>Exp. Revenue</td>
<td>6.17</td>
<td>6.03</td>
<td>6.16</td>
</tr>
<tr>
<td></td>
<td>Sale Probability</td>
<td>0.2144</td>
<td>0.2119</td>
<td>0.2139</td>
</tr>
<tr>
<td>BIN Auctions</td>
<td>Exp. Revenue</td>
<td>8.47</td>
<td>8.31</td>
<td>8.37</td>
</tr>
<tr>
<td></td>
<td>Sale Probability</td>
<td>0.2018</td>
<td>0.1994</td>
<td>0.2000</td>
</tr>
</tbody>
</table>
Table B.6: Predicted and true values for the share of sold items and expected revenue by mechanism.

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>FP listings</td>
<td>0.215</td>
<td>13.75</td>
<td>12.06</td>
</tr>
<tr>
<td>Auctions</td>
<td>0.589</td>
<td>23.99</td>
<td>24.47</td>
</tr>
<tr>
<td>BIN auctions</td>
<td>0.361</td>
<td>23.25</td>
<td>22.19</td>
</tr>
</tbody>
</table>

Table B.7: Mechanism choice by seller size

<table>
<thead>
<tr>
<th>Seller Size</th>
<th>FP listings</th>
<th>Auctions</th>
<th>BIN Auctions</th>
</tr>
</thead>
<tbody>
<tr>
<td>Small Sellers</td>
<td>6.63%</td>
<td>65.89%</td>
<td>27.48%</td>
</tr>
<tr>
<td>Large Sellers</td>
<td>21.69%</td>
<td>24.12%</td>
<td>54.20%</td>
</tr>
</tbody>
</table>

Figure B.5: Distribution of outside option values relative to face value by seller size
Table B.8: Risk attitudes by seller size

<table>
<thead>
<tr>
<th></th>
<th>( \xi = .01 )</th>
<th>( \xi = .1 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>small sellers</td>
<td>34.14%</td>
<td>26.36%</td>
</tr>
<tr>
<td>large sellers</td>
<td>63.66%</td>
<td>11.41%</td>
</tr>
</tbody>
</table>

Figure B.6: Distribution of small sellers’ outside option values relative to face value by mechanism.

Table B.9: Development of outside options over time

<table>
<thead>
<tr>
<th>Days to game</th>
<th>Small Sellers</th>
<th>Large Sellers</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>mean</td>
<td>std. dev.</td>
</tr>
<tr>
<td>21-40</td>
<td>0.2248</td>
<td>1.0769</td>
</tr>
<tr>
<td>11-20</td>
<td>0.2066</td>
<td>0.9982</td>
</tr>
<tr>
<td>1-10</td>
<td>0.0851</td>
<td>1.0961</td>
</tr>
</tbody>
</table>
Figure B.7: Distribution of large sellers’ outside option values relative to face value by mechanism.

Table B.10: Development of several measures of ticket quality over time

<table>
<thead>
<tr>
<th>Days before Game</th>
<th>1-10</th>
<th>11-20</th>
<th>21-40</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>mean</td>
<td>std. dev.</td>
<td>mean</td>
</tr>
<tr>
<td>face value</td>
<td>27.8654</td>
<td>13.3834</td>
<td>27.9572</td>
</tr>
<tr>
<td>game quality</td>
<td>0.4327</td>
<td>0.2485</td>
<td>0.4202</td>
</tr>
<tr>
<td>row quality</td>
<td>0.6233</td>
<td>0.2951</td>
<td>0.6221</td>
</tr>
<tr>
<td>section quality</td>
<td>0.2800</td>
<td>0.1906</td>
<td>0.2833</td>
</tr>
</tbody>
</table>

Table B.11: Estimated distributions for sellers’ mechanism costs

<table>
<thead>
<tr>
<th>small sellers</th>
<th>large sellers</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\mu_{\text{BIN}}$</td>
<td>0.3485</td>
</tr>
<tr>
<td>$\sigma_{\text{BIN}}$</td>
<td>0.3853</td>
</tr>
<tr>
<td>$\mu_{\text{Auction}}$</td>
<td>-0.3223</td>
</tr>
<tr>
<td>$\sigma_{\text{Auction}}$</td>
<td>0.2190</td>
</tr>
</tbody>
</table>
Bibliography


Biography

Christoph Bauner was born in Würzburg, Germany on April 25, 1978. He attended Bayerische Julius-Maximilians-Universität Würzburg from 1997 to 2001. After visiting the University of Texas at Austin as an exchange student from 2000 to 2001 he transferred to Universität Mannheim where he earned his Diplom in Volkswirtschaftslehre (equivalent to M.A. in Economics) in 2004. From 2004 to 2005 Christoph held a position as Wissenschaftlicher Mitarbeiter at Universität Mannheim. After that he attended Duke University where he received an M.A. in Economics in 2008. He is graduating with a Ph.D. in Economics in 2011.